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978-1-108-07042-3 - A History of the Theory of Elasticity and of the Strength of Materials: Volume 1: From Galilei to Saint-Venant

Isaac Todhunter Edited by Karl Pearson

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