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## Surveys in Combinatorics 2013

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## Preface

The Twenty-Fourth British Combinatorial Conference was organised by Royal Holloway, University of London. It was held in Egham, Surrey in July 2013. The British Combinatorial Committee had invited nine distinguished combinatorialists to give survey lectures in areas of their expertise, and this volume contains the survey articles on which these lectures were based.

In compiling this volume we are indebted to the authors for preparing their articles so accurately and professionally, and to the referees for their rapid responses and keen eye for detail. We would also like to thank Roger Astley and Sam Harrison at Cambridge University Press for their advice and assistance.

Finally, without the previous efforts of editors of earlier *Surveys* and the guidance of the British Combinatorial Committee, the preparation of this volume would have been daunting: we would like to express our thanks for their support.

Simon R. Blackburn, Stefanie Gerke and Mark Wildon

Royal Holloway, University of London

January 2013