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978-1-107-52900-7 - Geometry, Topology, and Dynamics in Negative Curvature

Edited by C. S. Aravinda, F. T. Farrell and J.- F. Lafont

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