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# **Physical Properties**

As a natural science, the variability of river processes must be examined through the measurement of physical parameters. This chapter describes dimensions and units (Section 1.1), physical properties of water (Section 1.2), and sediment (Section 1.3).

## 1.1 Dimensions and Units

Physical properties are usually expressed in terms of the following fundamental dimensions: mass (M), length (L), and time (T). Temperature  $(T^{\circ})$  is also sometimes considered. The fundamental dimension of mass is preferred to the corresponding force.

The fundamental dimensions are measurable in quantifiable units. In the SI system of units, the units for mass, length, time, and temperature are the kilogram (kg), the meter (m), the second (s), and degrees Kelvin (K). The Celsius scale (°C) is commonly preferred in river engineering because it refers to the freezing point of water as 0°C. The abbreviations for cubic meters per second (1 cms = 1 m<sup>3</sup>/s) and cubic feet per second (1 cfs = 1 ft<sup>3</sup>/s) are commonly used to describe the flow discharge of a river.

A Newton (N) is the force required to accelerate 1 kg at 1 m/s<sup>2</sup>, or 1 N = 1 kg m/s<sup>2</sup>. The gravitational acceleration at the Earth's surface is g = 9.81 m/s<sup>2</sup>. The weight of one kilogram is  $F = \text{mass} \times g = 1$  kg  $\times 9.81$  m/s<sup>2</sup> = 9.81 N. The pressure is given in pascals from 1 Pa = 1 N/m<sup>2</sup>. The unit of work (or energy) is the joule (J), which equals the product of 1 N  $\times$  1 m. The unit of power is a watt (W), which is 1 J/s. Prefixes indicate multiples or fractions of units by powers of 10:

$$\begin{split} \mu(\text{micro}) &= 10^{-6}, \qquad k(\text{kilo}) = 10^{3}, \\ m(\text{milli}) &= 10^{-3}, \qquad M(\text{mega}) = 10^{6}, \\ c(\text{centi}) &= 10^{-2}, \qquad G(\text{giga}) = 10^{9}. \end{split}$$

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For example, sand particles are coarser than 62.5  $\mu$ m or microns; gravels are coarser than 2 mm; and 1 megawatt (MW) equals 1 million watts (1,000,000 or 10<sup>6</sup> W).

In the English system of units, the time unit is a second, the fundamental units of length and mass are, respectively, the foot (ft), equal to 30.48 cm, and the slug, equal to 14.59 kg. The force to accelerate a mass of one slug at 1 ft/s<sup>2</sup> is a pound force (lb). In this text, a pound always refers to a force, not a mass. Temperature in degrees Celsius,  $T^{\circ}C$ , is converted to the temperature in degrees Fahrenheit,  $T^{\circ}F$ , by  $T^{\circ}F = 32.2^{\circ}F + 1.8 T^{\circ}C$ .

Variables are classified as geometric, kinematic, dynamic, and dimensionless variables. As shown in Table 1.1, geometric variables describe the geometry in terms of length, area, and volume. Kinematic variables describe the

		Fundamental	
Variable	Symbol	dimensions	SI units
Geometric (L)			
Length	$L, x, h, d_s$	L	m
Area	A	$L^2$	$m^2$
Volume	Α	$L^3$	$m^3$
Kinematic $(L, T)$			
Velocity	$v_x, V, u_*$	$LT^{-1}$	m/s
Acceleration	$a, a_x, g$	$LT^{-2}$	$m/s^2$
Kinematic viscosity	ν	$L^{2}T^{-1}$	$m^2/s$
Unit discharge	q	$L^{2}T^{-1}$	m <sup>2</sup> /s
Discharge	Q	$L^{3}T^{-1}$	m <sup>3</sup> /s
Dynamic $(M, L, T)$			
Mass	т	M	1 kg
Force	F = ma, mg	$MLT^{-2}$	$1 \text{ kg m/s}^2 = 1 \text{ N}$
Pressure	p = F/A	$ML_{1}^{-1}T_{2}^{-2}$	$1 \text{ N/m}^2 = 1 \text{ Pa}$
Shear stress	$ au_{xy},  au_0,  au_c$	$ML_{2}^{-1}T_{2}^{-2}$	$1 \text{ N/m}^2 = 1 \text{ Pa}$
Work or energy	E = Fd	$ML^2T^{-2}$	1  Nm = J
Mass density	$ ho,  ho_s$	$ML^{-3}$	kg/m <sup>°</sup>
Specific weight	$\gamma, \gamma_s = \rho_s g$	$ML^{-2}T^{-2}$	N/m <sup>3</sup>
Dynamic viscosity	$\mu = \rho v$	$ML^{-1}T^{-1}$	1  kg/m s = 1  Pa s
Dimensionless			
Slope	$S_0, S_f$	-	-
Specific gravity	$G = \gamma_s / \gamma$	-	-
Reynolds number	$\text{Re} = Vh/\nu$	-	-
Grain shear			
Reynolds number	$\operatorname{Re}_* = u \cdot d_s / \nu_{o_s}$	-	-
Froude number	$Fr = u/(gh)^{0.5}$	-	-
Shields parameter	$\tau_* = \tau / (\gamma_s - \gamma) d_s$	-	-
Concentration	$C_v, C_w$	_	-

Table 1.1. Geometric, kinematic, dynamic, and dimensionless variables

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#### 1.1 Dimensions and Units

Table 1.2. Unit conversions

TT	1	
Unit	kg, m, s	N, Pa, W
1 acre	$4,047 \text{ m}^2$	
1 acre-foot (acre-ft)	$1,233 \text{ m}^3$	
1 atmosphere (atm)	$101,325 \text{ kg/m s}^2$	101.3 kPa
1 bar	$100,000 \text{ kg/m s}^2$	100 kPa
1 barrel (US, dry) (bbl)	$0.1156 \text{ m}^3$	
1 cubic foot per second $(ft^3/s)$	0.0283 m <sup>3</sup> /s	
$(1 \text{ m}^3/\text{s} = 35.32 \text{ ft}^3/\text{s})$		
1 degree Celsius (°C) = $(T^{\circ}F - 32^{\circ}) 5/9$	1 degree Kelvin (K)	
1 degree Fahrenheit (°F) = $32 + 1.8 T^{\circ}C$	0.5556 degree Kelvin	
1 drop	$61.6 \text{ mm}^3$	
1 dvne (dvn)	$0.00001 \text{ kg m/s}^2$	10 иN
1 dyne per square centimeter $(dyn/cm^2)$	$0.1 \text{ kg/m s}^2$	0.1 Pa
1 fathom (fath)	1 829 m	011 1 4
1 foot (ft)	0 3048 m	
1  gallon (US gal) (1 US gal = 3 785 l)	$0.003785 \text{ m}^3$	
1 horsenower (hn) $- 550$ lb ft/s	$745.7 \text{ kg m}^2/\text{s}^3$	745 7 W
1 inch (in ) (1 ft $-$ 12 in )	0.0254 m	/+3./ //
1 inch of mercury (in Hg)	$3.386 \text{ kg/m s}^2$	3 386 Pa
1 inch of water	$2/18 \ 8 \ kg/m \ s^2$	248 8 Pa
1  kin  (1  kin  -1 000  lb)	$4.448 \text{ kg m/s}^2$	240.01 a 1 118 N
1  kp (1  kp - 1,000  lb)	-4,440  Kg  m/s	4,440 IN
1 liter (1) (1 $m^3 - 1.000$ l)	$0.001 \text{ m}^3$	
$1 \operatorname{micrometer} \operatorname{armicron} (\operatorname{um})$	$1 \times 10^{-6}$ m	
1 mile (neuticel)	1 × 10 III 1 × 2 m	
1 mile (flatfical) 1 mile (statute) (1 mile $-5.280$ ft)	1,652 III 1,600 m	
1 mile (statute) (1 mile = $3,200$ ft) 1 million collors nor day (mod) = $1.55$ ft <sup>3</sup> /c	1,009  m	
1 minion gallons per day (ingd) = $1.55$ it /s	0.04362 III /8	
1 duite (avoirdupois) (oz)	0.02853  kg	
1 null ounce $(US)$	$2.957 \times 10^{-1} \text{ m}^{-1}$	1 NT/2
1 pascal (Pa)	1  kg/m s	I IN/M
1 pint (US pint)	$0.0004/32 \text{ m}^2$	0 1 D
1 poise (P) 1 1 $(11)$ (11) 1 1 $(12)^{2}$	0.1  kg/m s	0.1 Pa s
1 pound-force (lb) (1 lb = 1 slug $\times$ 1 ft/s <sup>-</sup> )	$4.448 \text{ kg m/s}^{-}$	4.448 N
l pound-force per cubic foot (lb/ft <sup>3</sup> )	$15/.1 \text{ kg/m}^2 \text{ s}^2$	15/.1 N/m <sup>3</sup>
l pound-toot (lb-tt)	$1.356 \text{ kg m}^2/\text{s}^2$	1.356 N m
l pound per square foot (lb/ft <sup>2</sup> or pst)	$4/.88 \text{ kg/m s}^2$	47.88 Pa
l pound per square inch (lb/in. <sup>2</sup> or psi)	$6,895 \text{ kg/m s}^2$	6,895 Pa
1 quart (US) (1 qt = 2 pint)	0.0009463 m <sup>3</sup>	
1 slug	14.59 kg	
1 slug per cubic foot (slug/ft <sup>-</sup> )	515.4 kg/m <sup>3</sup>	
$1 \text{ stoke } (S) = 1 \text{ cm}^2/\text{s}$	0.0001 m <sup>2</sup> /s	
1 ton (UK long)	1,016 kg	
1  ton (SI metric)  (1,000  kg = 1  Mg)	1,000 kg	
1  ton (US short) = 2,000  lb	8,900 kg m/s <sup>2</sup>	8.9 kN
1 yard (yd) (1 yd = 3 ft)	0.9144 m	

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Figure 1.1. Newtonian fluid properties

motion of fluids and solids, and are depicted by only two fundamental dimensions: L and T. Dynamic variables always include mass M terms. Force, pressure, shear stress, work, energy, power, mass density, specific weight, and dynamic viscosity are common examples of dynamic variables. Several conversion factors are listed in Table 1.2.

#### 1.2 Water Properties

Rivers carry water to the oceans. The properties of water are sketched in Figure 1.1.

*Mass density of water*  $\rho$ . The mass of water per unit volume defines the mass density  $\rho$ . The maximum mass density of water is 1,000 kg/m<sup>3</sup> at 4°C and decreases slightly with temperature, as shown in Table 1.3. In comparison, the mass density of sea water is approximately 1,025 kg/m<sup>3</sup>, and the mass density of air at sea level is 1.29 kg/m<sup>3</sup> at 0°C. The conversion factor for mass density is 1 slug/ft<sup>3</sup> = 515.4 kg/m<sup>3</sup>. The density of ice is approximately 10 percent less than that of water and it increases as the subzero temperature decreases. For instance, the ice cover on lakes can crack during winter nights and expand in daytime. When the cracks fill up with water at night, very large forces will be applied on the banks of rivers, lakes, and reservoirs.

Specific weight of water  $\gamma$ . The weight per unit volume is the specific weight  $\gamma$ . At 10°C, water has a specific weight,  $\gamma = 9,810 \text{ N/m}^3$  or 62.4 lb/ft<sup>3</sup>

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1.2 Water Properties

Temperature	Density $\rho$	Specific	Dynamic viscosity $\mu$	Kinematic
(°C)	$(kg/m^3)$	weight $\gamma$ (N/m <sup>3</sup> )	(N s/m <sup>2</sup> or kg/m s)	viscosity $\nu$ (m <sup>2</sup> /s)
-30	921	9,035	Ice	Ice
-20	919	9,015	Ice	Ice
-10	918	9,005	Ice	Ice
0	999.9	9,809	$1.79 \times 10^{-3}$	$1.79 \times 10^{-6}$
4	1,000	9,810	$1.56 \times 10^{-3}$	$1.56 \times 10^{-6}$
5	999.9	9,809	$1.51 \times 10^{-3}$	$1.51 \times 10^{-6}$
10	999.7	9,807	$1.31 \times 10^{-3}$	$1.31 \times 10^{-6}$
15	999	9,800	$1.14 \times 10^{-3}$	$1.14 \times 10^{-6}$
20	998	9,790	$1.0 \times 10^{-3}$	$1.0 \times 10^{-6}$
25	997	9,781	$8.91 \times 10^{-4}$	$8.94 \times 10^{-7}$
30	996	9,771	$7.97 \times 10^{-4}$	$8.00 \times 10^{-7}$
35	994	9,751	$7.20 \times 10^{-4}$	$7.25 \times 10^{-7}$
40	992	9,732	$6.53 \times 10^{-4}$	$6.58 \times 10^{-7}$
50	988	9,693	$5.47 \times 10^{-4}$	$5.53 \times 10^{-7}$
60	983	9,643	$4.66 \times 10^{-4}$	$4.74 \times 10^{-7}$
70	978	9,594	$4.04 \times 10^{-4}$	$4.13 \times 10^{-7}$
80	972	9,535	$3.54 \times 10^{-4}$	$3.64 \times 10^{-7}$
90	965	9,467	$3.15 \times 10^{-4}$	$3.26 \times 10^{-7}$
100	958	9,398	$2.82 \times 10^{-4}$	$2.94 \times 10^{-7}$
°F	slug/ft <sup>3</sup>	lb/ft <sup>3</sup>	lb s/ft <sup>2</sup>	ft <sup>2</sup> /s
0	1.7844	57.40	Ice	Ice
10	1.7839	57.34	Ice	Ice
20	1.7816	57.31	Ice	Ice
30	1.7787	57.25	Ice	Ice
32	1.938	62.40	$3.75 \times 10^{-5}$	$1.93 \times 10^{-5}$
40	1.94	62.43	$3.23 \times 10^{-5}$	$1.66 \times 10^{-5}$
50	1.938	62.4	$2.73 \times 10^{-5}$	$1.41 \times 10^{-5}$
60	1.936	62.37	$2.36 \times 10^{-5}$	$1.22 \times 10^{-5}$
70	1.935	62.30	$2.0 \times 10^{-5}$	$1.0 \times 10^{-5}$
80	1.93	62.22	$1.80 \times 10^{-5}$	$0.930 \times 10^{-5}$
100	1.93	62.00	$1.42 \times 10^{-3}$	$0.739 \times 10^{-5}$
120	1.92	61.72	$1.17 \times 10^{-3}$	$0.609 \times 10^{-5}$
140	1.91	61.38	$0.981 \times 10^{-3}$	$0.514 \times 10^{-3}$
160	1.90	61.00	$0.838 \times 10^{-3}$	$0.442 \times 10^{-3}$
180	1.88	60.58	$0.726 \times 10^{-5}$	$0.385 \times 10^{-5}$
200	1.87	60.12	$0.637 \times 10^{-3}$	$0.341 \times 10^{-3}$
212	1.86	59.83	$0.593 \times 10^{-5}$	$0.319 \times 10^{-5}$

Table 1.3. Physical properties of clear water at atmospheric pressure

(1 lb/ft<sup>3</sup> = 157.09 N/m<sup>3</sup>). Specific weight varies with temperature as given in Table 1.3. The specific weight  $\gamma$  equals the product of mass density  $\rho$  and gravitational acceleration g = 32.2 ft/s<sup>2</sup> = 9.81 m/s<sup>2</sup>:

$$\gamma = \rho g. \tag{1.1}$$

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Dynamic viscosity  $\mu$ . As a fluid is brought into low rates of deformation, the velocity of the fluid at any boundary equals the velocity of the boundary. The ensuing rate of fluid deformation causes a shear stress  $\tau_{zx}$  that is proportional to the dynamic viscosity  $\mu$  and the rate of deformation of the fluid,  $dv_x/dz$ :

$$\tau_{zx} = \mu \frac{\mathrm{d}v_x}{\mathrm{d}z}.\tag{1.2}$$

The fundamental dimension of the dynamic viscosity  $\mu$  is M/LT. In Table 1.3, the dynamic viscosity of water decreases with temperature. The dynamic viscosity of clear water at 20°C is 1 centipoise: 1 cP = 0.01 P = 0.001 kg/m s = 0.001 N s/m<sup>2</sup> = 0.001 Pa s. The conversion factor for the dynamic viscosity is 1 lb s/ft<sup>2</sup> = 47.88 N s/m<sup>2</sup> = 47.88 Pa s.

*Kinematic viscosity of water v.* The kinematic viscosity is obtained when the dynamic viscosity of a fluid  $\mu$  is divided by its mass density  $\rho$ . The kinematic viscosity v of water in  $L^2/T$  is shown in Table 1.3 to decrease with temperature. The viscosity of clear water at 20°C is 1 centistokes = 1 cS =  $0.01 \text{ cm}^2/\text{s} = 1 \times 10^{-6} \text{ m}^2/\text{s}$ . The conversion factor is 1 ft<sup>2</sup>/s = 0.0929 m<sup>2</sup>/s. The change in kinematic viscosity of water v with temperature  $T^\circ$  in degrees Celsius can be roughly estimated from

$$v = \frac{\mu}{\rho} = (1 + 0.0337 T_C^\circ + 0.0002217 T_C^{\circ 2})^{-1} \times 1.78 \times 10^{-6} \text{m}^2/\text{s}$$
(1.3)

#### **1.3 Sediment Properties**

Rivers also carry vast amounts of sediment that helps shape their own morphology. The physical properties of sediment are classified into single particles (Section 1.3.1), sediment mixtures (Section 1.3.2), sediment suspensions (Section 1.3.3), and sediment deposits (Section 1.3.4).

#### 1.3.1 Sediment Particles

The physical properties of a single solid particle of volume  $\forall_s$  are sketched in Figure 1.2. The mass density of a solid particle  $\rho_s$  describes the solid mass per volume of solids. The mass density of quartz particles is  $\rho_s = 2,650 \text{ kg/m}^3$  (1 slug/ft<sup>3</sup> = 515.4 kg/m<sup>3</sup>).

Specific weight of sediment  $\gamma_s$ . The particle specific weight  $\gamma_s$  corresponds to the solid weight per unit volume of solid. Typical values of  $\gamma_s$  are 26.0 kN/m<sup>3</sup> or 165.4 lb/ft<sup>3</sup> and the conversion factor is 1 lb/ft<sup>3</sup> = 157.09 N/m<sup>3</sup>. The specific

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Figure 1.2. Physical properties of a single solid particle

weight of a solid  $\gamma_s$  is the product of the mass density of a solid particle  $\rho_s$  and gravitational acceleration g

$$\gamma_s = \rho_s g. \tag{1.4}$$

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Specific gravity of sediment G. The ratio of the specific weight of a solid particle to the specific weight of fluid at a standard reference temperature defines the specific gravity G. With reference to water at 4°C, the specific gravity of quartz particles is G = 2.65

$$G = \frac{\gamma_s}{\gamma} = \frac{\rho_s}{\rho} = 2.65. \tag{1.5}$$

The specific gravity is a dimensionless parameter independent of the system of units.

Submerged specific weight of sediment  $\tilde{\gamma}_s$ . The specific weight of a solid particle  $\gamma_s$  submerged in a fluid of specific weight  $\gamma$  equals the difference

$$\tilde{\gamma}_s = \gamma_s - \gamma = (G - 1)\gamma. \tag{1.6}$$

Sediment size  $d_s$ . The most important physical property of a sediment particle is its size. The first two columns of Table 1.4 show the grade scale commonly used in sedimentation (1 in. = 25.4 mm). The size of sediment particles can be determined in a number of ways described in detail in Julien (2010). Some of the main characteristics associated with particle size are listed in Table 1.4.

## 1.3.2 Sediment Mixtures

The properties of a sediment mixture are sketched in Figure 1.3. The total volume,  $\forall_t$ , is the total of the volume of solids  $\forall_s$  and the volume of voids  $\forall_v$ .

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Table 1.4. Sediment grade scale and approximate properties

Class name	Particle diameter $d_s$ (mm)	Angle of repose $\phi$ (deg)	Critical shear stress $\tau_c$ (N/m <sup>2</sup> )	Critical shear velocity <i>u</i> * <sub>c</sub> (m/s)	Settling velocity $\omega_0$ (mm/s)
<i>Boulder</i> Very large Large Medium Small	>2,048 >1,024 >512 >256	42 42 42 42	1,790 895 447 223	1.33 0.94 0.67 0.47	5,430 3,839 2,715 1,919
<i>Cobble</i> Large Small	>128 >64	42 41	111 53	0.33 0.23	1,357 959
Gravel Very coarse Coarse Medium Fine Very fine	>32 >16 >8 >4 >2	40 38 36 35 33	26 12 5.7 2.71 1.26	0.16 0.11 0.074 0.052 0.036	678 479 338 237 164
Sand Very coarse Coarse Medium Fine Very fine	>1.000 >0.500 >0.250 >0.125 >0.062	32 31 30 30 30	0.47 0.27 0.194 0.145 0.110	0.0216 0.0164 0.0139 0.0120 0.0105	109 66.4 31.3 10.1 2.66
Silt Coarse Medium Fine Very fine	>0.031 >0.016 >0.008 >0.004	30 30	0.083 0.065	0.0091 0.0080	$\begin{array}{c} 0.67 \\ 0.167^{a} \\ 0.042^{a} \\ 0.010^{a} \end{array}$
<i>Clay</i> Coarse Medium Fine Very fine	>0.0020 >0.0010 >0.0005 >0.00024		Cohesive material		$\begin{array}{c} 2.6\times10^{-3a}\\ 6.5\times10^{-4a}\\ 1.63\times10^{-4a}\\ 4.1\times10^{-5a} \end{array}$

<sup>a</sup>Possible flocculation.

Sediment particle-size distribution. The example of particle-size distribution in Figure 1.3 also shows the percentage by weight of material finer than a given sediment size. The median grain diameter is the size  $d_{50}$  for which 50 percent of the material is finer. Likewise  $d_{90}$  and  $d_{10}$  are sediment sizes for which 90 percent and 10 percent of the material are finer.

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Figure 1.3. Particle-size distribution

Gradation coefficients  $\sigma_g$  and Gr. The gradation of the sediment mixture is a measure of the particle-size distribution of a sediment mixture. It can be described as

$$\sigma_g = \left(\frac{d_{84}}{d_{16}}\right)^{1/2} \tag{1.7a}$$

or

$$Gr = \frac{1}{2} \left( \frac{d_{84}}{d_{50}} + \frac{d_{50}}{d_{16}} \right).$$
(1.7b)

Both gradation coefficients reduce to unity for uniform sediment mixtures, i.e. when  $d_{84} = d_{50} = d_{16}$ . The gradation coefficient increases with nonuniformity, and high gradation coefficients describe well-graded mixtures.

Angle of repose  $\phi$ . Typical values of the angle of repose  $\phi$  of granular material are shown in Figure 1.4. The angle of repose varies with grain size and angularity of the material. Typical values of the angle of repose are also given in column three of Table 1.4 for material coarser than medium silt.

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Figure 1.4. Angle of repose of granular material (after Simons, 1957)



Figure 1.5. Properties of a sediment suspension

#### 1.3.3 Sediment Suspensions

The properties of a sediment suspension are sketched in Figure 1.5, with the volume of void  $\forall_v$  completely filled with water  $\forall_w$ , i.e. without air in the mixture.

Sediment concentration. The volumetric sediment concentration  $C_v$  is the ratio of the volume of solids  $\forall_s$  to the total volume  $\forall_t = \forall_s + \forall_w$ .

$$C_{\nu} = \frac{\text{sediment volume}}{\text{total volume}} = \frac{\forall_s}{\forall_s + \forall_w}.$$
 (1.8a)

The sediment concentration is commonly measured in milligrams per liter  $C_{mg/l}$  while other measurements include the concentration by weight  $C_w$  and the concentration in parts per million (ppm). The following conversions from Julien (2010) are

$$C_{w} = \frac{\text{sediment weight}}{\text{total weight}} = \frac{C_{v}G}{1 + (G - 1)C_{v}},$$
(1.8b)

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1.3 Sediment Properties

$C_{v}$	$C_w$	C <sub>ppm</sub>	$C_{\rm mg/l}$	$p_0$	$\gamma_{md}$ lb/ft <sup>3</sup>	$\gamma_{md}$ kN/m <sup>3</sup>
Suspension						
0.0001	0.00026	265	265			
0.001	0.00264	2,645	2,650			
0.0025	0.00659	6,598	6,625			
0.005	0.01314	13,141	13,250			
0.0075	0.01963	19,632	19,875			
0.01	0.02607	26,069	26,500			
0.025	0.06363	63,625	66,250			
<i>Hyperconcentrations</i>						
0.05	0.12240	122,401	132,500	0.95		
0.075	0.17700	176,863	198,750	0.925		
0.1	0.22750	227,467	265,000	0.9	16.5	2.6
0.20	0.39850	398,496	530,000	0.8	33.0	5.2
0.25	0.46900	469,027	662,500	0.75	41.3	6.5
0.30	0.53200	531,772	795,000	0.70	49.6	7.8
0.40	0.63900	638,554	1,060,000	0.60	66.2	10.4
Sediment deposits						
0.5	0.72600	726,027	1,325,000	0.50	82.7	13
0.6	0.79900	798,995	1,590,000	0.40	99.2	15.6
0.7	0.86080	860,788	1,855,000	0.30	116	18.2
0.75	0.88800	888,268	1,987,500	0.25	124	19.5

Table 1.5. Equivalent concentrations for  $C_{\nu}$ ,  $C_{w}$ ,  $C_{ppm}$ ,  $C_{mg/l}$ ,  $p_0$ , and  $\gamma_{md}$ 

*Note*: Calculations based on G = 2.65.

$$C_{\rm ppm} = 10^6 C_w,$$
 (1.8c)

$$C_{\rm mg/l} = {{\rm sediment\ mass}\over {\rm total\ volume}} = \rho G C_{\rm v}.$$
 (1.8d)

Equivalent sediment concentrations are listed in columns one to four of Table 1.5. In practice, there is a negligible difference (<10 percent) between  $C_{\rm ppm}$  and  $C_{\rm mg/l}$  when  $C_{\rm ppm} < 145,000$ .

Specific weight of a mixture  $\gamma_m$ . The specific weight of a submerged mixture is the total weight of solid and water in the voids-per-unit total volume. The specific weight of a mixture  $\gamma_m$  is a function of the volumetric concentration  $C_v$  as

 $\gamma_m = \frac{\text{total weight}}{\text{total volume}} = \gamma_s C_v + \gamma (1 - C_v).$ (1.9)

The specific mass  $\rho_m$  of a submerged mixture is the total mass of solid and water in the voids-per-unit total volume. The specific mass is given by  $\rho_m = \gamma_m/g$ .

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**Physical Properties** 

## 1.3.4 Sediment Deposits

The properties of sediment deposits usually include the porosity  $p_0$  and the dry specific weight  $\gamma_{md}$  of sediment mixtures.

*Porosity*  $p_0$ . The porosity  $p_0$  is the volume of void  $\forall_v$  per total volume  $\forall_t$ .

$$p_0 = \frac{\forall_v}{\forall_t}.\tag{1.10}$$

The values of porosity are listed in column five of Table 1.5.

Dry specific weight of a mixture  $\gamma_{md}$ . The dry specific weight of a mixture is the weight of solid-per-unit total volume, including the volume of solids and voids. The dry specific weight of a mixture  $\gamma_{md}$  is a function of porosity  $p_0$  as

$$\gamma_{md} = \frac{\text{sediment weight}}{\text{total volume}} = \gamma G C_v = \gamma_s (1 - p_0). \tag{1.11}$$

The dry specific weight of sand deposits is approximately ~14.75 kN/m<sup>3</sup> or 93 lb/ft<sup>3</sup>. The dry specific mass of a mixture is the mass of solid-per-unit total volume. The dry specific mass of a mixture is  $\rho_{md} = \gamma_{md}/g$ .

## Problem 1.1

Determine the mass density, specific weight, dynamic viscosity, and kinematic viscosity of clear water at 20°C (a) in SI units and (b) in the English system of units.

[*Answers*: (a)  $\rho = 998 \text{ kg/m}^3$ ,  $\gamma = 9,790 \text{ N/m}^3$ ,  $\mu = 1.0 \times 10^{-3} \text{ N s/m}^2$ ,  $v = 1 \times 10^{-6} \text{ m}^2$ /s, (b)  $\rho = 1.94 \text{ slug/ft}^3$ ,  $\gamma = 62.3 \text{ lb/ft}^3$ ,  $\mu = 2.1 \times 10^{-5} \text{ lb/ft}^2$ ,  $v = 1.1 \times 10^{-5} \text{ ft}^2$ /s]

## ♦Problem 1.2

Determine the sediment size, mass density, specific weight, submerged specific weight, and angle of repose of small quartz cobbles (a) in SI units and (b) in English units.

### **♦**♦*Problem* 1.3

The volumetric sediment concentration of a sample is  $C_v = 0.05$ . Determine the corresponding: (a) concentration by weight  $C_w$ , (b) concentration in parts per million  $C_{\text{ppm}}$ , (c) concentration in milligrams per liter  $C_{\text{mg/l}}$ , (d) porosity  $p_0$ , and (e) void ratio *e*.

[Answers: The answers are found in Table 1.5.]

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# ♦Problem 1.4

The porosity of a sandy loam is 0.45. Determine the corresponding soil properties: (a) volumetric concentration, (b) void ratio e, (c) specific weight  $\gamma_{m}$ , (d) specific mass  $\rho_{m}$ , (e) dry specific weight  $\gamma_{md}$ , and (f) dry specific mass  $\rho_{md}$ .

## ♦Problem 1.5

Calculate the gradation coefficients  $\sigma_g$  and Gr from the particle distribution in Figure 1.3.

[Answer: It is a well-graded sediment mixture  $\sigma_g = 8$ , and Gr = 10.]