

Cambridge Elements =

Elements in Quantitative Finance edited by Riccardo Rebonato EDHEC Business School

A PRACTITIONER'S GUIDE TO DISCRETE-TIME YIELD CURVE MODELLING

WITH EMPIRICAL ILLUSTRATIONS AND MATLAB EXAMPLES

Ken Nyholm European Central Bank, Frankfurt





CAMBRIDGE UNIVERSITY PRESS

University Printing House, Cambridge CB2 8BS, United Kingdom One Liberty Plaza, 20th Floor, New York, NY 10006, USA 477 Williamstown Road, Port Melbourne, VIC 3207, Australia 314–321, 3rd Floor, Plot 3, Splendor Forum, Jasola District Centre, New Delhi – 110025, India

79 Anson Road, #06-04/06, Singapore 079906

Cambridge University Press is part of the University of Cambridge.

It furthers the University's mission by disseminating knowledge in the pursuit of education, learning, and research at the highest international levels of excellence.

www.cambridge.org
Information on this title: www.cambridge.org/9781108972123
DOI: 10.1017/9781108975537

© Ken Nvholm 2020

This publication is in copyright. Subject to statutory exception and to the provisions of relevant collective licensing agreements, no reproduction of any part may take place without the written permission of Cambridge University Press.

First published 2020

A catalogue record for this publication is available from the British Library.

ISBN 978-1-108-97212-3 Paperback ISSN 2631-8571 (online) ISSN 2631-8563 (print)

Additional resources for this publication at www.cambridge.org/nyholm

Cambridge University Press has no responsibility for the persistence or accuracy of URLs for external or third-party internet websites referred to in this publication and does not guarantee that any content on such websites is, or will remain, accurate or appropriate.



A Practitioner's Guide to Discrete-Time Yield Curve Modelling

With Empirical Illustrations and MATLAB Examples

Elements in Quantitative Finance

DOI: 10.1017/9781108975537 First published online: December 2020

Ken Nyholm European Central Bank, Frankfurt

Author for correspondence: Ken Nyholm, ken.nyholm@ecb.europa.eu

Abstract: This Element is intended for students and practitioners as a gentle and intuitive introduction to the field of discrete-time yield curve modelling. I strive to be as comprehensive as possible, while still adhering to the overall premise of putting a strong focus on practical applications. In addition to a thorough description of the Nelson-Siegel family of model, the Element contains a section on the intuitive relationship between P and Q measures, one on how the structure of a Nelson-Siegel model can be retained in the arbitrage-free framework, and a dedicated section that provides a detailed explanation for the Joslin, Singleton, and Zhu (2011) model.

Keywords: yield curve modelling, discrete-time, arbitrage-free models, Nelson-Siegel type models

JEL classifications: G1, E4, C5, C13

© Ken Nyholm 2020

ISBNs: 9781108972123 (PB), 9781108975537 (OC) ISSNs: 2631-8571 (online), 2631-8563 (print)



Contents

1	Empirical Analysis of Term Structure Data	1
2	${\mathbb P}$ and ${\mathbb Q}$ measures	23
3	The Basic Yield Curve Modelling Set-Up	43
4	Modelling Yields under the ${\mathbb Q}$ Measure	83
5	Model Implementation	97
6	Scenario Generation	106
	Appendix: On the Included MATLAB Codes and Scripts	137
	References	140