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978-1-107-13657-1 - Random Graphs, Geometry and Asymptotic Structure

Michael Krivelevich, Konstantinos Panagiotou, Mathew Penrose and Colin Mediarimid

Table of Contents

[More information](#)

Contents

| | | |
|----------|---|---------------|
| | Editors' introduction | <i>page</i> 1 |
| 1 | Long paths and Hamiltonicity in random graphs | 4 |
| | <i>Michael Krivelevich</i> | |
| 1 | Introduction | 4 |
| 2 | Tools | 5 |
| | 2.1 Preliminaries | 5 |
| | 2.2 Depth First Search and its applications for finding long paths | 7 |
| | 2.3 Pósa's Lemma and boosters | 10 |
| 3 | Long paths in random graphs | 13 |
| | 3.1 Linearly long paths in the supercritical regime | 13 |
| | 3.2 Nearly spanning paths | 16 |
| 4 | The appearance of Hamilton cycles in random graphs | 17 |
| | <i>References</i> | 27 |
| 2 | Random graphs from restricted classes | 28 |
| | <i>Konstantinos Panagiotou</i> | |
| 1 | Introduction | 28 |
| | 1.1 Preliminaries | 30 |
| 2 | Random trees | 32 |
| | 2.1 Random trees via a sampling algorithm | 33 |
| | 2.2 Coarse estimates | 36 |
| | 2.3 Fine estimates | 39 |
| 3 | Random graphs from block-stable classes | 45 |
| | 3.1 Combinatorial constructions and Boltzmann samplers | 47 |
| | 3.2 Sampling from block-stable graph classes | 51 |
| | 3.3 Asymptotic analysis | 53 |
| | 3.4 The distribution of blocks | 54 |
| | 3.5 Simple vs complex graph classes | 57 |

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Table of Contents

[More information](#)

| | | |
|----------|---|------------|
| vi | <i>Contents</i> | |
| | 3.6 Degree distribution for simple classes | 61 |
| | 3.7 Further directions | 64 |
| | <i>References</i> | 65 |
| 3 | Lectures on random geometric graphs | 67 |
| | <i>Mathew Penrose</i> | |
| 1 | Introduction | 67 |
| 2 | Edge counts | 69 |
| 3 | Edge counts: normal approximation | 73 |
| 4 | The maximum degree | 78 |
| 5 | A sufficient condition for connectivity | 84 |
| 6 | Connectivity and Hamiltonicity | 91 |
| 7 | Solutions to exercises | 94 |
| | <i>References</i> | 101 |
| 4 | On random graphs from a minor-closed class | 102 |
| | <i>Colin McDiarmid</i> | |
| 1 | Introduction | 102 |
| 2 | Properties of graph classes | 103 |
| | 2.1 Minor-closed classes | 103 |
| | 2.2 Decomposable, bridge-addable and addable graph classes | 104 |
| 3 | Bridge-addability, being connected and the fragment | 105 |
| | 3.1 Bridge-addability and being connected | 105 |
| | 3.2 Bridge-addability and the fragment | 106 |
| 4 | Growth constants | 107 |
| | 4.1 When is there a growth constant? | 108 |
| | 4.2 Pendant Appearances Theorem | 109 |
| | 4.3 Some applications of the Pendant Appearances Theorem | 110 |
| 5 | Unlabeled graphs | 111 |
| 6 | Smoothness | 113 |
| | 6.1 Smoothness for surface and addable minor-closed classes | 114 |
| | 6.2 Boltzmann Poisson random graph | 114 |
| | 6.3 The fragment for surface and addable minor-closed classes | 116 |
| | 6.4 Smoothness and unlabeled graphs | 117 |
| 7 | Concluding remarks | 118 |
| | <i>References</i> | 118 |
| | <i>Index</i> | 121 |