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978-1-108-05028-9 - A Treatise on Analytical Statics: With Numerous Examples: Volume 1

Edward John Routh

Table of Contents

[More information](#)

## CONTENTS.

## CHAPTER I.

## THE PARALLELOGRAM OF FORCES.

ARTS.		PAGES
1—12.	Elementary considerations on forces, &c. . . . .	1—7
13—18.	Dynamical and statical laws . . . . .	7—11
19—21.	Rigid bodies . . . . .	12
22—23.	Resultant forces . . . . .	13
24—30.	Parallelogram of forces . . . . .	14—17
31.	Historical summary . . . . .	17—18

## CHAPTER II.

## FORCES ACTING AT A POINT.

32—40.	Geometrical Method. Triangle, Polygon and Parallelepiped of forces. Three methods of resolution . . . . .	19—23
41—46.	Method of analysis. Resultant of any number of forces . . . . .	23—26
47.	Forces which act normally to the faces of a polyhedron . . . . .	26
48—49.	Theorems on Determinants . . . . .	26—27
50.	Oblique axes . . . . .	27
51—53.	The mean centre. Its use in resolving and compounding forces . . . . .	27—31
54—61.	Equilibrium of a particle. Smooth curves and surfaces . . . . .	31—34
62—69.	The principle of Work . . . . .	34—38
70—74.	Astatic equilibrium. The astatic triangle of forces . . . . .	38—40
75—77.	Stable and unstable equilibrium. A free body under two and three forces . . . . .	40—42

## CHAPTER III.

## PARALLEL FORCES.

ARTS.		PAGES
78—81.	Resultant of two and any number of parallel forces . . . . .	43—45
82—84.	The centre of parallel forces . . . . .	45—46
85—86.	Conditions of equilibrium . . . . .	46—48
87.	A body suspended from a fixed point . . . . .	48—50
88.	A body resting on a plane . . . . .	50—51
89—103.	Theory of couples . . . . .	51—60

## CHAPTER IV.

## FORCES IN TWO DIMENSIONS.

104—108.	Resultant of any number of forces . . . . .	61—63
109—115.	Conditions of equilibrium . . . . .	63—65
116—117.	Varignon's theorem . . . . .	65—66
118—120.	The single resultant force or couple . . . . .	66—68
121—129.	The solution of problems. Constrained rods, discs, spheres, &c. See also note at page 376. . . . .	68—77
130.	Equilibrium of four repelling or attracting particles . . . . .	77
131—133.	Reactions at joints. Theorems of Euler, Fuss &c. A note on a property of triangles . . . . .	77—84
134—140.	Polygon of heavy rods. Funicular polygon. See also Arts. 356—357. . . . .	84—87
141.	Examples . . . . .	87—89
142—147.	Reactions at rigid connections. Bending moment. Beam with weights, diagram of stress. Various examples . . . . .	89—94
148—149.	Indeterminate problems . . . . .	94—97
150—152.	Frameworks. Conditions of stiffness . . . . .	97—99
153.	Equations of equilibrium of a body or framework derived from those of a single particle. See foot-note . . . . .	99
154—155.	Sufficiency of the equations to find the reactions when the frame is just stiff. Exceptional cases. See also Arts. 235, 236. Supplementary equations when the frame is over stiff . . . . .	99—101
156—163.	Astatics. Astatic resultant. Centre of forces, &c. . . . .	101—104

## CHAPTER V.

## ON FRICTION.

164—171.	Laws of friction. The friction force and friction couple. The angle of friction and limiting friction . . . . .	105—110
172—175.	Particle constrained by a rough curve, surface, &c. The cone of friction . . . . .	110—112

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978-1-108-05028-9 - A Treatise on Analytical Statics: With Numerous Examples: Volume 1

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Table of Contents

[More information](#)

## CONTENTS.

ix

ARTS.	PAGES
176—178. Problems on friction when the direction is known. Different methods of solution. Various examples . . . . .	112—120
179. Wheel and axle with friction . . . . .	120—122
180—187. Friction in unknown directions. Two methods . . . . .	122—127
188—190. Examples. Rotation of bodies on a finite and an infinite number of supports. String of particles, &c. . . . .	127—134

## CHAPTER VI.

## THE PRINCIPLE OF WORK.

191—195. Proof of the principle . . . . .	135—138
196. The forces which do not appear in the equation of work . . . . .	138—140
197. Work of a bent string See also Art. 493. . . . .	140—142
198. Infinite forces . . . . .	142
199. Converse of the principle of work . . . . .	142—143
200—201. Initial motion . . . . .	143
202—204. Equations of equilibrium derived from work . . . . .	143—146
205. Examples on the principle . . . . .	146—148
206—213. The work function . . . . .	148—152
214—225. Stable and unstable equilibrium. Analytical method . . . . .	153—159
226—228. Attracting or repelling atoms . . . . .	159—161
229—234. Determination of stress in a simply stiff frame. Examples . . . . .	161—168
235—236. Abnormal deformations . . . . .	168—169
237—238. Indeterminate tensions. Theorems of Crofton and Lévy. See also Art. 368. . . . .	169—170
239—243. Geometrical method of determining the stability of a body. The circle of stability . . . . .	170—174
244—2. 6. Rocking stones, Examples . . . . .	175—177
247—254. Rocking stones, spherical and not spherical to a second approximation in two and three dimensions . . . . .	177—182
255—256. Lagrange's proof of the principle of virtual work . . . . .	182—183

## CHAPTER VII.

## FORCES IN THREE DIMENSIONS.

257—259. Resultants of a system of forces. Conditions of equilibrium. See also Art. 331. . . . .	184—186
260—262. Components of a force . . . . .	186—187
263—267. Moment of a force . . . . .	188—190
268—269. Problems on equilibrium. Pressures on an axis, rods, spheres, rod on wall, curtain ring, &c. . . . .	190—194
270. Poinso't's central axis . . . . .	194—195
271—278. The equivalent wrench. Analytical method . . . . .	195—199
279—283. The Invariants . . . . .	199—201

ARTS.	PAGES
284—286. Equivalent wrench of two wrenches or forces . . . . .	202—203
287—291. The Cylindroid . . . . .	203—205
292—293. Work of a wrench . . . . .	205—207
294—297. Reciprocal screws . . . . .	207—208
298—302. The Nul plane . . . . .	208—209
303—314. Conjugate forces . . . . .	209—214
315. Theorems on three forces . . . . .	214
316—319. Four forces. The hyperboloid. Forces acting normally to the faces of a tetrahedron. Forces normal to a surface	214—218
320—323. Five forces. The two directors . . . . .	218—220
324—330. Six Forces, <i>analytical view</i> . The polar plane. Lines in involution and the two determinants. Resolution of a force along six arbitrary lines . . . . .	220—224
331—333. The sufficiency of the general conditions of equilibrium . . . . .	224—225
334—338. Six Forces, <i>geometrical view</i> . The transversals. Theorems on the fifth and sixth force . . . . .	225—227
339. Tetrahedral coordinates . . . . .	227—228

## CHAPTER VIII.

## GRAPHICAL STATICS.

340. <i>Analytical view</i> . Reciprocal figures . . . . .	229—230
341—342. Theorems of Maxwell and Cremona . . . . .	230—231
343—345. Example of Maxwell's theorem . . . . .	231—232
346—348. Mechanical property of reciprocal figures. Figures which have no reciprocals . . . . .	232—233
349—350. Methods of lettering and drawing reciprocal figures . . . . .	233—234
351. Euler's theorems . . . . .	235
352—355. <i>Statical view</i> . Construction of the resultant force. Con- ditions of equilibrium . . . . .	236—239
356. Parallel forces. Funicular polygon. See also Arts. 134—140 . . . . .	239
357—360. Various graphical constructions . . . . .	239—241
361—362. Graphical construction of stress problems . . . . .	241—242
363—365. Frameworks . . . . .	243—245
366—367. Method of sections . . . . .	245—246
368. Indeterminate tensions. See Arts. 237, 238. . . . .	246—247
369—371. Line of pressure. Theorems . . . . .	247—249
372. Examples . . . . .	249—250

## CHAPTER IX.

## CENTRE OF GRAVITY.

373—379. Definitions and fundamental equations . . . . .	251—253
380—382. Working rule. Examples . . . . .	254—255
383—386. Area and perimeter of a triangle . . . . .	255—257
387—388. Quadrilateral and pentagonal areas . . . . .	257—259

## CONTENTS.

xi

ARTS.	PAGES
389—395. Tetrahedron. Volume, faces, and edges. Pyramid, cone and double tetrahedra. Isosceles tetrahedron . . . . .	259—263
396—399. Centres of gravity of arcs. Circle, catenary, cycloid, &c. . . . .	263—264
400—402. Centres of gravity of circular areas . . . . .	264—265
403—408. Geometrical and analytical projection of areas . . . . .	265—268
409—412. Centre of gravity of any area . . . . .	268—271
413—417. Theorems of Pappus . . . . .	271—274
418—419. Areas on the surface of a right cone . . . . .	274—276
420—424. Areas on a sphere. Theory of maps . . . . .	276—279
425—427. Surfaces and solids of revolution. Moments and products of inertia . . . . .	279—281
428—430. Ellipsoidal volumes and shells . . . . .	281—283
431—432. Any surfaces and volumes . . . . .	283—285
433—434. Heterogeneous bodies. Octant of ellipsoid. Triangular area, &c. . . . .	285—287
435—438. Lagrange's two theorems . . . . .	287—289
439—441. Applications to pure geometry . . . . .	289—291

## CHAPTER X.

## ON STRINGS.

442—445. Catenary. Equations and properties . . . . .	292—295
446—448. Problems on free and constrained catenaries . . . . .	295—301
449. Stability of catenaries . . . . .	302
450—453. Heterogeneous chains. Cycloid, parabola, and the catenary of equal strength . . . . .	302—306
454. String under any forces. General intrinsic equations . . . . .	306—307
455—456. General Cartesian equations . . . . .	308—309
457—458. Constrained strings. Light string on a smooth curve. Problem of Bernoulli . . . . .	309—310
459—462. Heavy string on a smooth curve. The anti-centre and statical directrix. Examples . . . . .	310—314
463—466. Light string on a rough curve. Rough pegs . . . . .	315—317
467—471. Heavy string on a rough curve . . . . .	317—320
472—473. Endless strings. Strings which just fit a curve . . . . .	321—323
474—477. Central forces. Various laws of force. Kinetic analogy. Two centres . . . . .	323—328
478—480. String on a smooth surface. Cartesian and Intrinsic equations. Various theorems. Case of no forces . . . . .	328—331
481. String on a surface of revolution . . . . .	331—332
482. Spherical catenary . . . . .	332—333
483. String on a cylinder . . . . .	333—335
484. String on a right cone . . . . .	335—332
485—486. String on a rough surface . . . . .	335—337
487. Minimum force to move a heavy circular string on a rough plane, and other problems . . . . .	337—338

Cambridge University Press

978-1-108-05028-9 - A Treatise on Analytical Statics: With Numerous Examples: Volume 1

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Table of Contents

[More information](#)

xii

## CONTENTS.

ARTS.		PAGES
488.	Calculus of variations . . . . .	338—339
489—491.	Elastic string. Hooke's law . . . . .	339—340
492.	Heavy elastic string suspended by one end . . . . .	341—342
493.	Work of an elastic string . . . . .	342—343
494.	Heavy elastic string on a smooth curve. The statical directrix . . . . .	343—344
495.	Light elastic string on a rough curve. Rough pegs . . . . .	344—345
496—499.	Elastic string under any forces . . . . .	345—346
500—501.	Elastic catenary . . . . .	346—347

## CHAPTER XI.

## THE MACHINES.

502—505.	Mechanical advantage. Efficiency . . . . .	348—349
506—516.	The Lever. Conditions of equilibrium. Pressure on axis. Various kinds of Levers. For lever under any forces see Art. 268; rough axis Art. 179. . . . .	349—353
517.	Roberval's balance . . . . .	353—354
518—520.	The common balance . . . . .	354—355
521—524.	The common and Danish Steelyard . . . . .	356—358
525—528.	The single pulley . . . . .	358—359
529—530.	The system of pulleys with one rope . . . . .	359—361
531.	Rigidity of cords . . . . .	361
532—536.	Systems of pulleys with several ropes . . . . .	361—365
537—539.	The inclined plane . . . . .	366—368
540—543.	The wheel and axle. The differential axle . . . . .	368—369
544—546.	Toothed wheels . . . . .	369—371
547—549.	The wedge . . . . .	371—373
550—553.	The screw . . . . .	373—375
	NOTE ON TWO THEOREMS IN CONICS ASSUMED IN ARTS. 126, 127 . . . . .	376—378

## CONTENTS OF VOLUME II.

ATTRACTIONS.

THE BENDING OF RODS.

ASTATICS.