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978-1-316-51655-3 — Orthogonal Polynomials in the Spectral Analysis of Markov Processes

Manuel Domínguez de la Iglesia

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