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978-1-107-40419-9 - Solitons: Differential Equations, Symmetries and Infinite Dimensional Algebras

T. Miwa, M. Jimbo and E. Date

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