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978-1-107-49396-4 - The Rational Quartic Curve: In Space of Three and
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H. G. Telling

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by

H. G. TELLING

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CONTENTS

<i>Preface</i>	<i>page</i> vii
<i>Bibliography</i>	viii

CHAPTER I

RATIONAL QUARTIC CURVE C IN [4]

1.1. Linear transformations	1
2.1. Definition of C	2
2.2. Osculating system of reference	4
2.3. Projective generation of C	5
2.4. Fundamental polarity	8
2.5. Trisecant planes	9
2.6. Chords	10
3.1. Invariants and covariants	11
3.2. Symbolic notation	15
3.3. Quadrics with apolar curve C	17
3.4. Cubic primal with apolar curve C	17
3.5. Extension to normal curves of higher order	18
4.1. Quadratic involutions on C : director lines and planes	19
4.2. The g -lines	20
5.1. The chordal J	23
6.1. Quartic surface K	25
6.2. Equations of K	27
6.3. The system of Segre cubic primals	29
6.4. Configuration of nodes on K	30
6.5. Representation of g -lines: the manifold G	32
7.1. Linear complexes containing C	34
7.2. Linear complexes apolar to C	36
7.3. Representation of the lines of [4]	38

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[More information](#)

CHAPTER II

RATIONAL QUARTIC CURVE C_1 IN [3]

8.1. Quartic curves of the first and second kind	41
9.1. Fundamental quartic f	42
9.2. Principal involutions	43
9.3. The flexes	46
9.4. The trisecants and hessian points	46
9.5. Cubic involutions on C_1 : cubic osculants	47
10.1. Osculating planes and the e -polarity	50
11.1. The tangents	51
12.1. Quadratic involutions on C_1	52
13.1. Bitangent planes: the nodal curve and g -polarity	55
14.1. The Steiner surface (k)	57
14.2. The surface of Veronese K^*	59
14.3. Equations of (k) and of its asymptotic curves	61
14.4. Complementary quartic curves on (k)	62
15.1. Particular quartic curves C_1	64
15.2. The equianharmonic curve C_1	65
15.3. The harmonic curve C_1	67
15.4. The quartic curve C_1 with one stationary tangent	69
15.5. The quartic curve C_1 with a cusp	70
15.6. The quartic curve C_1 with two stationary tangents	72

NOTE ON INVOLUTIONS ON C

16.1. Introductory	74
16.2. Quintic involutions	74
16.3. Sextic involutions	76

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P R E F A C E

This essay, first drafted as a Fellowship Essay, was originally much longer. The necessary compression has involved that some of the subsidiary material should be left in the form of exercise or suggestions for the reader, and it is hoped that this arrangement may have the advantage of emphasising the main line of development.

References to the literature are so fully and compactly given in the Encyclopaedia articles, mentioned on p. viii, that it has seemed unnecessary to repeat them here, except in the case of particular points on which a reader may be likely to demand further information.

My thanks are due to Professor Baker without whose constant help and encouragement the essay would never have been written.

To the Press I am indebted for their courtesy; the reader will doubtless join me in appreciation of their elegant handling of the formulae.

H. G. T.

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