

Cambridge University Press

978-1-107-01369-8 - Encyclopedia of Mathematics and its Applications: Finite Ordered Sets: Concepts, Results and Uses

Nathalie Caspard, Bruno Leclerc and Bernard Monjardet

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