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Facets of Algebraic Geometry
A Collection in Honor of William Fulton's
80th Birthday

VOLUME 1

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We dedicate these volumes with gratitude and admiration to William Fulton, on the occasion of his 80th birthday. We hope that the articles collected here, written by colleagues, friends, and students, may reflect the breadth of Bill's impact on mathematics, along with the depth of his enduring influence on all of us who have had the great good fortune to learn from and be inspired by him.

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Edited by Paolo Aluffi , David Anderson , Milena Hering , Mircea Mustață , Sam Payne

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