Quantitative Analysis of Ecological Networks

Network thinking and network analysis are rapidly expanding features of ecological research. Network analysis of ecological systems includes representations and modeling of the interactions in an ecosystem, in which species or factors are joined by pairwise connections. This book provides an overview of ecological network analysis including generating processes, the relationship between structure and dynamic function, and statistics and models for these networks. Starting with a general introduction to the composition of networks and their characteristics, it includes details on such topics as measures of network complexity, applications of spectral graph theory, how best to include indirect species interactions, and multilayer, multiplex and multilevel networks. Graduate students and researchers who want to develop and understand ecological networks in their research will find this volume inspiring and helpful. Detailed guidance to those already working in network ecology but looking for advice is also included.

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Quantitative Analysis of Ecological Networks

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Ecology is about understanding how organisms interact with other organisms and the environment they inhabit (i.e. fundamental and realised niches). It is easy to imagine an individual organism of any kind as a dot with all sorts of arrows impinging upon it; an arrow can represent abiotic factors (temperature, light, etc.), along with many arrows for all the other organisms (biotic factors, intra- and inter-specific interactions) that affect it. Ecology aims therefore to determine the magnitude and rate associated with some of the arrows and identify which are the most important and why. Each organism also has its own effects on the same list of factors, even if the effects are small, so we can also imagine arrows going out from the same dot, one to each of the same factors (they can be dots too). Again, a challenge is to determine the associated weights and importance of the arrows, some of which are directed towards other organisms. As soon as we consider more than a single organism, even just a few, we immediately have a complex structure of dots and arrows: an ecological network!

It is an obvious step to consider ecological systems as ecological networks, and as such to assess how network theory (concepts and methods) might be applied to them. Network theory and the mathematics of graph theory that underlie network analysis provide simple concepts that can applied to systems that are complex both in structure and dynamics. It is those concepts that allow us to provide a sorted set of methods for the quantitative analysis of ecological networks, together with thoughts and advice on how best to proceed. Through the years, the need to take a network analysis framework to study complex systems has arisen in many fields (physics, computer science, communication science [transportation, electricity, social], and bio- and eco-informatics), and there is a challenging diversity of approaches, methods and measures that should be understood, or at least sorted, before applying them to our own data. The overarching goal of this book is to help ecologists in selecting the appropriate network methods to represent, analyse and model their ecological systems using network theory.

As the title suggests, this book is for ecologists with an interest in ecological networks. Perhaps they have a project in mind or even some potential network data “in hand” but are not sure how to proceed or on which network characteristics to concentrate. This book provides both background and some advice on how to answer interesting ecological questions in the context of network analysis. It does cover some general network material (that is needed as background), but to the breadth of books like Newman (2010) or Estrada (2012). It was partly inspired by Kolaczyk (2009), but
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it is less technical in tone and detail and more inclusive of recent developments. All three of the books just cited, together with Kolaczyk and Csárdi (2014) which supplies R code, are excellent resources for more information, as needed. The other inspiration for our current book is Dale (2017), which focused on applying graph theory in ecology, and mentioned, but did not cover, network analysis. The current project moves forward into network analysis from that work but does not assume its material as background.

As is often the case, the book evolved as it was being written. Initially, there was no separate chapter on multilayer and multilevel networks, but it became obvious that it was both necessary and crucial – hence Chapter 4. Similarly, we had not explicitly included causal networks in the original outline, although it now seems central to the presentation. Hence, now a central theme of the book is to stress the interplay between the structure and the dynamics (or between form and function) of these complex networks from ecological systems. Last, the ending of the book started out as only the summary diagram “It all ties together,” but when we got to the end, there was more that needed to be said – hence Chapter 5 (we did keep it short). One factor in driving the evolution of this book is the speed at which the field of the study of ecological networks, let us call it “network ecology,” is growing, developing and advancing. It is very challenging just to keep pace with developments, but it is also very satisfying to see the subdiscipline getting the attention and application we think it should.

There are many people and organisations to thank for supporting the project, starting with Natural Sciences and Engineering Research Council (NSERC), NSERC Canada Research Chair, the University of British Columbia, and the University of Toronto for financial support. We thank Alex Aravind, Charlotte Brown, Cheryl Smyth, Conan Veitch, and J. C. Cahill for their reading of chapters and their thoughtful advice for improvements. We especially thank J. B. Grace for permission to use material from an unpublished manuscript on statistical models and causal analysis as the basis for Table 3.4.

Writing this book has been an exciting and rewarding journey of discovery through the rapidly changing landscape of network ecology. No book can be completely up to date, but the hope is that the course it has followed is in the right direction for continuation into the future. It is also our hope that the book can serve an as exciting and helpful guide for others on a similar journey of discovery.