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978-1-107-13743-1 - Convergence of One-Parameter Operator Semigroups: In Models of
Mathematical Biology and Elsewhere

Adam Bobrowski

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