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978-1-107-44288-7 - Reversibility in Dynamics and Group Theory: London Mathematical Society

Lecture Note Series: 416

Anthony G. O'Farrell and Ian Short

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