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978-1-107-13657-1 - Random Graphs, Geometry and Asymptotic Structure

Michael Krivelevich, Konstantinos Panagiotou, Mathew Penrose and Colin Mediarimid

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Random Graphs, Geometry and Asymptotic Structure

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