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THE COLLECTED

MATHEMATICAL PAPERS

OF

ARTHUR CAYLEY, Sc.D., F.R.S.,

LATE SADLERIAN PROFESSOR OF PURE MATHEMATICS IN THE UNIVERSITY OF CAMBRIDGE.

VOL. IX.

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THE present volume contains 74 papers, numbered 556 to 629, published for the most part in the years 1874 to 1877.

The Table for the nine volumes is

Vol. I.	Numbers	1	to	100,
„ II.	„	101	„	158,
„ III.	„	159	„	222,
„ IV.	„	223	„	299,
„ V.	„	300	„	383,
„ VI.	„	384	„	416,
„ VII.	„	417	„	485,
„ VIII.	„	486	„	555,
„ IX.	„	556	„	629.

A. R. FORSYTH.

17 *December* 1895.

CONTENTS.

	PAGE
556. <i>On Steiner's surface</i>	1
Proc. Lond. Math. Society, t. v. (1873—1874), pp. 14—25	
557. <i>On certain constructions for bicircular quartics</i>	13
Proc. Lond. Math. Society, t. v. (1873—1874), pp. 29—31	
558. <i>A geometrical interpretation of the equations obtained by equating to zero the resultant and the discriminants of two binary quartics</i>	16
Proc. Lond. Math. Society, t. v. (1873—1874), pp. 31—33	
559. [<i>Note on inversion</i>]	18
Proc. Lond. Math. Society, t. v. (1873—1874), p. 112	
560. [<i>Addition to Lord Rayleigh's paper "On the numerical calculation of the roots of fluctuating functions"</i>]	19
Proc. Lond. Math. Society, t. v. (1873—1874), pp. 123, 124	
561. <i>On the geometrical representation of Cauchy's theorems of root-limitation</i>	21
Camb. Phil. Trans., t. XII. Part II. (1877), pp. 395—413	
562. <i>On a theorem in maxima and minima: addition [to Mr Walton's paper] by Professor Cayley</i>	40
Quart. Math. Jour., t. x. (1870), pp. 262, 263	
563. <i>Note on the transformation of two simultaneous equations</i>	42
Quart. Math. Jour., t. XI. (1871), pp. 266, 267	
564. <i>On a theorem in elimination</i>	43
Quart. Math. Jour., t. XII. (1873), pp. 5, 6	

	PAGE
565. <i>Note on the Cartesian</i>	45
Quart. Math. Jour., t. XII. (1873), pp. 16—19	
566. <i>On the transformation of the equation of a surface to a set of chief axes</i>	48
Quart. Math. Jour., t. XII. (1873), pp. 34—38	
567. <i>On an identical equation connected with the theory of invariants</i>	52
Quart. Math. Jour., t. XII. (1873), pp. 115—118	
568. <i>Note on the integrals $\int_0^\infty \cos x^2 dx$ and $\int_0^\infty \sin x^2 dx$</i>	56
Quart. Math. Jour., t. XII. (1873), pp. 118—126	
569. <i>On the cycloide</i>	64
Quart. Math. Jour., t. XII. (1873), pp. 148—165	
570. <i>On the superlines of a quadric surface in five-dimensional space</i>	79
Quart. Math. Jour., t. XII. (1873), pp. 176—180	
571. <i>A demonstration of Dupin's theorem</i>	84
Quart. Math. Jour., t. XII. (1873), pp. 185—191	
572. <i>Theorem in regard to the Hessian of a quaternary function</i>	90
Quart. Math. Jour., t. XII. (1873), pp. 193—197	
573. <i>Note on the (2, 2) correspondence of two variables</i>	94
Quart. Math. Jour., t. XII. (1873), pp. 197, 198	
574. <i>On Wronski's theorem</i>	96
Quart. Math. Jour., t. XII. (1873), pp. 221—228	
575. <i>On a special quartic transformation of an elliptic function</i>	103
Quart. Math. Jour., t. XII. (1873), pp. 266—269	
576. <i>Addition to Mr Walton's paper "On the ray-planes in biaxal crystals"</i>	107
Quart. Math. Jour., t. XII. (1873), pp. 273—275	
577. <i>Note in illustration of certain general theorems obtained by Dr Lipschitz</i>	110
Quart. Math. Jour., t. XII. (1873), pp. 346—349	

CONTENTS.

ix

	PAGE
578. <i>A memoir on the transformation of elliptic functions</i>	113
Phil. Trans., t. CLXIV. (for 1874), pp. 397—456	
579. <i>Address delivered by the President, Professor Cayley, on presenting the Gold Medal of the [Royal Astronomical] Society to Professor Simon Newcomb</i>	176
Monthly Notices R. Ast. Society, t. xxxiv. (1873—1874), pp. 224—233	
580. <i>On the number of distinct terms in a symmetrical or partially symmetrical determinant; with an addition</i>	185
Monthly Notices R. Ast. Society, t. xxxiv. (1873—1874), pp. 303—307; p. 335	
581. <i>On a theorem in elliptic motion</i>	191
Monthly Notices R. Ast. Society, t. xxxv. (1874—1875), pp. 337—339	
582. <i>Note on the Theory of Precession and Nutation</i>	194
Monthly Notices R. Ast. Society, t. xxxv. (1874—1875), pp. 340—343	
583. <i>On spheroidal trigonometry</i>	197
Monthly Notices R. Ast. Society, t. xxxvii. (1876—1877), p. 92	
584. <i>Addition to Prof. R. S. Ball's paper "Note on a transformation of Lagrange's equations of motion in generalised coordinates, which is convenient in Physical Astronomy"</i>	198
Monthly Notices R. Ast. Society, t. xxxvii. (1876—1877), pp. 269—271	
585. <i>A new theorem on the equilibrium of four forces acting on a solid body</i>	201
Phil. Mag., t. xxxi. (1866), pp. 78, 79; Camb. Phil. Soc. Proc., t. i. (1866), p. 235	
586. <i>On the mathematical theory of isomers</i>	202
Phil. Mag., t. XLVII. (1874), pp. 444—467	
587. <i>A Smith's Prize dissertation [1873]</i>	205
Messenger of Mathematics, t. III. (1874), pp. 1—4	
588. <i>Problem [on tetrahedra]</i>	209
Messenger of Mathematics, t. III. (1874), pp. 50—52	

C. IX.

b

	PAGE
589. <i>On residuation in regard to a cubic curve</i>	211
Messenger of Mathematics, t. III. (1874), pp. 62—65	
590. <i>Addition to Prof. Hall's paper "On the motion of a particle toward an attracting centre at which the force is infinite"</i>	215
Messenger of Mathematics, t. III. (1874), pp. 149—152	
591. <i>A Smith's Prize paper and dissertation [1874]; solutions and remarks</i>	218
Messenger of Mathematics, t. III. (1874), pp. 165—183; t. IV. (1875), pp. 6—8	
592. <i>On the Mercator's projection of a skew hyperboloid of revolution</i>	237
Messenger of Mathematics, t. IV. (1875), pp. 17—20	
593. <i>A Sheepshanks' problem (1866)</i>	241
Messenger of Mathematics, t. IV. (1875), pp. 34—36	
594. <i>On a differential equation in the theory of elliptic functions</i>	244
Messenger of Mathematics, t. IV. (1875), pp. 69, 70	
595. <i>On a Senate-House problem</i>	246
Messenger of Mathematics, t. IV. (1875), pp. 75—78	
596. <i>Note on a theorem of Jacobi's for the transformation of a double integral</i>	250
Messenger of Mathematics, t. IV. (1875), pp. 92—94	
597. <i>On a differential equation in the theory of elliptic functions</i>	253
Messenger of Mathematics, t. IV. (1875), pp. 110—113	
598. <i>Note on a process of integration</i>	257
Messenger of Mathematics, t. IV. (1875), pp. 149, 150	
599. <i>A Smith's Prize dissertation</i>	259
Messenger of Mathematics, t. IV. (1875), pp. 157—160	
600. <i>Theorem on the n-th Roots of Unity</i>	263
Messenger of Mathematics, t. IV. (1875), p. 171	
601. <i>Note on the Cassinian</i>	264
Messenger of Mathematics, t. IV. (1875), pp. 187, 188	

CONTENTS.

xi

	PAGE
602. <i>On the potentials of polygons and polyhedra</i>	266
Proc. Lond. Math. Society, t. vi. (1874—1875), pp. 20—34	
603. <i>On the potential of the ellipse and the circle</i>	281
Proc. Lond. Math. Society, t. vi. (1874—1875), pp. 38—58	
604. <i>Determination of the attraction of an ellipsoidal shell on an exterior point</i>	302
Proc. Lond. Math. Society, t. vi. (1874—1875), pp. 58—67	
605. <i>Note on a point in the theory of attraction</i>	312
Proc. Lond. Math. Society, t. vi. (1874—1875), pp. 79—81	
606. <i>On the expression of the coordinates of a point of a quartic curve as functions of a parameter</i>	315
Proc. Lond. Math. Society, t. vi. (1874—1875), pp. 81—83	
607. <i>A memoir on prepotentials</i>	318
Phil. Trans., t. CLXV. (for 1875), pp. 675—774	
608. [<i>Extract from a</i>] <i>Report on Mathematical Tables</i>	424
Brit. Assoc. Report, 1873, pp. 3, 4	
609. <i>On the analytical forms called factions</i>	426
Brit. Assoc. Report, 1875, Notices of Communications to the Sections, p. 10	
610. <i>On the analytical forms called Trees, with application to the theory of chemical combinations</i>	427
Brit. Assoc. Report, 1875, pp. 257—305	
611. <i>Report on mathematical tables</i>	461
Brit. Assoc. Report, 1875, pp. 305—336	
612. <i>Note sur une formule d'intégration indéfinie</i>	500
Comptes Rendus, t. LXXVIII. (1874), pp. 1624—1629	
613. <i>On the group of points G_4^1 on a sextic curve with five double points</i>	504
Math. Ann., t. VIII. (1875), pp. 359—362	
614. <i>On a problem of projection</i>	508
Quart. Math. Jour., t. XIII. (1875), pp. 19—29	

b 2

	PAGE
615. <i>On the conic torus</i>	519
Quart. Math. Jour., t. XIII. (1875), pp. 127—129	
616. <i>A geometrical illustration of the cubic transformation in elliptic functions</i>	522
Quart. Math. Jour., t. XIII. (1875), pp. 211—216	
617. <i>On the scalene transformation of a plane curve</i>	527
Quart. Math. Jour., t. XIII. (1875), pp. 321—328	
618. <i>On the mechanical description of a Cartesian</i>	535
Quart. Math. Jour., t. XIII. (1875), pp. 328—330	
619. <i>On an algebraical operation</i>	537
Quart. Math. Jour., t. XIII. (1875), pp. 369—375	
620. <i>Correction of two numerical errors in Sohnke's paper respecting modular equations</i>	543
Crelle, t. LXXXI. (1876), p. 229	
621. <i>On the number of the univalent radicals $C_n H_{2n+1}$</i>	544
Phil. Mag., Ser. 5, t. III. (1877), pp. 34, 35	
622. <i>On a system of equations connected with Malfatti's problem</i>	546
Proc. Lond. Math. Society, t. VII. (1876), pp. 38—42	
623. <i>On three-bar motion</i>	551
Proc. Lond. Math. Society, t. VII. (1876), pp. 136—166	
624. <i>On the bicursal sextic</i>	581
Proc. Lond. Math. Society, t. VII. (1876), pp. 166—172	
625. <i>On the condition for the existence of a surface cutting at right angles a given set of lines</i>	587
Proc. Lond. Math. Society, t. VIII. (1877), pp. 53—57	
626. <i>On the general differential equation $\frac{dx}{\sqrt{X}} + \frac{dy}{\sqrt{Y}} = 0$, where X, Y are the same quartic functions of x, y respectively</i>	592
Proc. Lond. Math. Society, t. VIII. (1877), pp. 184—199	

CONTENTS.

xiii

	PAGE
627. <i>Geometrical illustration of a theorem relating to an irrational function of an imaginary variable.</i>	609
Proc. Lond. Math. Society, t. VIII. (1877), pp. 212—214	
628. <i>On the circular relation of Möbius</i>	612
Proc. Lond. Math. Society, t. VIII. (1877), pp. 220—225	
629. <i>On the linear transformation of the integral $\int \frac{du}{\sqrt{U}}$</i>	618
Proc. Lond. Math. Society, t. VIII. (1877), pp. 226—229	

Plate *to face p. 460*

CLASSIFICATION.

GEOMETRY :

- Möbius' circular relation, 628
- Malfatti's problem, 622
- Inversion, 559
- Projections, 592, 614
- Mechanical construction of curves, 557, 618
- Quartic curve and functions of a single parameter, 606
- Cartesian, 565
- Cassinian, 601
- Sextic curves, 613, 624
- Correspondence, residuation and transformation, 566, 573, 589, 617
- Conformal representation, 627
- Illustrations of algebraical theorems, 558, 561
- Three-bar motion, 623
- Spheroidal Trigonometry, 583
- Dupin's theorem, 571
- Cyclide, 569
- Steiner's surface, 556
- Surface orthogonal to set of lines, 625
- Conic torus, 615
- Quadrics in hyperdimensional space, 570

ASTRONOMY and DYNAMICS :

- Presidential address, 579
- Elliptic motion, 581
- Precession and nutation, 582
- General equations of dynamics, 577, 584, 590
- Potentials, attractions and prepotentials, 602, 603, 604, 605, 607

ANALYSIS :

- Determinant, number of terms in, 580
- Elimination, 564
- Invariants and covariants, 567, 572, 619
- Mathematical tables, 608, 611
- Trees, and their applications to chemistry, 586, 610, 621
- Roots of Unity, 600
- Transformation of equations, 563
- Maxima and minima, 562
- Factions, 609
- Fluctuating functions, 560
- Wronski's theorem of expansion, 574
- Integration and definite integrals, 568, 596, 598, 612
- Elliptic functions, 626, 629
- Transformation of elliptic functions, 575, 578, 594, 597, 616, 620
- Smith's Prize Dissertations and Solutions, 587, 591, 599
- Miscellaneous, 576, 585, 588, 593, 595