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978-1-107-64056-6 - Complexity Science: The Warwick Master's Course

Edited by Robin Ball, Vassili Kolokoltsov and Robert S. Mackay

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