

## Index

Page numbers for entries within a footnote are followed by an *n* and the footnote number; **bold** numbers indicate a term's definition. GR = General Relativity, SR = Special Relativity.

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