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978-1-316-60195-2 - Geometry in a Fréchet Context: A Projective Limit Approach

C. T. J. Dodson, George Galanis and Efstathios Vassiliou

Table of Contents

[More information](#)

Contents

	<i>Preface</i>	<i>page</i> vii
1	Banach manifolds and bundles	1
	1.1 Banach manifolds	1
	1.2 Banach-Lie groups	7
	1.3 Smooth actions	12
	1.4 Banach vector bundles	14
	1.5 Connections on vector bundles	27
	1.6 Banach principal bundles	37
	1.7 Connections on principal bundles	53
	1.8 The curvature of a principal connection	63
	1.9 Holonomy groups	67
	1.10 Classification of flat bundles	71
2	Fréchet spaces	73
	2.1 The topology of Fréchet spaces	73
	2.2 Differentiability	79
	2.3 Fréchet spaces as projective limits	82
	2.4 Differential equations in Fréchet spaces	99
3	Fréchet manifolds	105
	3.1 Smooth structures on Fréchet manifolds	106
	3.2 The tangent bundle of a plb-manifold	111
	3.3 Vector fields	119
	3.4 Fréchet-Lie groups	121
	3.5 Equations with Maurer-Cartan differential	127
	3.6 Differential forms	131
4	Projective systems of principal bundles	139
	4.1 Projective systems and Fréchet principal bundles	139
	4.2 Connections on limit principal bundles	150

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Table of Contents

[More information](#)

vi

Contents

4.3	Parallel translations and holonomy groups	160
4.4	The curvature of a plb-connection	165
4.5	Flat plb-bundles	172
5	Projective systems of vector bundles	183
5.1	A particular Fréchet group	183
5.2	Projective systems and Fréchet vector bundles	185
5.3	Morphisms of plb-vector bundles	192
5.4	The sections of plb-vector bundles	198
5.5	The pull-back of plb-vector bundles	199
6	Examples of projective systems of bundles	207
6.1	Trivial examples of plb-vector bundles	207
6.2	Plb-vector bundles of maps	208
6.3	The infinite jet bundle	211
6.4	The tangent bundle of a plb-bundle	213
6.5	The generalized frame bundle	216
6.6	Generalized associated bundles	219
7	Connections on plb-vector bundles	225
7.1	Projective limits of linear connections	225
7.2	Parallel displacement and holonomy groups	231
7.3	Connections on plb-vector and frame bundles	237
8	Geometry of second order tangent bundles	245
8.1	The (first order) tangent bundle in brief	246
8.2	Second order tangent bundles	248
8.3	Second order differentials	253
8.4	Connection dependence	256
8.5	Second order Fréchet tangent bundles	257
8.6	Second order frame bundles	262
	<i>Appendix: Further study</i>	273
	<i>References</i>	281
	<i>List of Notations</i>	291
	<i>Subject index</i>	299