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978-1-108-00314-8 - Dynamics: A Text-Book for the Use of the Higher Divisions in  
Schools and for First Year Students at the Universities

Arthur Stanley Ramsey

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