

CAMBRIDGE LIBRARY COLLECTION

Books of enduring scholarly value

Technology

The focus of this series is engineering, broadly construed. It covers technological innovation from a range of periods and cultures, but centres on the technological achievements of the industrial era in the West, particularly in the nineteenth century, as understood by their contemporaries. Infrastructure is one major focus, covering the building of railways and canals, bridges and tunnels, land drainage, the laying of submarine cables, and the construction of docks and lighthouses. Other key topics include developments in industrial and manufacturing fields such as mining technology, the production of iron and steel, the use of steam power, and chemical processes such as photography and textile dyes.

The Electric Arc

An electric arc is formed when a current passes between two conductors through a non-conducting medium like air. Although the phenomenon was discovered during early electrical experiments and utilised widely in lighting by the end of the nineteenth century, its problems were not fully understood. First published in 1902, this book represents one of the first systematic investigations of the electric arc, and the best-known work of suffragist and electrical engineer Hertha Ayrton (1854–1923). It includes a chapter on the history of the discovery, over a hundred illustrations and tables, and Ayrton's explanation of the enduring problem of arc instability. As a result of her research, she went on to patent anti-aircraft lights and new arc-lamp technology. She later became the first female recipient of the Royal Society's Hughes Medal. Remaining relevant to students of electrical engineering and the history of science, this book shares her insights and expertise.



Cambridge University Press has long been a pioneer in the reissuing of out-of-print titles from its own backlist, producing digital reprints of books that are still sought after by scholars and students but could not be reprinted economically using traditional technology. The Cambridge Library Collection extends this activity to a wider range of books which are still of importance to researchers and professionals, either for the source material they contain, or as landmarks in the history of their academic discipline.

Drawing from the world-renowned collections in the Cambridge University Library and other partner libraries, and guided by the advice of experts in each subject area, Cambridge University Press is using state-of-the-art scanning machines in its own Printing House to capture the content of each book selected for inclusion. The files are processed to give a consistently clear, crisp image, and the books finished to the high quality standard for which the Press is recognised around the world. The latest print-on-demand technology ensures that the books will remain available indefinitely, and that orders for single or multiple copies can quickly be supplied.

The Cambridge Library Collection brings back to life books of enduring scholarly value (including out-of-copyright works originally issued by other publishers) across a wide range of disciplines in the humanities and social sciences and in science and technology.



The Electric Arc

HERTHA AYRTON





CAMBRIDGE UNIVERSITY PRESS

Cambridge, New York, Melbourne, Madrid, Cape Town, Singapore, São Paolo, Delhi, Mexico City

Published in the United States of America by Cambridge University Press, New York

www.cambridge.org Information on this title: www.cambridge.org/9781108052689

© in this compilation Cambridge University Press 2012

This edition first published 1902 This digitally printed version 2012

ISBN 978-1-108-05268-9 Paperback

This book reproduces the text of the original edition. The content and language reflect the beliefs, practices and terminology of their time, and have not been updated.

Cambridge University Press wishes to make clear that the book, unless originally published by Cambridge, is not being republished by, in association or collaboration with, or with the endorsement or approval of, the original publisher or its successors in title.





то

MADAME BODICHON,

WHOSE CLEAR-SIGHTED ENTHUSIASM FOR THE FREEDOM

AND ENLIGHTENMENT OF WOMEN ENABLED HER TO STRIKE

AWAY SO MANY BARRIERS FROM THEIR PATH;

WHOSE GREAT INTELLECT, LARGE TOLERANCE AND

NOBLE PRESENCE WERE AN INSPIRATION TO ALL

TO HER

WHO KNEW HER;

WHOSE FRIENDSHIP CHANGED AND BEAUTIFIED MY
WHOLE LIFE, I DEDICATE THIS BOOK,



THE ELECTRIC ARC.

By HERTHA AYRTON,

MEMBER OF THE INSTITUTION OF ELECTRICAL ENGINEERS.

LONDON:

"THE ELECTRICIAN" PRINTING AND PUBLISHING COMPANY, LIMITED,

SALISBURY COURT, FLEET STREET, E.C.

[All Rights Reserved.]



Printed and Published by
"THE ELECTRICIAN" PRINTING AND PUBLISHING CO., LIMITED,
1, 2, and 3, Salisbury Court, Fleet Street,
London, E.C.



PREFACE.

THIS book, which owes its origin to a series of articles published in The Electrician in 1895-6, has attained to its present proportions almost with the growth of an organic body. In experimenting on the arc, my aim was not so much to add to the large number of isolated facts that had already been discovered, as to form some idea of the bearing of these upon one another, and thus to arrive at a clear conception of what takes place in each part of the arc and carbons at every moment. The attempt to correlate all the known phenomena, and to bind them together into one consistent whole, led to the deduction of new facts, which, when duly tested by experiment, became parts of the growing body, and, themselves, opened up fresh questions, to be answered in their turn by experiment. Thus the subject grew and developed in what might almost be called a natural way.

From the first it seemed to me that the fact that the resistance of the material in the gap between the carbons must not only depend upon the current, but that it must depend upon it in many apparently contradictory ways, could not but lead to curious complications

A



iv. PREFACE.

in the relation between the P.D. and the current—quite apart from any back E.M.F. that the arc might possess. In the attempt to disentangle the various effects on this resistance that a change of current must produce, and to see how far all that was apparently mysterious in the arc might be the natural result of such complexity in the resistance of a portion of the circuit, the theory presented in Chapter XII. gradually evolved itself. This theory, whatever may be its shortcomings, has at least not been hastily built up to fit a few of the more salient characteristics of the arc; it has literally evolved itself, during the course of a detailed study, from many points of view, of each separate phenomenon. although the central idea, that the carbon vapour changed into mist at a short distance from the crater, occurred to me at a very early period of the work, its complete application to the whole series of phenomena, and the full recognition of all that it entailed, followed but slowly, as each part of the subject was considered in turn.

The experiments of other observers have been employed in two ways: (I) In confirmation of theory developed from my own experiments, and (2) as the basis of theory, for which further tests were devised. The law connecting P.D., current, and length of arc, for instance, was first constructed from my own results, and then was shown to be applicable to those obtained much earlier by Messrs. Edlund, Peukert, Cross and Shepard, and Ayrton. The theory concerning the light, on the other hand, was entirely deduced from the experiments of others. M. Blondel's interesting and systematic researches, the admirable work of Mr. Trotter, and Prof. Ayrton's Chicago Paper were all laid under



PREFACE.

v.

contribution, and the deductions drawn from them were then tested by new experiments.

In seeking to compare my results with those of other observers, and in searching for accounts of experiments that might furnish material for theory, I have often been struck with the excellent work that has been done by men whose names are quite unfamiliar to us in England. There are admirable Papers on the arc, for instance, by Nebel, Feussner, Luggin, Granquist, and Herzfeld, to which reference is seldom seen in any English publication; while other work, which is in some cases far inferior, is constantly quoted. I have, therefore, given in Chapter II. short abstracts of most of the important Papers on the direct-current arc that appeared up to the end of the nineteenth century, while those referring principally or entirely to the light are discussed in Chapter XI. At the end of Chapter II. is a chronological list of all the original communications that I could find when that chapter was written; but the names of a few to which my attention has since been directed, and of some that appeared after the list was made, together with the dates of my own contributions to The Electrician and to various societies, are added at the end of the Appendix. The latest paper of allan extremely interesting one "On the Resistance and Electromotive Forces of the Electric Arc," read by Mr. Duddell before the Royal Society in June last-I should much have liked to discuss in connection with this book, but, as it is not yet published in full, that is unfortunately impossible.

As it seemed better not to wait till the whole book was ready, before publishing the most important of the new results obtained, some part of almost every chapter

a 2



vi. PREFACE.

has been made the subject of a Paper that has been read before one or other of the societies interested in such work. These Papers generally covered but a portion of the ground, however, giving the main experiments and conclusions only, without following them up, or showing how they bore upon one another. In the book these are all connected together, and many new results are set forth which have been developed during the process. At the end of each chapter is a summary of the most important conclusions reached in it, which, it is hoped, may be found useful in making each step perfectly clear before the next is taken.

Besides the light experiments already mentioned, all those on the time-change of P.D. immediately after starting the arc, and after sudden changes of current, originally formed part of Prof. Ayrton's ill-fated Chicago Paper, which, after being read at the Electrical Congress in 1893, was accidentally burnt in the Secretary's office, whilst awaiting publication. These highly important experiments were not only the first of their kind, but, as far as I know, they still remain unique. Most of the figures in the first chapter, all the experiments and curves that relate to cored carbons in the fourth and fifth, and some of those on hissing in the tenth, also belonged to this Chicago Paper, which was as full of suggestion as it was rich in accomplished work.

Although the book is concerned entirely with the arc itself, and does not touch at all upon lamps and their devices, it is hoped that it may appeal to the practical man as well as to the physicist. For not only the cause but the practical bearing of each peculiarity of the arc has been considered; the directions in which improvements may be hoped for have been pointed out,



PREFACE.

vii.

and the conditions requisite to secure the maximum production of light from a given expenditure of power in the generator have been fully discussed.

In conclusion, I have to thank Prof. Blondel, Prof. Fleming and Mr. Trotter for kind permission to use figures from their Papers; Mr. Fithian for taking the beautiful photographs of the Hissing Arc reproduced in Fig. 81; Mr. Mather for much valuable advice and assistance with experiments, and Mr. Maurice Solomon for his suggestive criticism of the MS. and careful revision of the proofs.

HERTHA AYRTON.





ix.

PAGE

TABLE OF CONTENTS.

CHAPTER I.

THE APPEARANCE OF THE ARC	1
Colours of Different Parts of Arc.—General Shapes of Arc and Carbons.—Influence of Current and Length of Arc on Shape and Size of Arc and Shapes of Carbons.—Positive Crater.—Effect of Core on Colour, Size and Shape of Arc.—Crater in Negative Carbon.	
CHAPTER II.	
A SHORT HISTORY OF THE ARC	19
Uncertainty of Discoverer and of Date of Discovery of Arc.— Mutual Attraction between Arc and Magnet.—First Observation of Crater, "Mushrooms," Smell of Arc, and Difference of Temperatures of Electrodes.—Application of Laws of Elec- trolysis to Arc.—Experiments on Arcs in Various Gases.— Photographic Power of Arc.—First Experiments on Arcs between Carbons Steeped in Metallic Salts.—Hissing.—Trans- ference of Matter from One Pole to the Other.—Electric Blowpipe.—Water as One Electrode.—Edund's Discovery of Straight Line Law of Resistance and Length of Arc, and Suggestion of a Back E.M.F.—Fall of P.D. with Hissing.— Internal Pressure of Arc.—Measurements of P.D. and Current with Constant Lengths of Arc.—Measurements of Supposed True Resistance of Arc.—Tests for Back E.M.F.—Determinations of Temperatures of Electrodes.—Arcs under Pressure.—Measure- ments of Light.—Rotation.—Apparent Negative Resistance.— Attraction of Solid Carbon Particles out of Arc.—Suggested "Thomson Effect" in Arc.—List of Original Communications.	



X.

Cambridge University Press 978-1-108-05268-9 - The Electric Arc Hertha Ayrton Frontmatter More information

TABLE OF CONTENTS.

CHAPTER III.

"Striking" the Arc and Sudden Variations of Current 97

Impossibility at First of getting Definite P.D. with Fixed Current and Length of Arc.—Cause of Difficulty.—Low P.D. and Subsequent Rapid Rise on Striking Arc with Cored Positive Carbon.—Influence of Current, Length of Arc, and Shapes and Temperatures of Carbons on Time Required for P.D. to become Constant after Striking Arc.—First Rise of P.D. with Increase of Current with Cored Carbons.—Peculiar Changes of P.D. with Sudden Changes of Current, and their Causes.—Summary.

CHAPTER IV.

General Character of Curves for P.D. and Current with Constant Length of Arc for Solid Carbons.—Same with Positive Carbon Cored.—Discussion of Variations Caused by Core.—Different Positions of Hissing Points with Solid Carbons and with Positive Carbon Cored.—Influence of Strength of Current on Diminution of P.D. due to Core.—Hypothesis as to Action of Core in Modifying P.D.—Curves showing Straight Line Law connecting P.D. with Length of Arc, for Constant Current, with Solid Carbons.—Curves for Same Connection with Cored Positive Carbon, showing P.D. Practically Independent of Current for One Length of Arc.—Discussion of Differences between the Two Sets of Curves, and Explanation, on Abovementioned Hypothesis.—Soft and Hard Crater Ratios.—Deductions from them as to Influence of Current and Length of Arc on Area of Crater.—Summary.

CHAPTER V.

Measurements of Diameter of Crater with Arc Burning.—Curves of Area of Crater and P.D. between Carbons for Various Currents and Lengths of Arc.—Curves of Area of Crater and Length of Arc, of Soft Crater Ratio and Length of Arc, and of



TABLE OF CONTENTS.

хi.

Hard Crater Ratio and P.D.—Curves of Area of Crater and Current.—Measurements of Depth of Crater.—P.D. Uninfluenced by Depth of Crater.—Comparison of P.Ds. for Same Current and Length of Arc but Different-sized Carbons.—Curves of Apparent Resistance and Length of Arc.—Constant P.D. Curves.—Summary.

CHAPTER VI.

Two Fundamental Straight Line Laws Found to Exist with Solid Carbons.—Power and Length of Arc with Constant Current, and Power and Current with Constant Length of Arc.—Equation for Power, Current, and Length of Arc found by Combining these.—Equation for P.D., Current and Length of Arc, Deduced from it, having Four Constants Depending Solely on Nature of Carbons.—Straight Line Power Laws Shown to Fit Experiments of Edlund, Frölich, Peukert, and Cross and Shepard, and Equations for P.D., Current and Length of Arc similar to Above, Deduced from their Results.—Summary.

CHAPTER VII.

THE P.D. BETWEEN EACH CARBON AND THE ARC, AND THE FALL OF POTENTIAL THROUGH THE ARC 207

Repulsion and Attraction of Arc, and other Disturbances caused by Third Carbon.—Definitions of Positive Carbon P.D., Negative Carbon P.D., Vapour P.D.—Variation of Positive Carbon P.D. with Current and Length of Arc.—Resemblances and Differences between Positive Carbon P.D. Curves and Total P.D. Curves.—Variation of Negative Carbon P.D. with Current, but not with Length of Arc.—Curves and Equation for Positive Carbon P.D., Current and Length of Arc ; Negative Carbon P.D. and Current; and Sum of Carbon P.Ds., Current and Length of Arc.—Similarity between Independent Constant in the Last Equation and Similar Constant in Equation for Total P.D., Current and Length of Arc, Showing that if this Latter Represents a Back E.M.F., it must be Located at Junctions of the Two Carbons with the Arc.—Equation for Total P.D., Current and Length of Arc with Third Carbon in Arc.—Location of P.Ds. Represented by Three out of



xii.

TABLE OF CONTENTS.

PAGE

Four Terms of Equation for Total P.D., Current and Length of Arc.—Measurements of Carbon P.Ds., Plus Vapour P.D.—Carbon and Vapour P.Ds. with Cored Carbons.—Diminution of P.D. due to Core Traced to Junction of Positive Carbon and Arc, and to Lowering of Resistance of Vapour Column.—Summary.

CHAPTER VIII.

Graphical Method of Finding Relations between E.M.F. of Generator, Resistance in Series with Arc, P.D., Current and Length of Arc.—Impossibility of Keeping either Current or Length of Arc really Constant.—Greatest Length of Arc possible with Given Resistance in Series.—Reason for Difficulty frequently found in Maintaining Long Arcs with Small Currents.—Necessity of "Steadying Resistance" in order that Silent Arc may be Maintained at all.—Variation of Minimum Value of Steadying Resistance with Current and Length of Arc.—Longest Silent Arc and Smallest Current that can be Maintained with Given E.M.F. and Resistance in Series with Arc.—Largest Resistance and Smallest Current that can be Used with Given E.M.F. and Length of Arc.—Largest Resistance and Longest Arc that can be Maintained with given E.M.F. and Current.—Summary.

CHAPTER IX.

General Conditions for Ratio of Power Expended in Arc to Power Developed by Generator (Power Efficiency) to be Greatest Possible.—Conditions for Power Efficiency to be Greatest Possible (1) when Length of Arc alone is Fixed, (2) when E.M.F. alone is Fixed, (3) when Current alone is Fixed, (4) when Resistance in Series alone is Fixed, (5) when P.D. alone is Fixed.—Minimum Resistance that can be used in Series with Arc varies Inversely as Square of Current for Fixed Length of Arc.—Minimum Resistance Required to Maintain Silent Arc at all Depends only on Nature of Carbons.—Summary.



TABLE OF CONTENTS.

xiii.

CHAPTER X.

PAGE 977

Variety of Hissing Sounds.-Hissing Arc not necessarily Short .-Instability of Arc about Hissing Point.—Laws of Hissing from P.D.-Current Curves.—Cross and Shepard's and Luggin's Experiments.—Equation to Curve on which Hissing Points Lie.— Largest Current with which Arc, however long, can Remain Silent-Equation for P.D. and Length of Arc with Hissing .-Fall of P.D. at Positive Carbon, and Diminution of Resistance of Arc, with Hissing.—Equation Connecting Change of P.D. when Hissing Begins with Length of Arc.—Smallest Hissing Current with given Length of Arc.-Connection between Largest Silent and Smallest Hissing Current of same Arc.—Change in Appearance of Crater, Arc, and Carbons with Hissing .- Crater more than Covering End of Positive Carbon with Hissing.—Laws of Hissing Deduced from Shapes of Positive Carbons with various Currents. -Cause of Hissing.—Experiments on Arcs enclosed in Crucible.— Blowing Various Gases against Crater.—Different Behavour of Arc when Hydrogen is Blown against Crater in Open Air and in

CHAPTER XI.

Crucible.—Cause of Hissing Sound.—Summary.

THE LIGHT AND LUMINOUS EFFICIENCY OF THE ARC. ... 313

Sources of Light in Arc.—Obstruction of Crater Light by Negative Carbon.—Trotter's Theorem.—Quantity of Light Obstructed by Negative Carbon Estimated from Diagrams of Arc and Carbons.— Reason for Light being Greater with very short Arcs than with longer ones, with Large Currents.-Measurements of Mean Spherical Candle-Power of Arc (W. E. Ayrton) and Total Light of Arc (Blondel)-Simultaneous Discovery of Certain Length of Arc and Certain P.D. with which the Light is a Maximum for a Constant Current.-Curves Connecting Crater Light with Length of Arc, Deduced from Diagrams of Arc and Carbons.-Distinction between Polar Light Curves, Rousseau's Curves, and Curves connecting Illuminating Power with Length of Arc.-Suggested Absorption of Crater Light by Arc.-Facts tending to show that Arc does Absorb Light.—Experiments on Shadows of Candle and Gas Flames. -- Arc Shadow. -- Refractive Power of Arc Mist.—Arc Vapour turning into Carbon Mist.—Violet Colour of Long Arcs as Proof of Absorption.-Light, Length of Arc Curves, from Diagrams of Arc, allowing for Absorption of Crater Light in Arc.—Similarity between these and Experimental Curves.-Effect of Variation of Current on Total Light emitted by Arc.—Very small Luminous Efficiency of all sources of Light, Even Arc. - Distribution of Power supplied to Arc between



xiv.

TABLE OF CONTENTS.

PAGE

Carbon Ends and Mist.—Waste of Power in Mist in Long Arcs.—Conditions for Light to be Maximum for given Power developed by Generator.—Influence of Cross Sections of Carbons on Lighting Power.—With Solid Carbons Light Efficiency is greater, and Arc with which Maximum Light Efficiency is obtained is Shorter the Smaller the Carbons.—Low Efficiency of Commercial Arc Lamps due to Thickness of Carbons.—Variation of Light Efficiency with Current.—Effect of Composition of Carbons on Light Efficiency.—Arcs in Series.—Only Fair Method of Comparing Light Efficiency of Two Sources.—Summary.

CHAPTER XII.

THE MECHANISM OF THE ARC—ITS TRUE RESISTANCE—HAS
IT A LARGE BACK E.M.F.?—THE REASON FOR THE
DIFFERENT EFFECTS OF SOLID AND CORED CARBONS...

39**1**

How Arc forms on Separating Carbons.—Changing of Vapour into Carbon Mist,—Resistivities of Vapour, Mist, and Flame.—Source of Heat of Arc.—Hollowing of Crater.—Shaping of Carbons.—Dependence of Area of Crater on both Current and Length of Arc.—Imitation of Back E.M.F. by Vapour Film.—Time-Change of Resistance of Arc.—Effect of Frequency of an Added Alternating Current on Value and Sign of $\frac{\delta V}{\delta A}$.—Curve of $\frac{\delta V}{\delta A}$ and Frequency.—Frequency with which $\frac{\delta V}{\delta A}$ Measures True Resistance of Arc.—Tests for this Frequency.—Two Ways in which Cores in Carbons may Affect Resistance of Arc.—How Cores Affect Mean Cross Section of Mist.—How they Affect Resistivity

tance of Arc.—Tests for this Frequency.—Two Ways in which Cores in Carbons may Affect Resistance of Arc.—How Cores Affect Mean Cross Section of Mist.—How they Affect Resistivity of Arc and thus Alter Shapes of P.D.-Current Curves.— Influence of Cores on Value of $\frac{\delta V}{\delta A}$, (1) in Change of Cross Section, (2) in Change of Specific Resistance—Curves Connecting $\frac{\delta V}{\delta A}$ with Current, for Constant Length of Arc, with Length of Arc for Constant Current, and with Frequency of Alternating Current, for both Solid and Cored Carbons.— Summary.

APPENDIX.

445

Apparent Area of Disc Viewed from Any Distance.—Our Method of Estimating Brilliancy of a Source of Light.—Assumptions Made in Photometry.—Mean Spherical Candle Power and Total Light.— Measurement of Either, by Means of Rousseau's Figures.—Why Area of Polar Light Curve Cannot Measure Either.—Candle and Gas Shadow Experiments.—Supplementary List of Original Communications.



LIST OF ILLUSTRATIONS.

FIG.		PAGE
1	Image of Arc and Carbons, Five Times Full Size	3
2	Section of Positive Carbon Showing Outer Crust Curling Away	5
3	Drawing of Arc and Carbons with both Carbons Solid-4 mm.	_
	20 ampere Arc facing	6
4	Drawing of Arc and Carbons with both Carbons Solid—7 mm.	_
_	20 ampere Arc facing	6
5	Drawing of Arc and Carbons with Cored Positive and Solid	
	Negative Carbon—7 mm. 20 ampere Arc facing	7
6	Drawing of Arc and Carbons with Cored Positive and Solid	
	Negative Carpon—18 mm. 20 ampere Arc facing	7
7	Diagrams of Arcs of various Lengths and with various Currents,	
	between 18 mm. Cored Positive and 15 mm. Solid Negative	
	Carbons (W. E. Ayrton)	9
8	Diagrams of Arcs of various Lengths and with various Currents,	
	between 13 mm. Cored Positive and 11 mm. Solid Negative	
	Carbons (W. E. Ayrton)	10
9	Diagrams of A cs of various Lengths, and with various Currents,	
	between 9 mm. Cored Positive and 8 mm. Solid Negative	
	Carbons (W. E. Ayrton)	12
10	Diagrams or Carpons before and after Sudden Changes of	
	Current (W. E. Ayrton)	15
11	Diagrams of Arcs between Solid Carbons (W. E. Ayrton)	15
12	Diagrams of Arcs between Solid Positive and Cored Negative	*0
	Carbons (W. E. Ayrton)	16
13	Horizontal Arc copied from "Davy's Elements of Chemical	10
10	TO 1 1 11	27
14	Figure sho ing the Rotation of the Arc at the Pole of a Magnet	29
		49
15	Vertical Parallel Carbons showing the Position the Arc takes	7.0
	up near the ends (W. E. Ayrton)	36
16	Apparatus for Measuring the Resistance of the Arc (Von Lang)	43
17	Apparatus for Testing for a Back E.M.F. in the Arc (Lecher)	52
18	Curves showing Conditions for Arc to be Stable (Blondel)	62
19	Apparatus for Testing the Conductivity of the Arc (Fleming)	70



xvi.	LIST OF ILLUSTRATIONS.	
FIG.		PAGE
20	Apparatus for Measuring the Resistance of the Arc (Frith)	73
21	Apparatus for Measuring the Resistance of the Arc (Frith and Rodgers)	76
2 2	Curves Connecting the Instantaneous dV/dA with the Current	
2 3	for a Constant P.D. (Frith and Rodgers) Curves Connecting the Instantaneous dV/dA with the P.D. for	79
•	a Constant Current (Frith and Rodgers)	80
24	Apparatus for Measuring the Back E.M.F. of the Arc (Arons)	82
25	Illustration of Experiments on Particles Shot out from Carbons (Herzfeld)	85
26	Apparatus for Testing for a Back E.M.F. in the Arc (Blondel)	88
27	Apparatus for Testing for a Back E.M.F. in the Arc (Granquist)	92
28	Hand Fed Arc Lamp	98
29	Plan of Arc Lamps, Lens, Mirror and Diagram Screen for	
	Magnifying the Image of the Arc	99
30	P.D. and Current Curves drawn before the Time-Variability of	
	the P.D. was Realised (W. E. Ayrton)	101
31	Curves for Time-Change of P.D. with Constant Current and	
	Length, after starting the Arc between Cored Positive and	
	Solid Negative Carbons (W. E. Ayrton)	103
32	Curves for Time-Change of P.D. with Constant Current and	100
04	Length, after starting the Arc between Carbons of various	
	kinds, with ends variously shaped (W. E. Ayrton)	105
33	The same (W. E. Ayrton)	107
34	Curves showing the Influence of the Shape of the Negative	101
04		109
35	Carbon on the Time-Change of P.D. (W. E. Ayrton)	109
33		110
7.		110
36	Curves for Time-Change of P.D. with Sudden Changes of Current, showing the Influence of a Core in the Positive Carbon	
	(W. E. Ayrton)	113
37	Curves for Time-Change of P.D. with Sudden Changes of Current,	
	Showing the Influence of the Length of the Arc (W. E. Ayrton)	114
38	Curves connecting the P.D. with the Current for various	
	Constant Lengths of Arc, with Solid Carbons	120
39	The same, with 18 mm. Cored and 15 mm. Solid Carbons (W. E.	
	Ayrton)	128
40	The same with 13 mm. Cored and 11 mm. Solid Carbons (W. E.	
	Ayrton)	129
41	The same with 9 mm. Cored and 8 mm. Solid Carbons (W. E.	
	Ayrton)	130
42	Curves showing the Changes in the P.D. produced by Coring	
	the Positive Carbon (W. E. Ayrton)	132
43	Hypothetical Curves of P.D. and Current, for a Constant	
	Length of Arc, showing the Effect of Coring the Positive	
	Carbon	134
44	Curves connecting P.D. and Length of Arc for various Constant	
	Currents. Solid Carbons	136
		_00



	LIST OF ILLUSTRATIONS.	xvii.
FIG.		PAGE
45	The same with 18 mm. Cored and 15 mm. Solid Carbons (W. E. Ayrton)	139
46	The same with 13 mm. Cored and 11 mm. Solid Carbons (W. E. Ayrton)	140
47	The same with 9 mm. Cored and 8 mm. Solid Carbons (W. E. Ayrton)	140
48	The same with both Carbons Cored (W. E. Ayrton)	142
49	Hypothetical Curves of P.D. and Length of Arc, for a Con-	
43	stant Current, showing the Effect of Coring the Positive	144
50	Curves connecting the Area of the Crater with the P.D. between	277
	the Carbons, for various Constant Currents	153
51	Curves connecting the Area of the Crater with the Length of the Arc, for various Constant Currents	1.55
5 0	Curves connecting the Soft Crater Ratio with the Length of the	100
52	Arc, for various Constant Currents	156
53	Curves connecting the Hard Crater Ratio with the P.D. between	
	the Carbons, for various Constant Currents	157
54	Curves connecting the Area of the Crater with the Current, for	
	various Constant Lengths of Arc	159
55	Curves connecting the P.D. between the Carbons with the	
	Length of the Arc, for Cored Positive and Solid Negative	
	Carbons of various Diameters	163
56	Curves connecting the Apparent Resistance of the Arc with its Length, for various Constant Currents, with 18 mm. Cored	
	and 15 mm, Solid Carbons	164
57	The same with 13 mm. Cored and 11 mm. Solid Carbons	165
58	The same with 9 mm. Cored and 8 mm. Solid Carbons	166
5 9	Curves connecting Current with Length of Arc for various Constant P.Ds	169
60	Curve connecting Current with Time for a Constant P.D. and Length of Arc	171
61	Curves connecting P.D. with Current, for various Constant Lengths of Arc, with Solid Carbons	177
62	Curves connecting Power expended in Arc with Length of Arc,	
	for various Constant Currents, with Solid Carbons	180
63	Curves connecting Power with Current, for Lengths of Arc 0 mm. and 7 mm., with Solid Carbons	182
64	Hyperbola connecting P.D. with Current, for a Constant Length	
	of Arc, with Solid Carbons	187
65	Curves connecting Power with Length of Arc, for various Constant Currents, from Peukert's Experiments	194
66	Curves connecting Power with Current, for Lengths of Arc 0 mm.	
	and 10 mm., from Peukert's Experiments	196
67	Curves connecting Power with Length of Arc for various	100
68	Constant Currents, from Cross and Shepard's Experiments Curves connecting Power with Current for Lengths of Arc 0	199
JU	and $\frac{1}{32}$ inch, from Cross and Shepard's Experiments	200



xviii	. LIST OF ILLUSTRATIONS.	
FIG.		PAGE
69	Diagrammatic Representation of Apparatus used for Finding	
	the P.D. between each Carbon and the Arc	209
70	Diagrammatic Representation of various Arrangements of	
	Main and Exploring Carbons	213
71	Curves connecting Positive-Carbon P.D. with Current, for	
	various Constant Lengths of Arc	215
72	Curves connecting Positive-Carbon P.D. with Length of Arc, for	210
14	various Constant Currents	216
73	Curves connecting Negative-Carbon P.D. with Current, for	210
10		218
74	various Constant Lengths of Arc	210
14		219
	various Constant Currents	219
7 5	Curves connecting Positive-Carbon Power with Length of Arc,	000
	for various Constant Currents	220
7 6	Curves connecting Positive-Carbon Power with Current, for	
	various Constant Lengths of Arc	221
77	Curve connecting Negative-Carbon Power with Current for any	
	Length of Arc	224
78	Curves connecting Positive-Carbon P.D. plus Negative Carbon	
	P.D. with Current, for various Constant Lengths of Arc	226
79	Curves used for determining graphically the Relations between	
	the E.M.F. of the Dynamo, the outside Resistance in the	
	Circuit, the P.D., Current, and Length of Arc with Solid	
	Carbons	242
08	Curves connecting P.D. with Current, for various Constant	
	Lengths of Arc, with Solid Carbons	280
81	Photographs of Arcs-immediately after Hissing has begun,	
	after Hissing has continued some time, and when the Arc has	
	become Silent again facing	292
82	Diagram of a Short Hissing Arc	293
83	Diagrams of a Silent and a Hissing Arc	294
84	Diagrams of Arcs and Carbons with Current increasing from	
٠.	6 amperes, silent, to 30 amperes, hissing	295
85	Diagrams of Arcs and Carbons with the same Current and	200
00	Length of Arc, but different sized Carbons	296
86	Crucible Employed for Experiments on Enclosed Arcs	302
87	Curves connecting P.D. with Current for a nearly Constant	004
0,		704
88	Disable and the second of the	304
		317
89	Tracings of "Normal" Arc (Trotter)	318
90	Tracings of Short Arc (Trotter)	319
91	Polar Curves of Apparent Area of Crater and Candle Power in	
	"Normal" Arc (Trotter)	320
92	Polar Curves of Apparent Area of Crater and Candie Power in	
	Short Arc (Trotter)	321
93	Curve connecting Apparent Area of Crater with Light of	
	"Normal" Arc (Trotter)	322



	LIST OF ILLUSTRATIONS.	xix.
FIG.		PAGE
94	Diagrams of Arcs and Carbons for showing the Variation in the Shape of the Negative Carbon with the same Current but	
95	different Lengths of Arc	324
	Candle Power of the Arc (W. E. Ayrton)	326
96	General Plan of Apparatus for Measuring the Mean Spherical Candle Power of the Arc (W. E. Ayrton)	327
97	Curves connecting Mean Spherical Candle Power with Length of Arc, for various Constant Currents (W. E. Ayrton)	329
98	Curves connecting Total Light emitted with Length of Arc for a Constant Current	330
991		
100)	the Arc (Blondel)	331
101	Curves connecting Total Light with Length of Arc for a Constant Current with Solid Carbons of various sizes (Blondel)	333
102	Curves connecting Total Light with Length of Arc, for a Constant Current, with Cored Positive and Solid Negative Carbons of	
	various Sizes (Blondel)	334
103	Diagrams of Arcs of different Lengths, with the same Current, between the same Carbons	336
104	Area proportional to Total Light that would be received from the	
	Crater if none were obstructed by the Negative Carbon	338
105	Area proportional to Total Light actually received from Crater	339
106	Diagram of Arc and Carbons with Lines for finding the Quantity	
	of Light Obscured by the Negative Carbon in any one direction	340
107	Geometrical Construction for the Area of Crater Obscured by the Negative Carbon in any one direction	341
108	Curves connecting Light received from Crater with Length of	0.1
	Arc, obtained from Diagrams in Fig. 103	343
109	Photograph of Candle Flame	3 50
110	Section of Apparatus used for Observing the Shadow of the Arc	353
111	The Light from the Crater, the Arc Mist, and the White Spot, passing through a narrow Slit on to a White Screen	358
112	Band of Violet Light, bordering a Shadow made by intercepting the Light of the Crater of an Arc	359
113	Arc with Mist divided into Layers of Equal Thickness	361
114	Hypothetical Curves obtained from Fig. 108 by allowing for	
	the Absorption of Crater Light by the Arc Mist	363
115	Diagrams of Arc and Carbons, showing the Effect on the Shapes of both Carbons of varying the Current with a Constant Length of Arc	765
116	Curves connecting the Mean Spherical Candle Power of the Arc with the Current, for Constant Lengths of Arc of 1 mm.	365
117	and 4 mm. (W. E. Ayrton)	366
•	Current, for a Constant P.D. of 45 volts (Blondel)	367
	A	*



xx.	LIST OF ILLUSTRATIONS.	
FIG.		PAGE
118	Curves connecting the Power supplied to the Arc and the Power absorbed by the Mist with the Length of the Arc, for a Constant Current of 10 amperes	373
1 19	Curve showing the proportion of the whole Power supplied to the Arc that is Wasted in the Mist, with a Constant Current	010
120	of 10 amperes	373
.120	Diagrams of Arc and Carbons with the same Current and Length of Arc, but different sized Carbons	376
121	The same	379
122	Curves connecting Light Efficiency with Length of Arc for a Constant Current of 10 amperes with Solid Carbons (Blondel)	381
123	The same with Cored Positive and Solid Negative Carbons (Blondel)	382
124	Curves connecting Light Efficiency with Length of Arc for a	385
125	Constant P.D. (Blondel)	395
126	Hypothetical Areas of Volatilisation and Non-volatilisation in	397
127	Shapes assumed by the Positive Carbon, with the same Area of Volatilisation, but with a Long Arc in the one Case and a	001
128	Short Arc in the other	398
	fully Outlined	401
129	Curve connecting the Power Expended in the Arc Mist with the Current, for a Constant Length of Arc of 2 mm.	403
130	Curves showing Simultaneous Time-Changes of P.D., Current and Resistance	405
131	Curves showing the Effect of the Frequency of an Alternating Current, Superimposed on a Direct Current Arc, on the Simultaneous Time-Changes of P.D. and Current	408
132	Curves connecting Values of $\frac{\delta V}{\delta A}$ with the Frequency of the	
	Superimposed Alternating Current	412
133	Curves connecting the Mean Cross Section of the Arc Mist with the Current, for a Constant Length of Arc, with Solid-	400
134	Solid, Solid-Cored, Cored-Solid, and Cored-Cored Carbons Hypothetical Curves Exemplifying the Changes, in the Curve connecting P.D. with Current for a Constant Length of Arc,	420
176	caused by a Core in the Positive Carbon δV_{δ}	423
135	Hypothetical Curves connecting $\frac{\delta V_s}{\delta A}$ with the Current, for a	070
136	Constant Length of Arc	430
100	Constant Length of Arc	432
137	Constant Length of Arc	
101		
	Constant Length of Arc	404



	LIST OF ILLUSTRATIONS.	xxi.
FIG.		PAGE
138	Hypothetical Curve of Time-Change of P.D. Accompanying a Sudden Change of Current	435
139	Sudden Change of Current	
	for a Constant Current	436
140	Hypothetical Curves Connecting $\frac{\delta V}{\delta A}$ with the Frequency of an	
	Addel Alternating Current	438
141 } 142 }	Figures Used in Finding the Apparent Area of a Disc \dots \dots	{ 416 { 447
143 /	Figures Used in Finding an Area Proportional to the Mean Spheri-	
144 (cal Candle Power of an Axially Symmetrical Source of Light	453
145	Polar Light Curves of Two Similar Sources, the one having	
	twice the Illuminating Power of the other	455
146	Photograph of the Shadow of a Candle Flame	457





xxiii.

LIST OF TABLES.

_		PAGE
	Current, Resistance, and E.M.F. of Arc (Schwendler)	
	Areas of Crater with Different Currents	
	P.Ds. with Silent and Hissing Arcs (Niaudet)	_
	P.D. Current and Length of Arc (Nebel)	-
	P.Ds. for Different Conditions of the Arc (Lecher)	
VI.	P.Ds. with Constant Current and Varying Lengths of Arc	
	(Luggin)	
VII.	P.D. between Carbons with and without a Sprinkling of	
	Soda (Luggin)	56
VIII.	Current Density and Area of Tip of Positive Carbon	
	(Luggin)	
	Experiments to Find Back E.M.F. of Arc (Blondel)	
	Experiments to Find Back E.M.F. of Arc (Granquist)	
XI.	P.D. for Normal 5mm. Are with Various Constant	
	Currents (Solid Carbons 11/9)	
XII.	P.D. and Current with Various Constant Lengths of Arc	
	(Solid Carbons 11/9)	
XIII.	Same as above (Cored Positive and Solid Negative	
	Carbons 18/15) (W. E. Ayrton)	125
XIV.	Same as above (Carbons 13/11)	126
	Same as above (Carbons 9/8)	
XVI.	Diameter of Crater, Square of Diameter, P.D., and	
	Current for Various Lengths of Arc	
XVII.	Diameters of Crater, Observed and Calculated, for Various	
	Currents and Lengths of Arc	154
XVIII.	Crater Ratios for Various Currents and Lengths of Arc	156
XIX.	Depth of Crater with Different Currents and Lengths of	•
	Arc	160
XX.	Influence of Diameters of Carbons (Positive Cored) on P.D.	162
	Comparison of Observed and Calculated P.Ds. for Different	,
	Currents and Lengths of Arc (Solid Carbons 11/9)	185
XXII.	Edlund's Results referred to General Equation for P.D.,	
		190



xxiv. LIST OF TABLES.

		PAGE
XXIII.	Frölich's Results referred to General Equation for P.D.,	
		192
		195
XXV.	Cross and Shepard's Results referred to the same Equation	201
XXVI.	Duncan Rowland and Todd's Results referred to the same	
		204
XXVII.	Positive Carbon P.Ds. for Various Currents and Lengths	04.4
********	of Arc (Solid Carbons 11/9)	214
XXVIII.	Negative Carbon P.Ds. for Various Currents and Lengths	015
3737137	of Arc (Solid Carbons 11/9) Calculated Values of Positive Carbon P.Ds. (Solid	217
XXIX.		007
****	Carbons 11/9)	223
A.A.A.		225
VVVI	Sum of Positive and Negative Carbon P.Ds., for Various	440
ддаі,	Currents and Lengths of Arc (Solid Carbons 11/9)	997
vvvii	Calculated Values of Sum of Positive and Negative	441
XXXII.	Carbon P.Ds. (Solid Carbons 11/9)	227
XXXIII.	P.D. between Carbons with Third Carbon in Arc near	
11,11,11,11,11,11,11,11,11,11,111,11	· · · · · · · · · · · · · · · · · · ·	229
XXXIV.	P.D. between Carbons with Third Carbon in Arc near	
	Negative Carbon (Solid Carbons 11/9)	229
XXXV.	Mean P.D. between Carbons with Third Carbon in Arc	
	(Solid Carbons 11/9)	230
XXXVI.	Calculated Values of P.D. between Carbons with Third	
	Carbon in Arc (Solid Carbons 11/9)	231
XXXVII.	Positive Carbon P.D. plus Vapour P.D. (Solid Carbons	
	11/9)	233
XXXVIII.	Negative Carbon P.D. plus Vapour P.D. (Solid Carbons	
		234
XXXIX.	Comparison, with Solid and Cored Carbons, of P.D. between	075
37.7	Carbons with Third Carbon in Arc	235
XL.	Comparison, with Solid and Cored Carbons, of Positive	074
VII	Carbon P.Ds	236
ALI.		237
VI.II	Conditions to obtain Maximum Power-Efficiency with	201
20111.	E.M.F., P.D., Current, Length, and Series Resistance	
	fixed, in Turn (Solid Carbons 11/9)	270
XLIII.	P.D. between Carbons at Hissing Points (Solid Carbons	
		283
XLIV.	11/9)	283
XLV.	Comparison of Calculated and Observed Values of P.Ds.	
	at Hissing Points (Solid Carbons 11/9)	
XLVI	Total P.Ds. and Positive Carbon P.Ds. at Hissing Points,	
	and with Hissing Arcs (Solid Carbons 11/9)	287
XLVII.	Diminution of Total and of Positive Carbon P.Ds. Accom-	
	panying Hissing (Solid Carbons 11/9)	287