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978-1-107-12954-2 - Noncommutative Algebraic Geometry

Gwyn Bellamy, Daniel Rogalski, Travis Schedler, J. Toby Stafford and Michael Wemyss

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