

DYNAMICS.

- 1. This name marks that department of physico-mathematical science which contains the abstract doctrine of moving forces; that is, whatever necessarily results from the relations of our ideas of motion, and of the immediate causes of its production and changes.
- 2. All changes of motion are considered by us as the indications, the characteristics, and the measures of changing causes. This is a physical law of human thought, and therefore a principle to which we may refer, and from which we must derive all our knowledge of those causes. When we appeal to our own thoughts or feelings, we do not find in ourselves any disposition to refer mere existence to any cause, although the beginning of existence certainly produces this reference in an instant. Had we always observed the universe in motion, it does not appear that we should have ascribed it to a cause, till the observation of relative rest, or something leading to it, had enabled us to separate, by abstraction, the notion of matter from that of motion. We might then perceive, that rest is not incompatible with matter; and we might



2 DYNAMICS.

even observe, by means of relative motions, that absolute rest might be produced by the concourse of equal and opposite motions. But all this requires reflection and reasoning; whereas we are now speaking of the first suggestions of our minds.

- 3. We cannot have any notion of motion in abstracto, without considering it as a state or condition of existence, which would remain, if not changed by some cause. It is from changes alone, therefore, that we infer any agency in nature; and it is in these that we are to find all that we know of their causes.
- 4. When we look around us, we cannot but observe, that the motions of bodies have, in most cases, if not always, some relation to the situation, the distance, and the discriminating qualities of other bodies. The motions of the moon have a palpable relation to the earth; the motions of the tides have as evident a relation to the moon; the motions of a piece of iron have a palpable dependence on a magnet. The vicinity of the one seems to be the occasion, at least, of the motions of the other. The causes of these motions have an evident connection with or dependence on the other body. We are even disposed to imagine, that they are inherent in that body, and that it possesses certain qualities which are the causes of those modifications of motion in other bodies. These serve to distinguish some bodies from others, and may therefore be called PROPERTIES; and, since the condition of other bodies so evidently depends on them, these properties express very interesting relations of bodies, and are chiefly attended to in the enumeration of the circumstances which ascertain what we call the nature of any thing. We do not mean to say, that these inferences are always just; nay, we know that many of them are ill-founded: but they are real, and they serve abundantly for informing us what we may expect from any proposed situation of things. It is enough for us to know, that when a piece of iron is



DYNAMICS.

3

so and so situated in relation to a magnet, it will move in a certain manner.

This mutual relation of bodies is differently considered, according to the interest that we chance to take in the phenomenon. The cause of the approach of the iron to a magnet is generally ascribed to the magnet, which is said to attract the iron, because we commonly employ the magnet in order that these motions may take place. milar approach of a stone to the earth is ascribed to the stone, and we say that it tends to the earth. In all probability, the procedure of nature is the same in both; for they are observed, in every instance, to be mutual between the related bodies. As iron approaches a magnet, so the magnet approaches the iron. The same thing is observed in the motions of electrified bodies; also in the case of the Therefore the cause of the motions stone and the earth. may be conceived as inherent in either, or in both.

The qualities thus inherent in bodies, constituting their mechanical relations, have been called the MECHANICAL AFFECTIONS OF MATTER. But they are more commonly named powers or forces; and the event which indicates their presence, is considered as the effect and mark of their agency. The magnet is said to act on the iron, the earth is said to act on the stone; and the iron and the stone are said to act on the magnet and on the earth.

All this is figurative or metaphorical language. All languages have begun with social union, and have improved along with it. The first collections of words expressed the most familiar and the most interesting notions. In the process of social improvement, the number of words did not increase in the same proportion with the notions that became interesting and familiar in their turn: for it often happened that relations of certain ideas so much resembled the relations of certain other ideas, that the word expressing one of them served very well for expressing the other; because the dissimilar circumstances of the two



4 DYNAMICS.

cases prevented all chance of mistake. Thus we are said to surmount a difficulty, without attaching to the word the notion of getting over a steep hill. Languages are thus filled with figurative expressions.

5. Power, Force, and Action, are words which must have appeared in the language of the most simple people; because the notions of personal ability, strength, and exertion, are at once the most familiar and the most interesting that can have a place in the human mind. These terms, when used in their pure, primitive sense, express the notions of the power, force, and action of a sentient, active, being. Such a being only is an agent. The exertion of his power or force is (exclusively) action: But the relation of cause and effect so much resembles in its results the relation between this force and the work performed, that the same term may be very intelligibly employed for both. Perhaps the only case of pure unfigurative action is that of the mind on the body. But as this is always with the design of producing some change on external bodies, we think only of them; the instrument or tool is overlooked, and we say that we act on the external body. Our real action, therefore, is but the first movement in a long train of successive events, and is but the remote cause of the interesting event. The resemblance to such actions is very strong indeed in many cases of mechanical phenomena. A man throws a ball by the motion of his arm. A spring impels a ball in the same manner by unbending. These two events resemble each other in every circumstance but the action of the mind on the corporeal organ—the rest of it is a train of pure mechanism. In general, because the ultimate results of the mutual influence of bodies on each other greatly resemble the ultimate results of our actions on bodies, we have not invented appropriated terms, but have contented ourselves with those already employed for expressing our own actions, the exertions of our own powers or forces. The



DYNAMICS.

5

relation of physical cause and effect is expressed metaphorically in the words which belong properly to the relation of agent and action. This has been attended by the usual consequences of poverty of language, namely, ambiguity, and sometimes mistake, both in our reflections (which are generally carried on by mental discourse), our reasonings, and our conclusions. It is necessary to be on our guard against such mistakes; for they frequently amount to the confounding of things totally different. Many philoso-phers of great reputation, on no better foundation than this metaphorical language, have confounded the relations of activity and of causation, and even denied that there is any difference; and they have affirmed, that there is the same invariable relation between the determinations of the will and the inducements that prompt them, as there is between any physical power and its effect. Others have maintained, that the first mover in the mechanical operations, and indeed through the whole train of any complicated event, is a percipient and intending principle in the same manner as in our actions. According to these philosophers, a particle of gravitating matter perceives its relation to every other particle in the universe, and determines its own motion according to fixed laws, in exact conformity to its situation. But the language, and even the actions of all men, shew that they have a notion of the relation of an agent to the action, easily distinguishable (because all distinguish it) from the relation between the physical cause and its effect.

6. When we speak of powers or forces as residing in a body, and the effect as produced by their exertion, the body, considered as possessing the power, is said to acr on the other. A magnet is said to act on a piece of iron; a billiard ball in motion, is said to act on one that is hit by it: but if we attempt to fix our attention on this action, as distinct both from the agent and the thing acted on, we find no object of contemplation—the exertion or procedure



dynamics.

of nature in producing the effect does not come under our view. When we speak of the action as distinct from the agent, we find that it is not the action, properly speaking, but the act, that we speak of. In like manner, the action of a mechanical power can be conceived only in the effect produced.

- 7. A man is not said to act unless he produces some effect. Thought is the act of the thinking principle; motion of the limb is the act of the mind on it. In mechanics, also, there is action only in so far as there is mechanical effect produced. I must act violently in order to begin motion on a slide: I must exert force, and this force exerted produces motion. I conceive the production of motion, in all cases, as the exertion of force; but it requires no exertion to continue the motion along the slide; I am conscious of none, therefore I ought to infer that no force is necessary for the continuation of any motion. The continuation of motion is not the production of any new effect, but the permanency of an effect already produced. We indeed consider motion as the effect of an action; but there would be no effect if the body were not moving. Motion is not the action, but the effect of the action.
- 8. Mechanical actions have been usually classed under two heads: they are either Pressures or Impulsions. They are generally considered as of different kinds; the exertions of different powers. Pressure is supposed to differ essentially from Impulse.

Instead of attempting to define, or describe, these two kinds of forces and actions, we shall just mention some instances. This will give us all the knowledge of their distinctions that we can acquire.

When a ball lies on a table, and I press it gently on one side, it moves toward the other side of the table. If I follow it with my finger, continuing my pressure, it accelerates continually in its motion. In like manner, when I press on the handle of a common kitchen jack, the fly



DYNAMICS.

17

begins to move. If I continue to urge or press round the handle, the fly accelerates continually, and may be brought into a state of very rapid motion. These motions are the effects of genuine pressure. The ball would be urged along the table in the same manner, and with a motion continually accelerated, by the unbending of a spring. Also, a spring coiled up round the axis of the handle of the jack would, by uncoiling itself, urge round the fly with a motion accelerating in the same way. The more I reflect on the pressure of my finger on the ball, and compare it with the effect of the spring on it, the more clearly do I see the perfect similarity; and I call these influences, exertions, or actions, by one name, Pressure, taken from the most familiar instance of them.

Again, the very same motion may be produced in the ball or fly, by pulling the ball or the machine by means of a thread, to which a weight is suspended. As both are motions accelerated in the same manner, I call the influence or action of the thread on the ball or machine by the same name PRESSURE, and WEIGHT is considered as a pressing power. Indeed, I feel the same compression from the real pressure of a man on my shoulders, that I would feel from a load laid on them. But the weight in our example is acting by the intervention of the thread. By its pressure, it is pulling at that part of the thread to which it is fastened; this part is pulling at the next by means of the force of cohesion; and this pulls at a third, and so on, till the most remote pulls at the ball or the machine. Thus may elasticity, weight, cohesion, and other forces, perform the office of a genuine power; and since their result is always a motion beginning from nothing, and accelerating by perceptible degrees to any velocity, this resemblance makes us call them by one familiar name.

But farther, I see that if the thread be cut, the weight will fall with an accelerated motion, which will increase to any degree, if the length of the fall be great enough. I ascribe



8 DYNAMICS.

this also to a pressing power acting on the weight. Nay, after a very little refinement, I consider this power as the cause of the body's weight; which word is but a distinguishing name for this particular instance of pressing power. Gravitation is therefore added to the list of pressures; and, for similar reasons, the attractions and repulsions of magnets or electric bodies may be added to the list; for they produce actual compressions of bodies placed between them, and they produce motions gradually accelerated, precisely as gravitation does. Therefore all these powers may be distinguished by this descriptive name pressures, which, in strict language, belongs to one of them only.

Several writers, however, subdivide this great class into pressions and solicitations. Gravity is a solicitation ab extra, by which a body is urged downward. In like manner, the forces of magnetism and electricity, and a vast variety of other attractions and repulsions, are called solicitations. We see little use for this distinction, and the term is too like an affection of mind.

9. Impulsion is exhibited when a ball in motion puts another ball into motion by hitting, or (to speak metaphorically) by striking it. The appearances here are very different. The body that is struck acquires, in the instant of impulse, a sensible quantity of motion, and sometimes a very rapid motion. This motion is neither accelerated nor retarded after the stroke, unless it be affected by some other force. It is also remarked, that the rapidity of the motion depends, inter alia, on the previous velocity of the striking body For instance, if a clay ball, moving with any velocity, strike another equal ball which is at rest, the struck ball moves with half the velocity of the other. And it is farther remarkable, that the striking body always loses as much motion as the struck body gains. This universal and remarkable fact seems to have given rise to a confused or indistinct notion of a sort of transference of motion from one body to another. The phraseology in general



DYNAMICS.

use on this subject expresses this in the most precise terms. The one ball is not said to cause or produce motion in the other, but to communicate motion to it; and the whole phenomenon is called the communication of motion. We call this an indistinct notion; for surely no one will say that he has a clear conception of it. We can form the most distinct notion of the communication of heat, or of the cause of heat; of the communication of saltness, sweetness, and a thousand other things; but we cannot conceive how part of that identical motion which was formerly in A, is now infused into B, being given up by A. It is in our attempt to form this notion that we find that motion is not a thing, not a substance which can exist independently, and is susceptible of actual transference. It appears in this case to be a state, or condition, or mode of existence, of which bodies are susceptible, which is producible, or (to speak without metaphor) causable, in bodies, and which is the effect and characteristic of certain natural qualities, properties, or powers. We are anxious to have our readers impressed with clear and precise notions on this subject, being confident that such, and only such, will carry them through some intricate paths of mechanical and philosophical research.

10. The remarkable circumstance in this phenomenon is, that a rapid motion, which requires for the effecting it the action of a pressing power, continued for a sensible, and frequently a long time, seems to be effected in an instant by impulsion. This has tended much to support the notion of the actual transference of something formerly possessed exclusively by the striking body, inhering in it, but separable, and now transfused, into the body stricken. And now room is found for the employment of metaphor, both in thought and language. The striking body affects the body which it thus impels: It therefore possesses the power of impulsion, that is, of communicating motion. It possesses it only while it is in motion. This power, there-

O



10 DYNAMICS.

fore, is the efficient distinguishing cause of its motion, and its only office must be the continuation of this motion. It is therefore called the INHERENT FORCE, the force inherent in a moving body, vis insita corpori moto. This force is transfused into the body impelled; and therefore the transference is instantaneous, and the impelled body continues its motion till it is changed by some other action. All this is at first sight very plausible; but a scrupulous attention to those feelings which have given rise to this metaphorical conception, should have produced very different notions. I am conscious of exertion in order to begin motion on a slide; but if the ice be very smooth, I am conscious of no exertion in order to slide along. My power is felt only while I am conscious of exerting it: Therefore I have no primitive feeling or notion of power while I am sliding along. I am certain that no exertion of power is necessary here. Nay, I find that I cannot think of my moving forward without effort otherwise than as a certain mode of my existence. Yet we imagine that the partisans of this opinion did really deduce it in some shape from their feelings. We must continue the exertion of walking in order to walk on; our power of walking must be continually exerted, otherwise we shall stop. But this is a very imperfect, incomplete, and careless observation. Walking is much more than mere continuance in progressive motion. It is a continually repeated lifting our body up a small height, and allowing it to come down again. This renewed ascent requires repeated exertion.

11. We have other observations of importance yet to make on this force of moving bodies, but this is not the most proper occasion. Meanwhile we must remark, that the instantaneous production of rapid motion by impulse has induced the first mechanicians of Europe to maintain, that the power or force of impulse is unsusceptible of any comparison with a pressing power. They have asserted, that impulse is infinitely great when compared with pres-