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978-1-108-00259-2 - Electricity and Magnetism: An Introduction to the Mathematical Theory

Arthur Stanley Ramsey

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