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978-1-108-07764-4 - A History of the Mathematical Theory of Probability:
From the Time of Pascal to that of Laplace

Isaac Todhunter

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