

## Bayesian Methods for Interaction and Design

Intended for researchers and practitioners in interaction design, this book shows how Bayesian models can be brought to bear on problems of interface design and user modelling. It introduces and motivates Bayesian modelling and illustrates how powerful these ideas can be in thinking about human–computer interaction, especially in representing and manipulating uncertainty. Bayesian methods are increasingly practical as computational tools to implement them become more widely available, and offer a principled foundation to reason about interaction design.

The book opens with a self-contained tutorial on Bayesian concepts and their practical implementation, tailored for the background and needs of interaction designers. The contributed chapters cover the use of Bayesian probabilistic modelling in a diverse set of applications, including improving pointing-based interfaces, efficient text entry using modern language models, advanced interface design using cutting-edge techniques in Bayesian optimisation, and Bayesian approaches to modelling the cognitive processes of users.

JOHN H. WILLIAMSON is Senior Lecturer in Computing Science at the University of Glasgow.

ANTTI OULASVIRTA is Professor of Electrical Engineering and leads the User Interfaces research group at Aalto University and the Interactive AI research program at the Finnish Center for AI.

PER OLA KRISTENSSON is Professor of Interactive Systems Engineering in the Department of Engineering at the University of Cambridge and a Fellow of Trinity College, Cambridge.

NIKOLA BANOVIC is Assistant Professor of Electrical Engineering and Computer Science at the University of Michigan–Ann Arbor.

# Bayesian Methods for Interaction and Design

*Edited by*

JOHN H. WILLIAMSON  
*University of Glasgow*

ANTTI OULASVIRTA  
*Aalto University*

PER OLA KRISTENSSON  
*University of Cambridge*

NIKOLA BANOVIC  
*University of Michigan–Ann Arbor*



CAMBRIDGE  
UNIVERSITY PRESS

Cambridge University Press & Assessment  
 978-1-108-83499-5 — Bayesian Methods for Interaction and Design  
 Edited by J.H. Williamson, A. Oulasvirta, P.O. Kristensson, N. Banovic  
 Frontmatter  
[More Information](#)

CAMBRIDGE  
 UNIVERSITY PRESS

University Printing House, Cambridge CB2 8BS, United Kingdom  
 One Liberty Plaza, 20th Floor, New York, NY 10006, USA  
 477 Williamstown Road, Port Melbourne, VIC 3207, Australia  
 314–321, 3rd Floor, Plot 3, Splendor Forum, Jasola District Centre,  
 New Delhi – 110025, India  
 103 Penang Road, #05–06/07, Visioncrest Commercial, Singapore 238467

Cambridge University Press is part of the University of Cambridge.

It furthers the University's mission by disseminating knowledge in the pursuit of education, learning, and research at the highest international levels of excellence.

[www.cambridge.org](http://www.cambridge.org)

Information on this title: [www.cambridge.org/9781108834995](http://www.cambridge.org/9781108834995)

DOI: 10.1017/9781108874830

© Cambridge University Press 2022

This publication is in copyright. Subject to statutory exception and to the provisions of relevant collective licensing agreements, no reproduction of any part may take place without the written permission of Cambridge University Press.

First published 2022

*A catalogue record for this publication is available from the British Library.*

*Library of Congress Cataloging-in-Publication Data*

Names: Williamson, John H., 1980– editor. | Oulasvirta, Antti, 1979– editor. | Kristensson, Per Ola, editor. | Banovic, Nikola, 1982– editor.

Title: Bayesian methods for interaction and design / edited by John H. Williamson, University of Glasgow, Antti Oulasvirta, Aalto University, Finland, Per Ola Kristensson, University of Cambridge, Nikola Banovic, University of Michigan, Ann Arbor.

Description: First edition. | Cambridge, United Kingdom ; New York, NY, USA : Cambridge University Press, 2022. | Includes bibliographical references.

Identifiers: LCCN 2022016991 (print) | LCCN 2022016992 (ebook) | ISBN 9781108834995 (hardback) | ISBN 9781108792707 (paperback) | ISBN 9781108874830 (epub)

Subjects: LCSH: Human-machine systems—Mathematical models. | Human engineering—Mathematics. | User interfaces (Computer systems) | Bayesian statistical decision theory. | BISAC: COMPUTERS / Social Aspects

Classification: LCC TA167 .B39 2022 (print) | LCC TA167 (ebook) | DDC 620.8/2—dc23/eng/20220602

LC record available at <https://lcn.loc.gov/2022016991>

LC ebook record available at <https://lcn.loc.gov/2022016992>

ISBN 978-1-108-83499-5 Hardback

ISBN 978-1-108-79270-7 Paperback

Cambridge University Press has no responsibility for the persistence or accuracy of URLs for external or third-party internet websites referred to in this publication and does not guarantee that any content on such websites is, or will remain, accurate or appropriate.

## Contents

<i>List of Contributors</i>	page vii
<i>Preface</i>	ix
<b>Part I Introduction to Bayesian Methods</b>	1
<b>1 An Introduction to Bayesian Methods for Interaction Design</b> <i>J. H. Williamson</i>	3
<b>2 Bayesian Statistics</b> <i>A. Dix</i>	81
<b>Part II Probabilistic Interfaces and Inference of Intent</b>	115
<b>3 Bayesian Information Gain to Design Interaction</b> <i>W. Liu, O. Rioul and M. Beaudouin-Lafon</i>	117
<b>4 Bayesian Command Selection</b> <i>S. Zhu, X. Fan, F. Tian and X. Bi</i>	134
<b>5 Probabilistic UI Representation and Reasoning in Touch Interfaces</b> <i>D. Buschek</i>	163
<b>6 Statistical Keyboard Decoding</b> <i>D. Gaines, J. Dudley, P. O. Kristensson and K. Vertanen</i>	188
<b>7 Human–Computer Interaction Design and Inverse Problems</b> <i>R. Murray-Smith, J. H. Williamson and F. Tonolini</i>	212

<b>Part III Bayesian Optimisation in Interaction Design</b>	237
<b>8 Preferential Bayesian Optimisation for Visual Design</b> <i>Y. Koyama, T. Chong and T. Igarashi</i>	239
<b>9 Bayesian Optimisation of Interface Features</b> <i>J. Dudley</i> <i>and P. O. Kristensson</i>	259
<b>Part IV Bayesian Cognitive Modelling</b>	285
<b>10 Cue Integration in Input Performance</b> <i>B. Lee</i>	287
<b>11 Bayesian Parameter Inference for Cognitive Simulators</b> <i>J. Jokinen, U. Remes, T. Kujala and J. Corander</i>	308
<b>Appendix: Mathematical Background and Notation</b> <i>J. H. Williamson</i>	335

## Contributors

- Nikola Banovic *Electrical Engineering and Computer Science, University of Michigan, Ann Arbor, Michigan, USA*
- Michel Beaudouin-Lafon *CNRS, Inria, LISN, Paris-Saclay University, France*
- Xiaojun Bi *Department of Computer Science, Stony Brook University, Stony Brook, New York, USA*
- Daniel Buschek *Department of Computer Science, University of Bayreuth, Germany*
- Toby Chong *Department of Creative Informatics, Graduate School of Information Science and Technology, The University of Tokyo, Tokyo, Japan*
- Jukka Corander *Department of Mathematics and Statistics, University of Helsinki, Helsinki, Finland*
- Alan Dix *Computational Foundry, Swansea University, Swansea, Wales*
- John Dudley *Engineering Design Centre, University of Cambridge, Cambridge, UK*
- Xiangmin Fan *Institute of Software, Chinese Academy of Sciences, Beijing, China*
- Dylan Gaines *Department of Computer Science, Michigan Technological University, Houghton, Michigan, USA*
- Takeo Igarashi *Department of Creative Informatics, Graduate School of Information Science and Technology, The University of Tokyo, Tokyo, Japan*
- Jussi P. P. Jokinen *Department of Computer Science/Finnish Center for Artificial Intelligence (FCAI), University of Helsinki, Helsinki, Finland*
- Per Ola Kristensson *Engineering Design Centre, Department of Engineering, University of Cambridge, Cambridge, UK*

Yuki Koyama *National Institute of Advanced Industrial Science and Technology (AIST), Ibaraki, Japan*

Tuomo Kujala *Cognitive Science, University of Jyväskylä, Jyväskylä, Finland*

Byungjoo Lee *Department of Computer Science, Yonsei University, Seoul, Korea*

Wanyu Liu *STMS IRCAM-CNRS-Sorbonne Université, Paris, France*

Roderick Murray-Smith *School of Computing Science, University of Glasgow, Glasgow, UK*

Antti Oulasvirta *Finnish Center for Artificial Intelligence FCAI, Department of Communications and Networking, Aalto University, Helsinki, Finland*

Ulpu Remes *Department of Computer Science, University of Helsinki, Helsinki, Finland*

Olivier Rioul *ComElec, Télécom ParisTech, Paris, France*

Feng Tian *Institute of Software, Chinese Academy of Sciences, Beijing, China*

Francesco Tonolini *School of Computing Science, University of Glasgow, Glasgow, UK*

Keith Vertanen *Department of Computer Science, Michigan Technological University, Houghton, Michigan, USA*

John H. Williamson *School of Computing Science, University of Glasgow, Glasgow, UK*

Suwen Zhu *Grammarly, Inc., San Francisco, California, USA*

## Preface

### Motivation

This edited book synthesises recent progress in applications of probabilistic methods in the area of human–computer interaction (HCI). HCI is a field concerned with the design and study of computing systems for human use. Most design efforts in HCI follow a human-centred (also known as user-centred) approach that considers the context of use and the abilities and needs of stakeholders. However, most existing human-centred methods prescribe resource-intensive design and evaluation methods. The prevailing paradigm relies extensively on trial and error and expensive empirical measurements.

HCI has recently revived its interest in using algorithmic approaches to drive design and evaluation [17]. *Computational interaction* is a topic area that studies algorithmic methods to optimise designs, adapt user interfaces, automate evaluation, and even explain and describe interaction through simulation of user interfaces and prediction of user actions on those interfaces. However, traditional computational modelling approaches in HCI [1], such as model human processor (MHP) [5], GOMS [11] and Fitts' law [15], ignore uncertainty. Statistical analysis methods commonly used in HCI tend towards a frequentist treatment of probability with its known shortcomings [3, 13].

This book aims to fill a gap in the literature and promote research on Bayesian methods in HCI. Bayesian methods, such as *Bayesian statistical analysis* [9] (statistics that use Bayesian interpretation of probability of events) and *uncertainty quantification (UQ)* [10] (the characterisation and computation of uncertainty and confidence for models and data in a principled statistical manner), have been adopted across a wide range of scientific and engineering research disciplines and fields (e.g. physics [16], nuclear safety and management [18], astronautical engineering [6], medicine and healthcare [2]). However, despite there being Bayesian approaches to a variety



of related problems in science and engineering, applications in HCI are still nascent. Although there are already some examples of successful use of Bayesian methods in interaction design (e.g. supporting user modelling [4, 12], probabilistic interfaces [44], novel interactions [20, 21], design optimisation [8, 14], evaluation and statistical analysis [7, 13]), such methods are not yet widely adopted in the broader HCI community.

## Outline

The chapters in this book expose the reader to Bayesian methods for interaction design and teach them how to apply such principled methods to their own research and practice. One of the main goals of this book is to bridge the gap between literature on theoretical Bayesian methods and practical applications in interaction and design and make Bayesian methods accessible to a broader HCI audience.

This book does so through a series of chapters split in four parts, beginning with an introduction to Bayesian methods and Bayesian statistics, followed by a section that illustrates applications of Bayesian inference to infer user intents in probabilistic interfaces. This is followed by a collection of chapters on Bayesian optimisation in the design of interfaces. The final section illustrates use of Bayesian methods in cognitive and user performance modelling and simulation.

Part I of this book explains the Bayesian treatment of probability and uncertainty through two chapters. Chapter 1 makes a case for Bayesian modelling and illustrates principles and applications of Bayesian inference on simple, tutorial-like examples relevant to interactive design. Chapter 2 explains Bayesian statistics and its application to interactive design evaluation. After reading Part I, the reader will have the foundational knowledge on how to apply the Bayesian method to interactive design with a road map for how to explore related, more advanced topics further.

Part II illustrates how to design user interfaces that can reduce the uncertainty about the user's goals and intentions using Bayesian inference. Chapters 3–6 show how to infer user goals and intentions for four different, fundamental interaction types: information search, pointing target selection, command selection and text entry. Chapter 7 then discusses how to combine forward (traditional ML) models with inverse (Bayesian) modelling in the context of touch sensing. Having read Part II, the reader will know how to implement probabilistic user interfaces that can reason about and act in response to inherently uncertain user behaviours.

The next part of the book, Part III, illustrates Bayesian optimisation approaches to design user interfaces that optimise for user preferences and abilities. User preferences for particular features of an interface or the interface as a whole are notoriously difficult to elicit and often require repeated, costly empirical user studies. The chapters in this part detail how to use Bayesian optimisation to efficiently reduce the search space of all possible interfaces to a few user-desired options. The methods covered in this section will give the reader new tools to optimise their user interface design in a principled way that goes beyond trial and error.

Finally, Part IV illustrates applications of Bayesian approaches to computational cognitive models that simulate human decision-making and physical actions. Such approaches provide a theoretical and methodological update to traditional computational modelling approaches in HCI. After reading these final chapters, the reader will be able to apply a probabilistic lens onto the user's decision-making and how their cognitive plans result in physical action.

## References

- [1] N. Banovic, A. Oulasvirta and P. O. Kristensson. 2019. Computational modeling in human–computer interaction. Page 1–7, Paper No. W26 of: *Extended Abstracts of the 2019 CHI Conference on Human Factors in Computing Systems*. CHI EA '19. Association for Computing Machinery.
- [2] E. Begoli, T. Bhattacharya and D. Kusnezov. 2019. The need for uncertainty quantification in machine-assisted medical decision making. *Nature Machine Intelligence*, **1**(1), 20–23.
- [3] L. Besançon and P. Dragicevic. 2019. The continued prevalence of dichotomous inferences at CHI. Pages 1–11 of: *Extended Abstracts of the 2019 CHI Conference on Human Factors in Computing Systems*. Association for Computing Machinery.
- [4] X. Bi and S. Zhai. 2013. Bayesian touch: a statistical criterion of Target selection with finger touch. Pages 51–60 of: *Proceedings of the 26th Annual ACM Symposium on User Interface Software and Technology*. UIST '13. Association for Computing Machinery.
- [5] S. K. Card, A. Newell and T. P. Moran. 1983. *The Psychology of Human–Computer Interaction*. L. Erlbaum Associates Inc.
- [6] L. G. Crespo, S. P. Kenny and D. P. Giesy. 2014. The NASA Langley multidisciplinary uncertainty quantification challenge. In: *16th AIAA Non-Deterministic Approaches Conference*. American Institute of Aeronautics and Astronautics.
- [7] P. Dragicevic, Y. Jansen, A. Sarma, M. Kay and F. Chevalier. 2019. Increasing the transparency of research papers with explorable multiverse analyses. Pages 1–15, Paper No. 65 of: *Proceedings of the 2019 CHI Conference on Human Factors in Computing Systems*. CHI '19. Association for Computing Machinery.

- [8] J. J. Dudley, J. T. Jacques and P. O. Kristensson. 2019. Crowdsourcing interface feature design with Bayesian optimization. Pages 1–12, Paper No. 252 of: *Proceedings of the 2019 CHI Conference on Human Factors in Computing Systems*. CHI '19. Association for Computing Machinery.
- [9] A. Gelman, J. B. Carlin, H. S. Stern and D. B. Rubin. 2004. *Bayesian Data Analysis*, 2nd ed. Chapman and Hall/CRC.
- [10] R. Ghanem, D. Higdon and H. Owhadi, eds. 2017. *Handbook of Uncertainty Quantification*. Springer International Publishing.
- [11] B. E. John and D. E. Kieras. 1996. The GOMS family of user interface analysis techniques: comparison and contrast. *ACM Transactions on Computer–Human Interaction*, **3**(4), 320–351.
- [12] A. Kangasrääsiö, J. P. P. Jokinen, A. Oulasvirta, A. Howes and S. Kaski. 2019. Parameter inference for computational cognitive models with approximate Bayesian computation. *Cognitive Science*, **43**(6), e12738.
- [13] M. Kay, G. L. Nelson and E. B. Hekler. 2016. Researcher-centered design of statistics: why Bayesian statistics better fit the culture and incentives of HCI. Pages 4521–4532 of: *Proceedings of the 2016 CHI Conference on Human Factors in Computing Systems*. CHI '16. Association for Computing Machinery.
- [14] J. D. Lomas, J. Forlizzi, N. Poonwala, P. Patel, S. Shodhan, K. Patel, K. Koedinger and E. Brunskill. 2016. Interface design optimization as a multi-armed bandit problem. Pages 4142–4153 of: *Proceedings of the 2016 CHI Conference on Human Factors in Computing Systems*. CHI '16. Association for Computing Machinery.
- [15] I. S. MacKenzie. 1992. Fitts' law as a research and design tool in human–computer interaction. *Human–Computer Interaction*, **7**(1), 91–139.
- [16] W. L. Oberkampf, T. G. Trucano and C. Hirsch. 2004. Verification, validation, and predictive capability in computational engineering and physics. *Applied Mechanics Reviews*, **57**(5), 345–384.
- [17] A. Oulasvirta, X. Bi and A. Howes. 2018. *Computational Interaction*. Oxford University Press.
- [18] M. Pilch, T. G. Trucano and J. C. Helton. 2006. *Ideas Underlying Quantification of Margins and Uncertainties (QMU): A White Paper*. Technical report, Sandia National Laboratories.
- [44] J. Schwarz, J. Mankoff and S. Hudson. 2011. Monte Carlo methods for managing interactive state, action and feedback under uncertainty. Pages 235–244 of: *Proceedings of the 24th Annual ACM Symposium on User Interface Software and Technology*. UIST '11. Association for Computing Machinery.
- [20] A. Spielberg, A. Sample, S. E. Hudson, J. Mankoff and J. McCann. 2016. RapID: a framework for fabricating low-latency interactive objects with RFID tags. Pages 5897–5908 of: *Proceedings of the 2016 CHI Conference on Human Factors in Computing Systems*. CHI '16. Association for Computing Machinery.
- [21] E. Zhang and N. Banovic. 2021. Method for exploring generative adversarial networks (GANs) via automatically generated image galleries. In: *Proceedings of the 2021 CHI Conference on Human Factors in Computing Systems*. CHI '21. Association for Computing Machinery.