

## Index

- adsorption, 107, 117  
 air, 90  
 aluminium, 183  
 ammonia, 63  
 angle-dependent magnetoresistance oscillations (AMRO), 149  
 angle-resolved photoemission spectroscopy (ARPES), 149  
 angular momentum  
   quantization, 17  
   rigid rotor, 62  
 anomalous skin effect, 149  
 antiferromagnetism, 56, 192, 193  
 anyons, 126  
 argon, 1, 90  
 attractor, 44  
 average value, 5  
 Avogadro's number, 71  
  
 ballistic motion, 11, 98  
 Bayes' theorem, 23  
 benzene, 63  
 Bessel, F. W., 151  
 binary alloy, 193, 217  
 binomial distribution, 4, 11  
   large- $N$  limit, 14  
   mean, 12  
 binomial theorem, 4, 9, 17  
 biophysics, 193  
 bits, 33  
 black hole, 38, 153  
   Sagittarius A\*, 38  
 blackbody  
   cavity, 163  
   imperfect, 170  
   perfect, 170  
   radiation, 61, 161, 162, 165, 169, 185  
   spectrum, 166–168  
 Boltzmann distribution, 52, 210  
 Boltzmann equation, 89  
 Boltzmann factor, 52, 209  
   generalized, 113  
 Boltzmann's constant, 21, 71  
 Boltzmann, L. E., 2, 30  
 Bose–Einstein condensate, 173, 175  
  
 Bose–Einstein condensation, 2, 104, 161, 170, 172, 174, 186, 187, 239  
   experiment, 187  
 Bose–Einstein distribution, 125, 132, 133, 136, 137, 162, 163, 170, 178, 181, 184, 185  
 bosons, 69, 107, 122, 125–127, 130–132, 136, 161  
 bridge equation, 50, 52, 55, 112, 121  
   canonical ensemble, 50, 80  
   grand canonical ensemble, 113, 121  
   microcanonical ensemble, 37  
 broken symmetry, 46, 194, 214  
 Brown, R., 86, 95  
 Brownian motion, 7, 86, 95  
  
 $C_{60}$ , 63  
 canonical ensemble, 25, 48, 50, 54, 80, 107  
 carbon dioxide, 63, 72, 90  
 carbon-12, 154  
 cavity modes, 161  
 central limit theorem, 15, 21, 27, 77, 196  
 chain rule, 237  
 Chandrasekhar mass, 156  
   rotations, 157  
 chaos, 1  
 characteristic pressure  
   adsorption, 118  
 characteristic temperature  
   electronic transitions, 72  
   rotations, 63, 72, 110  
   translations, 64  
   vibrations, 72  
 chemical equation, 119  
 chemical equilibrium, 118–121  
 chemical potential, 107, 108, 111, 113, 115, 119, 187  
   Bose–Einstein condensate, 176  
   bosons, 132, 170, 176, 178, 187  
   fermions, 131, 139, 140, 143, 157, 178, 187  
   ideal gas, 109, 110  
   phonons, 181  
   photons, 161, 162, 185  
   white dwarf, 154  
 chemical reaction, 107, 118, 119  
 chemical symbol, 118  
 chemotaxis, 7  
 Clark, A., 151

- classical limit, 61, 69, 78, 125
  - bosons, 132
  - fermions, 131
- classical particles, 41, 126, 128
- closed system, 25
- coin toss experiment, 4, 5, 8, 17
- collision time, 98, 99
- complex fluids, 94
- compressibility
  - number, 115
- condensate fraction, 172, 173, 175
- conductance, 103
- conductivity, 103
- constraints, 16, 25, 111
- continuity equation, 43
- Cooper pair, 175
- copper, 149, 183
- Cornell, E. A., 173
- cosmic microwave background radiation, 167, 168
- Coulomb interaction, 150, 190
- Coulomb potential, 188
- critical density
  - Bose–Einstein condensation, 173
- critical exponents, 213
- critical point, 199, 201, 208, 212
- critical speed
  - superfluid, 174, 175
- critical temperature, 194, 216
  - Bose–Einstein condensation, 172
  - one-dimensional Ising model, 208
- Curie temperature, 17, 194
  - iron, 17
  - mean field estimate, Ising model, 198
- current, 103
- current density, 103
  
- de Haas van Alphen effect, 149
- Debye  $T^3$  law, 182, 183
- Debye frequency, 181
- Debye model, 80, 181–184, 186, 189
  - phonon density of states, 184
- Debye temperature, 182
- degeneracy, 56, 62, 67, 70, 81
  - spherical rotor, 63
  - symmetric rotor, 63
- degeneracy pressure, 145
- degenerate electron gas, 152
- density of states, 30, 87, 133–136
  - $k$ -space, 134
  - magnons, 185
  - one dimension, 135
  - phonons, 181, 183, 184
  - photons, 162
  - three dimensions, 134
  - two dimensions, 135
- detailed balance, 209, 210
  
- deuterium hydride, 85
- diatomic gas, 78, 83, 110
- diatomic molecule, 63, 72
- differential
  - enthalpy, 235
  - exact, 229
  - grand potential, 236
  - heat, 231
  - Helmholtz free energy, 235
  - inexact, 229
  - work, 230
- diffusion, 11, 22, 98
  - coefficient, 86, 98, 101
  - equation, 98
- dilute limit, 81, 127
- dimensionless parameters, 35
- dispersion relation, 162
- displacement
  - root mean square, 98
- distinguishable particles, 67, 81, 125–127
- DNA, 2
- domain wall, 202–204
- Dulong and Petit law, 79, 80, 183
- Dulong, P. L., 80
  
- effusion, 94, 104, 169
  - rate, 95
- Einstein model, 80
- electric field, 103
  - photons, 162
- electrical noise, 2
- electron, 67, 69, 125, 127, 148, 152, 154
  - rest mass energy, 155
  - spin, 17
- electron degeneracy pressure, 156
  - white dwarf, 152
- electroweak symmetry, 214
- emissivity, 170
- energy, 52, 114, 116
  - bosons, 177
  - conservation of, 55
  - Fermi gas, 144
  - fluctuations, 53, 54
  - gas of polyatomic molecules, 72
  - ideal gas, 71
  - magnons, 185
  - phonons, 182
  - quantum simple harmonic oscillator, 60
- energy density
  - blackbody radiation, 165, 166, 168
  - photons, 164
- energy eigenstates, 16, 25
  - particle in a box, 134
- energy eigenvalues
  - linear rotor, 63
  - particle in a box, 64, 87, 134

- simple harmonic oscillator, 59
- spherical rotor, 63
- symmetric rotor, 63
- energy flow, 27, 28, 125, 230
- energy fluctuations
  - ideal gas, 71
- energy level, 125, 130
- energy window, 30, 146
- ensemble average, 41, 45, 221
- enthalpy, 235
- entropy, 2, 19, 28, 37, 50, 53, 56, 231
  - blackbody radiation, 187
  - Boltzmann, 21, 27, 32, 36, 41
  - classical harmonic oscillator, 84
  - Fermi gas, 146
  - gas of polyatomic molecules, 72
  - Gibbs, 31–33, 41, 112, 146
  - ideal gas, 71
  - information, 21, 33
  - measure of ignorance, 2, 19, 21, 32, 146
  - of mixing, 73–75
  - quantum harmonic oscillator, 84
  - Shannon, 32
  - zero temperature, 56
- environment, 33, 48
- equation of state, 227
  - van der Waals, 75
- equations of motion, 2, 30, 42
- equilibration, 26, 41, 209
- equilibrium, 2, 26, 45, 55, 78, 110
  - average, 25
  - thermodynamic, 227
- equilibrium constant, 120, 121
- equipartition theorem, 47, 78, 79, 83, 84, 90, 97, 183, 184
- ergodic hypothesis, 45, 46, 218
- ergodicity, 45
- exchange energy, 191, 193
- exchange interactions, 190
- extensive variable, 54, 136, 228
- Fermi energy, 131, 139, 140, 144, 145, 148, 151, 154, 157
  - white dwarf, 154
- Fermi function, 131, 139
- Fermi gas, 139
- Fermi level, 144
- Fermi liquid theory, 151
- Fermi sea, 148
- Fermi surface, 149
- Fermi temperature, 140, 157
  - white dwarf, 152
- Fermi wavevector, 149
- Fermi–Dirac distribution, 117, 125, 131–133, 136, 137, 139, 157
- fermion degeneracy pressure, 153, 157
- fermions, 69, 107, 115, 125–127, 130, 131, 136, 139
- ferromagnetism, 17, 46, 190, 192, 193, 199
  - Ising model, 198
- Fick’s law, 100, 101
- fluctuation–dissipation theorem, 53
- fluctuations, 30
- flux, 94
- force
  - fluctuating, 96
- forced oscillator, 44
- Fourier series, 166
- fractional statistics, 126
- fugacity, 111, 113, 239
- gamma function, 143, 222–224
- Gaussian distribution, 14, 89
- Gaussian integral, 222
- Geim, A. K., 158
- genetic drift, 7
- geometric series, 59, 130
- giant molecular cloud, 105
- Gibbs ensemble, 119
- Gibbs factor, 113
- Gibbs free energy, 114, 119, 121, 236
- Gibbs, J. W., 2, 25, 73, 128
- Gibbs–Duhem relation, 124, 234
- glassy systems, 46, 56, 190
- Glauber dynamics, 210
- grand canonical ensemble, 25, 107, 113, 115, 119, 121, 125, 128, 129
- grand canonical partition function, 111–114, 121, 125, 130
  - adsorption, 117
  - blackbody radiation, 187
  - bosons, 130
  - fermions, 130
  - Maxwell–Boltzmann particles, 128, 129
  - two-level system, 116
- grand potential, 113, 114, 121, 236
  - adsorption, 117
  - bosons, 130, 186
  - fermions, 130, 145
  - Maxwell–Boltzmann particles, 129
- graphene, 158
- gravitational potential
  - stellar interior, 153
- ground state
  - macroscopic occupation, 172
- H*-theorem, 30
- Hamilton’s equations, 30, 42, 43
- Hamiltonian, 42, 128
  - particle in a box, 134
  - rigid rotor, 62
  - simple harmonic oscillator, 59
- Hawking, S. W., 38
- heat, 229, 230

- heat bath, 48, 65, 107  
 heat bath algorithm, 210  
 heat capacity, 53, 58, 233, 238  
   aluminium, 183  
   bosons, 177, 179, 239  
   classical harmonic oscillator, 84  
   cusp for bosons, 179  
   Debye model, 182, 183  
   electrons, 149  
   Fermi gas, 145  
   gas of polyatomic molecules, 73  
   ideal gas, 71  
   magnons, 185  
   metal, 149  
   phonons, 150, 182  
   quantum harmonic oscillator, 84  
   relation between  $C_V$  and  $C_P$ , 238  
   two-level system, 58  
 Heaviside step function, 139  
 Heisenberg model, 191, 219  
 helium-3, 69, 127, 175  
   superfluidity, 175  
 helium-4, 69, 127, 154, 174, 179  
   superfluidity, 174  
 Helmholtz free energy, 52, 80, 107, 109, 113, 119, 235  
   ideal gas, 70  
   one-dimensional Ising model, 207  
   uncoupled subsystems, 66  
 hemoglobin, 118  
 Herschel, F. W., 151  
 Hertzprung–Russell diagram, 152  
 Higgs boson, 127, 214  
 Hilbert space, 16  
 holes, 148  
 hydrogen, 85, 105, 118, 154  
   atom, 127  
  
 ideal gas, 2, 65, 70, 79, 86, 88, 91, 92, 109  
 ideal gas constant, 71  
 ideal gas law, 1, 70–72, 227  
 importance sampling, 209, 210  
 impurities  
   in crystals, 2  
 indistinguishable particles, 67, 68, 74, 81, 125–127  
 information theory, 2, 33, 193  
 initial conditions, 1, 26, 43, 210, 227  
   pathological, 44  
 initial state, 42, 125  
 intensive variable, 229  
 interaction potential, 75, 181  
 iron, 17, 190  
 irreversibility, 2  
 irreversible process, 26, 33, 75, 227  
 isentropic process, 228  
 Ising model, 190, 192, 193, 209, 216  
   binary alloy, 217  
  
   liquid–gas transition, 212  
   mean field theory, 195  
   Monte Carlo simulation, 209, 220  
   one dimension, 202  
   Onsager solution, 193, 208  
   solution in one dimension, 205  
   three dimensions, 213  
   two dimensions, 193, 203, 220  
 Ising spin, 192  
 Ising, E., 192  
 isobaric process, 228  
 isochoric process, 108, 228  
 isolated system, 25, 27  
 isothermal process, 108, 228  
 isotope, 95, 175  
 isotropic fluid, 94  
  
 Ketterle, W., 173  
 kinetic theory, 86, 91, 102  
 kurtosis, 7  
  
 Lagrange multiplier, 32, 48, 111, 112  
 lambda peak, 179, 180  
 Landau level, 159  
 Landau theory, 213, 216  
 Landau, L. D., 150, 174  
 Landauer, R. W., 33  
 Langevin equation, 96, 98  
 Langmuir adsorption isotherm, 117, 118, 130  
 latent heat, 201  
 lattice  
   bipartite, 192  
   cubic, 192  
   kagome, 56  
   square, 192  
   triangular, 192  
 law of mass action, 118, 119, 121  
 laws of thermodynamics, 55, 231  
   first, 55, 231  
   second, 2, 30, 56, 232  
   third, 56, 233  
   zeroth, 55, 231  
 lead, 183  
 Lee, D. M., 175  
 Legendre transform, 234, 235  
 Lennard–Jones potential, 75, 99  
 Lenz, W., 192  
 Liouville’s theorem, 41, 43, 45  
 liquid, 190  
 liquid crystals, 94  
 liquid helium, 174  
 liquid–gas transition, 212  
 Lorentzian distribution, 16  
  
 macrostate, 16, 19, 55  
   spin, 18  
 magnetic dipole interaction, 190

- magnetic domains, 2, 202
- magnetic moment
  - fermions, 151
- magnetic susceptibility, 160, 195
  - Ising model, 199, 221
- magnetism, 17, 193
- magnetization, 18, 34, 35, 194
  - Ising model, 198, 199
  - one-dimensional Ising model, 202, 207
- magnons, 69, 127, 161, 180, 184, 186
- main sequence star, 153
- many-body localization, 46
- Markov chain, 209
- Mawell, J. C., 2
- Maxwell relations, 236, 237
- Maxwell's equations, 161
- Maxwell–Boltzmann distribution, 129, 131–133, 136, 137
- Maxwell–Boltzmann particles, 187
- Maxwell–Boltzmann statistics, 127–129, 137
- Maxwell–Boltzmann velocity distribution, 86–89, 94, 95
  - moments, 89, 104
- mean field theory, 216
  - Ising model, 202
- mean free path, 98–101
- mean square displacement
  - random walk, 10, 24
- mesons, 127
- metals, 148
  - electrical transport, 103
- methane, 63
- Metropolis algorithm, 209, 210
- microcanonical ensemble, 25, 36, 41, 44, 54, 107
- microstate, 16, 19, 25, 27, 31, 37, 50, 87, 125
  - accessible, 41
  - Ising model, 193
  - spin, 18
- mole, 71
- molecular chaos, 30
- molecular collisions, 93
- molecular dynamics simulation, 2, 45
- molecular motors, 2, 7
- moment of inertia, 62
- monatomic gas, 70, 109
- Monte Carlo simulation, 2, 45, 209, 220
  - initial conditions, 209
  - initial state, 210
  - Monte Carlo steps, 210
- Mott insulator, 115
- multinomial theorem, 68
- multiplicity function, 18, 19, 27, 30, 37
  - spins, 18, 34
- muon, 127
- myoglobin, 118
- Nernst, W. H., 233
- neural networks, 193
- neutrino, 69, 127
- neutron, 69
  - ultra-cold, 83
- neutron degeneracy pressure, 156
- neutron star, 153, 156, 157
  - interior, 157
- Newton's second law, 96, 153
- nitrogen, 82, 83, 90
- non-ergodic systems, 46
- non-ideal gas, 75, 77, 83
- normal fraction, 173, 175
- normal modes, 161, 180
- normalization, 89
- Novoselov, K. S., 158
- nuclear fusion, 153
- number density, 70, 89, 99, 109, 155
  - photons, 163
- number fluctuations, 115
  - fermions, 147
- occupation number, 67–69, 129
  - quantum simple harmonic oscillator, 60
- Onsager, L., 208
- open system, 25
- order, 190
- order parameter, 193, 213, 216
- Osheroff, D. D., 175
- oxygen, 1, 82, 90, 100, 118
- oxygen-16, 154
- paramagnetism, 17, 194, 199, 212
- partial pressure, 111, 124
- particle bath, 107
- particle exchange, 127
- particle in a box, 16, 64, 87
- particle number, 107, 114, 130
  - bosons, 170
  - two-level system, 116
- partition function, 48, 49, 80, 112, 113
  - approximate for Ising model, 196
  - classical, 61, 75
  - classical simple harmonic oscillator, 61
  - derivatives, 52
  - distinguishable particles, 67, 127
  - gas of polyatomic molecules, 72
  - ideal gas, 70
  - indistinguishable particles, 69, 70
  - Ising model, 194
  - linear rotor, 63
  - non-ideal gas, 77
  - one-dimensional Ising model, 205
  - particle in a box, 64
  - quantum simple harmonic oscillator, 59
  - rigid rotor, 62

- single particle, 56, 127, 128
  - uncoupled subsystems, 66
- Pauli exclusion principle, 69, 116, 127, 190
- Penzias, A. A., 167
- periodic boundary conditions, 134, 162, 205
- Petit, A. T., 80
- phase of matter, 190
- phase space, 16, 41–45, 61, 88
  - volume, 44
- phase transition, 2, 173, 180, 190
  - first order, 201, 216
  - liquid–gas, 193, 212
  - second order, 201, 213, 216
- phonons, 69, 80, 127, 150, 161, 174, 180, 181, 186, 189
- photons, 69, 127, 161, 162, 180, 185
  - in the Sun, 2, 7
- Physics Nobel Prize
  - 1918, 166
  - 1978, 167
  - 1996, 175
  - 2001, 173
  - 2010, 158
- Pippard, A. B., 149
- Planck length, 38
- Planck's constant, 165
- Planck's formula, 61, 165, 167, 185
- Planck, M. K. E. L., 165
- Poincaré recurrence theorem, 30
- polarization
  - longitudinal, 162
  - phonons, 181
  - photons, 162
  - transverse, 162
- polyatomic molecules, 56, 72
- polymer folding, 2, 7, 23, 38
- potential difference, 103
- pressure, 54, 92, 110, 111
  - bosons, 177, 188
  - Fermi gas, 145
  - ideal gas, 70
  - isotropic fluid, 94
  - momentum transfer, 92
  - Mount Everest, 105
  - partial, 111, 124
  - radiation, 168
- pressure gradient
  - stellar interior, 154
- principle of maximum entropy, 28, 29, 32
- probability, 3
  - axioms, 3
  - microstates, 111
  - tree diagram, 4
- probability density, 5, 88
  - incompressible, 44
  - phase space, 43
  - quantum, 126
- probability distributions, 2, 5
  - central moments, 7
  - continuous, 5
  - discrete, 5
  - mean, 7
  - moments, 6
  - standard deviation, 7
  - variance, 7
- proton, 67, 69, 154, 159
- quantum concentration, 65, 109, 120, 171
- quantum degeneracy, 140
- quantum Hall effect, 115
  - fractional, 126, 159
- quantum number, 16, 151, 188
- quantum particles, 125, 126, 129, 136
- quantum statistical mechanics, 65, 125
- quantum statistics, 125
- quasi-static process, 228
- quasiparticle, 151
- random walk, 7, 17, 21, 98
  - biased, 11, 23
  - one dimension, 7, 8
  - two dimensions, 7
  - unbiased, 11
- randomness, 5
- Raoult's law, 124
- Rayleigh–Jeans formula, 166, 167
- renormalization, 150
- reservoir, 48
- resistance, 103
- reversible process, 227
- Richardson, R. C., 175
- Riemann zeta function, 164, 166, 239
- rigid rotor, 62
  - linear, 62, 63
  - spherical, 62
  - symmetric, 62, 63
- root mean squared (rms) distance, 11
- rubidium-87, 174
- Sackur, O., 71
- Sackur–Tetrode equation, 71
- Schottky anomaly, 58, 59
- Schrödinger equation, 1, 16, 30, 64
- separation of variables, 64, 161
- Shubnikov de Haas oscillations, 149
- simple harmonic oscillator, 16, 79
  - classical, 61, 162
  - quantum, 59
- Sirius, 151
- skew, 7
- solar mass, 156
- solar sail, 186
- solid, 190
- Sommerfeld expansion, 140, 144

- sound speed, 181
  - helium-4, 175
- specific heat
  - helium-4, 180
- speed
  - distribution in an ideal gas, 90
  - most probable, 90
- spin, 17, 69
  - operator, 191
- spin degeneracy, 87, 155
- spin waves, 184
- spin-statistics theorem, 126
- spins, 2, 34
  - in a magnetic field, 190
  - non-interacting, 17, 190
- spontaneous symmetry breaking, 214
- standard deviation, 7
- state
  - thermodynamic, 229
- state function, 228
- statistical ensembles, 25, 41, 54
- statistical mechanics, 1, 37, 55
- steepest descents, 224
- Stefan–Boltzmann constant, 170, 185
- Stefan–Boltzmann law, 169, 170, 185
- step function, 131
- Stirling’s formula, 11, 31, 34, 70, 222, 224
- stock prices, 2, 7
- strategy of least bias, 32
- stress, 93
  - shear, 94
  - tensile, 94
- stress tensor, 93, 94
- Sun, 152
  - luminosity, 186
- superconductivity, 175, 190
- superfluidity, 2, 161, 174, 175, 186, 190
  - laboratory frame, 175
- supernova, 153
  - SN 2003fg, 156
- symmetry breaking field, 214
  
- tau lepton, 127
- temperature, 28, 231
- temporal average, 41, 45
- tensor, 94
  
- Tetrode, H. M., 71
- thermal average, 133, 135
- thermal contact, 26
- thermal de Broglie wavelength, 65, 70
- thermal energy, 35
- thermally isolated system, 25
- thermodynamic limit, 55, 147
- thermodynamic potentials, 233
- thermodynamics, 1, 26, 37, 55, 227
- transfer matrix, 206
- transport, 86, 102
- two-level system, 56
  - energy, 56
  - fermions, 115
  - heat capacity, 58
  - partition function, 56
  
- ultra-cold atoms, 25, 173
- uncoupled subsystems, 65, 82
- undistinguished particles, 128, 137
- universality, 213
- uranium, 95, 104
- uranium hexafluoride, 63, 95
  
- van der Waals equation of state, 75, 77, 83
- vapour, 117
- variance, 7
- velocity
  - root mean square, 90
- viscosity, 105, 174
  - superfluid, 175
  
- W boson, 127, 214
- water, 118
- wavefunction, 125–127
- white dwarf, 2, 151, 153, 156, 157
  - Eridani B, 151
  - interior, 155
  - mass, 155
  - Sirius B, 151
- Wieman, C. E., 173
- Wien’s displacement law, 165
- Wilson, R. W., 167
- work, 229, 230
  
- Z boson, 127, 214
- zero temperature, 139