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978-1-108-07044-7 - A History of the Theory of Elasticity and of the Strength of Materials: Volume 2: Part 2: Saint-Venant to Lord Kelvin (2)

Isaac Todhunter Edited by Karl Pearson

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