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# Surveys in Combinatorics 2019

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## Preface

The Twenty-Seventh British Combinatorial Conference is to be held at the University of Birmingham from 29th July to 2nd August 2019. The British Combinatorial Committee had invited eight distinguished combinatorialists to give survey lectures in areas of their expertise, and this volume contains the survey articles on which these lectures were based.

In compiling this volume we are indebted to the authors for preparing their articles so accurately and professionally, and to the referees for their rapid responses and keen eye for detail. We would also like to thank Tom Harris and Clare Dennison at Cambridge University Press. Finally, without the previous efforts of editors of earlier Surveys and the guidance of the British Combinatorial Committee, the preparation of this volume would have been somewhat daunting.

This conference is organised in partnership with the Clay Mathematics Institute, the Heilbronn Institute, the Institute of Combinatorics and its Applications, the London Mathematical Society and the University of Birmingham; we thank each of these organisations for their generous involvement and support.

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