

Admissible Sets and Structures

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Admissible set theory is a major source of interaction between model theory, recursion theory and set theory, and plays an important role in definability theory. In this volume, the 7th publication in the Perspectives in Logic series, Jon Barwise presents the basic facts about admissible sets and admissible ordinals in a way that makes them accessible to logic students and specialists alike. It fills the artificial gap between model theory and recursion theory and covers everything the logician should know about admissible sets.

JON BARWISE works in the Department of Mathematics at the University of Wisconsin, Madison.



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PERSPECTIVES IN LOGIC

Admissible Sets and Structures

An Approach to Definability Theory

JON BARWISE

University of Wisconsin, Madison







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a and the memory of my father a



> method. At the end of an infinite discussion we found our name, and that of were promoted, savaged and scrapped. Gradually there emerged a form and a we write the books ourselves? How long would it take? Plans for authorless books the group. To begin with all was fluid. How ambitious should we be? Should Hans Hermes gave us encouragement and support. Later Hans Hermes joined in earnest and decided to go ahead with it. Professor F. K. Schmidt and Professor O. Gandy, A. Levy, G. H. Müller, G. Sacks, D. S. Scott) discussed the project Oderwolfach in the spring of 1969. Here the founding members of the group (R. on mathematical logic was first mooted. Various discussions led to a meeting at History of the Q-Group. During 1968 the idea of an integrated series of monographs

> > the series proves of value, the credit will be theirs.

and revisions suggested. But it is the authors who do the work; if, as we hope, for books are discussed and argued about at length. Later, encouragement is given the books in the series are written by individual authors, not by the group. Plans attain a reasonable degree of uniformity of notation and arrangement. However, coverage of the same material from different points of view. We have tried to to fit their book in with other planned volumes, sometimes deliberately seeking Although no book depends on another as prerequisite, we have encouraged authors present a single line of thought. Each book is, at its own level, reasonably self-contained. specialised. They also differ in scope: some offer a wide view of an area, others The books in the series differ in level: some are introductory some highly

esantindos dad techniques.

developing certain themes, it will be of greater interest than a mere assemblage to ensure that each book represents a coherent line of thought; and that, by particular philosophical programme. Nevertheless we have tried by critical discussion a definitive version of the elements of the subject. We are not committed to any shall not aim at encyclopaedic coverage; nor do we wish to prescribe, like Euclid, of the series to provide, as it were, maps or guides to this complex terrain. We mathematics proliferated. The subject is now both rich and varied. It is the aim connections between different lines of research and links with other branches of autonomous. As time passed, and more particularly in the last two decades, interthe modes of its expression. The pioneering investigations were diverse and largely the limits of rational or mathematical thought, and from a desire to systematise On Perspectives. Mathematical logic arose from a concern with the nature and

Preface to the Series



> H. Hermes G. H. Müller D. S. Scott

A. Levy G. Sacks

R. O. Gandy

Oberwolfach September 1975

and our indefatigable secretary Elfriede Ihrig.

those concerned.

Finally we thank the Oberwolfach Institute, which provides just the right atmosphere for our meetings, Drs. Ulrich Felgner and Klaus Gloede for all their help,

Academy; this was made possible by a special grant from the Kultusministerium von Baden-Württemberg (where Regierungsdirektor R. Goll was our counsellor). The success of the negotiations for this was largely due to the enthusiastic support of the former President of the Academy, Professor Wilhelm Doerr. We thank all

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the series. We established our centre in Heidelberg. We agreed to meet twice a year together with authors, consultants and assistants, generally in Oberwolfach. We soon found the value of collaboration: on the one hand the permanence of the founding group gave coherence to the over-all plans; on the other hand the stimulus of new contributors kept the project alive and flexible. Above all, we found how intensive discussion could modify the authors ideas and our own. Often the battle ended with a detailed plan for a better book which the author was keen to write and which would indeed contribute a perspective.

Preface to the Series

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Author's Preface

writing of this book and that may not be completely obvious. back, though, I can see some motives that remained more or less constant in the reason for writing it. In between, reasons are as numerous as the days. Looking It is only before or after a book is written that it makes sense to talk about the

model theory and recursion theory. I wanted to write a book that would fill what I see as an artificial gap between

on Abstract Structures, without assuming material from either. Model Theory for Infinitary Logic and Y. N. Moschovakis' Elementary Induction I wanted to write a companion volume to books by two friends, H. J. Keisler's

logician ought to know about admissible sets. logician knew about admissible sets. It also contains some material that every definability theory in particular. This book contains much of what I wish every have an important role to play in the future of mathematical logic in general and and specialist alike. I am convinced that the tools provided by admissible sets ordinals in a way that would, at long last, make them available to the logic student I wanted to set forth the basic facts about admissible sets and admissible

other residents of Freeland for making our visit in England such a pleasant one. prepare the final manuscript. I would also like to thank Mrs. Nora Day and the version of the manuscript. I owe a lot to Dana Scott for hours spent helping Schlipf, Matt Kaufmann and Azriel Levy for valuable comments on an earlier I would like to thank Martha Kirtley and Judy Brickner for typing and John G. Kreisel, and the support of the Ω -Group during the preparation of this book. the continued interest expressed in these topics over the past years by Professor particularly Professors Feferman, Gandy, Keisler and Scott. I also appreciate three institutions who helped to make it possible for me to write this book, Wisconsin and an SRC Fellowship at Oxford. I wish to thank colleagues at these academic year 1973—74 while I held a research grant from the University of 1973. The book was completed at Heatherton, Freeland, Oxfordshire during the first draft was written at Stanford during the unforgettable winter and spring of students of these courses for their interest, suggestions and corrections. A rough Several courses have grown out of my desire to write this book. I thank the



K'I'B'

Santa Monica

September 19, 1975

Author's Preface

book every eleven years. To Mary Ellen, on this our eleventh anniversary, I promise to write at most one the corrections; but most of all to Mary Ellen for her encouragement and patience. me to use her room as a study during the coal strike; to Jon Russell for help with A final but large measure of thanks goes to my family: to Melanie for allowing

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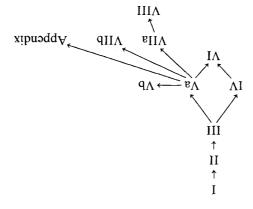
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(Va denotes the first three §§ of Chapter V, similarly for VIIa.)



Major Dependencies