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978-1-107-65649-9 - Lévy Processes and Infinitely Divisible Distributions: Revised Edition

Ken-Iti Sato

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