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James Joseph Sylvester

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THE COLLECTED
MATHEMATICAL PAPERS

OF

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VOLUME II

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PREFATORY NOTE.

AMONG the Papers contained in this Volume are, the Author's Lecture on Geometry, delivered before the Gresham Committee (No. 2), the Author's seven lectures on the Partition of Numbers, in outline (No. 26), the long memoir on Newton's Rule (No. 74), and the Presidential Address to the Mathematical and Physical Section of the British Association at Exeter (No. 100). The papers here numbered 87, 88, 89 and 94 were republished together with the title "Nugae Mathematicae," and are found in the British Museum Catalogue under that name.

As in the first Volume, save for obvious errors of algebraical formulae, the papers are reprinted unaltered, cross references, and—in a few cases—indications of correction, being enclosed in square brackets.

A Table of Contents is prefixed, a General Index being deferred to the last Volume.

H. F. BAKER.

ST JOHN'S COLLEGE, CAMBRIDGE.

2 *March* 1908.

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