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978-1-108-00531-9 - Statics: Including Hydrostatics and the Elements of the Theory of Elasticity

Horace Lamb

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