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# Integrable Systems and Algebraic Geometry

A Celebration of Emma Previato's 65th Birthday

Volume 1

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