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978-1-107-07189-6 - Encyclopedia of Mathematics and its Applications: Orthogonal Polynomials of Several Variables: Second Edition

Charles F. Dunkl and Yuan Xu

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