

CONTENTS

| | |
|--|----|
| PREFACE | ix |
| CHAPTER 1. ASPECTS OF PARADOX | 1 |
| 1.1. The liar and its variants | 1 |
| 1.2. Propositions and truth-values | 5 |
| 1.2.1. No proposition expressed | 6 |
| 1.2.2. Lack of truth-value | 9 |
| 1.3. The problem in a formal setting | 12 |
| 1.4. Tarski and Kripke | 16 |
| 1.5. The project | 20 |
| CHAPTER 2. AGAINST CLASSICAL LOGIC | 23 |
| 2.1. Different treatments of the paradoxes | 23 |
| 2.2. The first argument against classical logic | 26 |
| 2.3. The second argument against classical logic | 30 |
| 2.4. Variants of the arguments | 37 |
| 2.4.1. No set of truths | 37 |
| 2.4.2. Another paradox? | 38 |
| 2.4.3. Propositions again | 40 |
| 2.4.4. Quantifying into quotation | 41 |
| CHAPTER 3. AMBIGUITY AND INDEXICALITY | 45 |
| 3.1. Ambiguity | 45 |
| 3.1.1. The Tarskian hierarchy again | 45 |
| 3.1.2. Shifts of meaning | 47 |
| 3.2. The contextual approach to the liar | 50 |
| 3.2.1. The three-stage reasoning about sentence-types | 50 |
| 3.2.2. The three-stage reasoning about sentence-tokens | 56 |
| CHAPTER 4. A PROPOSITIONAL THEORY OF TRUTH | 69 |
| 4.1. What kind of logic? | 69 |
| 4.1.1. Avoiding contradiction | 69 |
| 4.1.2. Espousing and abandoning principles | 71 |

| | | |
|---|--|------------|
| 4.1.3. | Avoiding substructuralism | 75 |
| 4.2. | A propositional logic | 79 |
| 4.3. | The theory of truth | 93 |
| 4.4. | Strengthening the logic | 100 |
| CHAPTER 5. PROVING CENTRAL THEOREM 1 | | 107 |
| 5.1. | Preliminaries | 107 |
| 5.1.1. | Appropriate classes..... | 107 |
| 5.1.2. | <i>C</i> -insertable classes..... | 109 |
| 5.1.3. | The rule (Con) | 111 |
| 5.1.4. | Extending a class..... | 112 |
| 5.2. | Two theorems | 113 |
| 5.3. | Proof of Central Theorem 1 | 124 |
| 5.4. | Concluding remarks | 129 |
| CHAPTER 6. TRUTH AND DETERMINACY | | 131 |
| 6.1. | The concept of determinacy | 131 |
| 6.2. | A logic of determinacy | 133 |
| 6.2.1. | More operators..... | 139 |
| 6.3. | A theory of truth with the determinacy operator | 141 |
| 6.4. | Proving Central Theorems 2 and 3 | 146 |
| 6.4.1. | Central Theorem 2 | 146 |
| 6.4.2. | Central Theorem 3 | 148 |
| 6.5. | Trying to explain the failure of classical logic | 162 |
| CHAPTER 7. A FIRST-ORDER LOGIC AND THEORY OF TRUTH | | 173 |
| 7.1. | The logic | 173 |
| 7.1.1. | What kind of first-order logic?..... | 173 |
| 7.1.2. | Adorned wffs, frames and codesignation..... | 175 |
| 7.1.3. | Models _* and models | 179 |
| 7.1.4. | Validities and invalidities..... | 187 |
| 7.2. | A first-order theory of truth | 195 |
| CHAPTER 8. PROVING CENTRAL THEOREM 4 | | 207 |
| 8.1. | A problem..... | 207 |
| 8.2. | Preliminaries | 209 |
| 8.2.1. | <i>C</i> -implying and <i>C</i> -equivalence..... | 209 |
| 8.2.2. | Acceptable adorned conditionals..... | 212 |
| 8.2.3. | The rules (Con) and (Uni) | 217 |
| 8.2.4. | Extensions | 218 |
| 8.3. | Two theorems again | 219 |
| 8.4. | Parallel formulae | 232 |
| 8.5. | Constructing a sequence of models | 237 |
| 8.6. | Reaching Central Theorem 4 | 248 |

CONTENTS

vii

| | |
|---|-----|
| CHAPTER 9. ANOTHER FIRST-ORDER THEORY OF TRUTH | 255 |
| 9.1. Syntax and arithmetic | 255 |
| 9.2. A new language | 259 |
| 9.3. Syntactic definitions | 261 |
| 9.4. The new theory of truth | 279 |
| 9.5. Proving Central Theorem 5 | 285 |
| CHAPTER 10. TRUTH IN DIFFERENT NON-CLASSICAL LOGICS | 295 |
| 10.1. Field saving truth | 295 |
| 10.1.1. Revising Kripke | 295 |
| 10.1.2. Equivalents and non-contradiction | 299 |
| 10.1.3. Other differences from Field | 307 |
| 10.2. Tennant's core logic | 308 |
| 10.3. Zardini's substructuralism | 310 |
| 10.4. And Ripley's substructuralism | 321 |
| AFTERWORD | 327 |
| REFERENCES | 329 |
| INDEX | 337 |