

Index

- Aharonov–Bohm effect, 177
- amplitude squeezing, 212
- angular momentum commutation
 - relations, 179, 181
- annihilation operator, 24
- anti-Jaynes–Cummings model, 331
- antinormally ordered operators, 71
- atom–field interactions
 - classical field, 91–97
 - density operator approach, 119–122
 - dispersive model, 123–125
 - dressed states, 115–119
 - Jaynes–Cummings model, 105–115
 - perturbation theory, 89–91
 - quantized field, 97–102
 - Rabi model, 102–105
- atomic coherent states, 333
- atomic inversion, 104
- autocorrelation function, 137

- B92 protocol, 367–368
- Baker–Campbell–Hausdorff
 - theorem, 46
- Baker–Hausdorff lemma, 14
- balanced homodyne detection,
 - 209–211
- Barnett and Pegg Hermitian phase
 - operator, 42–45, 106
- BB84 protocol, 365–366
- beam-splitter quantum mechanics
 - Bose–Einstein condensation (BEC),
 - 167–168
 - classical, 157
 - classical states of light, 177–179
 - as displacer, 185
 - entanglement generation, 238–239
 - Heisenberg point of view, 157–162
 - photons at input, 168–172
 - Schrödinger point of view, 162–165
 - single photon, 165–166
 - SU(2) formulation, 179–185
 - vacuum and coherent state, 172–173
- beam-splitter transformation, 377
- Bell’s inequalities experiments
 - Franson’s experiment, 301
 - optical test of local realities,
 - 294–301
- Bell’s inequalities violation
 - entanglement, 340
 - nonlocality, 177
- birefringent material, 284, 295
- Bloch equations, 257
- Bloch sphere, 389–391
- Bloch vector, 126–127
- Born–Markov approximation, 258
- Bose–Einstein condensation (BEC),
 - 167–168
- bright and dark periods, 261–262, 268
- broadband squeezed light, 232–233

- Casimir effect, 35–37
- Casimir force, 37
- Cauchy’s inequality, 148, 237
- cavity QED (quantized electromagnetic
 - field)
 - high- Q microwave cavity, 315
 - microwave versus optical, 332
 - Schrödinger-cat states, 320–325
- center-of-mass motion (trapped
 - ion), 114
- chaotic light beams, 149
- characteristic function, 79–82
- circuit QED (quantized
 - electromagnetic field), 333
- classical bit, 6
- classical coherence functions,
 - 134–139
- classical current, 56
- classical first-order coherence
 - functions, 136–139

- classical first-order coherence theory, 135–136
- classical limit, 31
- C-NOT gate, 372
- coherence functions
 - classical, 134–139
 - quantum, 139–143
 - Young’s interference, 143–146
- coherence functions, higher order
 - Hanbury-Brown and Twiss experiment, 146–152
 - intensity–intensity correlation functions, 146
 - Q -parameter, 152–153
- coherent interactions and transients, 4–5
- coherent-state wave packet, 59
- coherent states
 - atomic, 333
 - characteristic function, 79–82
 - completeness relation, 62–63
 - density operators, 68
 - displaced vacuum states, 56–58
 - function, 63–64
 - generation, 60–61
 - independence, 63
 - minimum uncertainty states, 51–56
 - number state, 61–62
 - operator matrix states, 64–65
 - phase-space pictures, 65–67
 - phase-space probability distributions, 68–75
 - photon number parity operator and Wigner function, 75–78
 - Q function, 82, 83
 - right eigenstates of annihilation operator, 50–51
 - Schrödinger-cat states, 89
 - spin, 333
 - time evolution, 59–60
 - wave packets, 58–59
 - Wigner functions, 82
- complementarity, 289
- complexity classification, 359
- Compton effect, 155
- Compton wavelength, 34
- controlled phase gate, 373, 376
- Copenhagen interpretation, 217, 280
- correlated double-beam states of light, 216–232
- Coulomb gauge, 3
- Coulomb potential, 33
- Coulomb radiation gauge, 90
- creation operator, 15
- cryptography
 - information processing, 355–356
 - quantum, 364–370
- crypto-systems
 - private, 357–358
 - public, 358–360
- decoherence
 - coherent state generation, 275–276
 - nonlinear optical balance, 275–276
 - overview, 272–275
 - quantum error correction, 380
- decoherence-free subspace, 380
- degenerate four-wave mixing, 209
- degenerate parametric
 - down-conversion, 208
- density matrix, 121
- density operator
 - atom–field interactions, 119–122
 - dynamics, 395–396
 - overview, 386–389
- Deutsch’s problem, 374
- dipole approximation, 27, 91
- dipole interaction, 139
- dipole moment, 91
- disentangling theorem, 56
- dispersive interactions, 123–125
- dispersive model, 89
- displaced vacuum states, 56–58
- displacement operator, 56
- dissipative interaction, 6
- double-slit experiment, 380
- down-conversion processes, 406–407
 - entangled photon states, 285–287
 - metrology without absolute standards, 304
 - paired single-photon states, 281–285
- dressed states, 115–119
- dual-rail realization, 376
- eavesdropper, 356
- Ekert protocol, 369–370
- Einstein coefficients, 100–101

- electric field operator, 18–20
- electron shelving, 6
- ensembles, quantum mechanics
 - decoherence, 272–276
 - modeling losses with fictitious beam splitters, 270–272
- entangled photon states, 285–287
- entanglement
 - advantage, 340
 - generation, 238–239
 - photon, 186–187
 - research history of, 7
 - two-particle, 390–392
- entanglement applications
 - Heisenberg-limited interferometry, 343–353
 - quantum information processing, 353–381
- entanglement theorems
 - no-cloning, 342–343
 - no-signaling, 341–342
- entropy (von Neumann), 127, 394–395
- ergodic hypothesis, 135
- error circle, 67
- error contours, 205
- error correction, 380
- even coherent states, 218
- exponential decay law, 257
- factorization
 - property, 136
- fair sampling assumption, 300
- fictitious beam splitter, 270–272
- field ionization, 310
- field quantization
 - multimode fields, 20–27
 - quantum phase, 37–45
 - single-mode field harmonic oscillation, 11–17
 - single-mode field quadrature operators, 18–20
 - single-mode field quantum fluctuations, 17–18
 - thermal fields, 32
 - vacuum fluctuations and zero-point energy, 32–37
- Fock state basis, 127
- Franson’s experiment, 301
- Fredkin gate, 378
- fringe visibility, 136
- gauge transformations, 90
- Glauber–Sudarshan P function, 68
- Golden Rule, 96
- gravitational waves, 178
- Hadamard gate, 371–372
- Hamiltonian derivation, 402–405
- Hanbury Brown and Twiss experiment, 146–152
- harmonic generation, 5
- Heisenberg limit, 178
- Heisenberg-limited interferometry, 343–353
- Hermite polynomials, 59
- homodyne detection, 209–210
- Hong–Ou–Mandel effect, 170
- Hong–Ou–Mandel experiment (HOM experiment), 285–287
- Husimi function, 73
- idler mode, 240
- induced coherence experiment, 290–293
- induced quantum coherence experiment, 36
- intelligent states, 52
- interference
 - multiphoton, 186
 - non-interference, 186
 - one photon, 281–285
 - quantum, 3
 - two photon, 285–287, 390–392
 - Young’s, 143–146
- interferometry
 - classical states of light, 177–179
 - interaction-free measurement, 175–177
 - LIGO (Laser Interferometer Gravitational-Wave Observatory), 178
 - Mach–Zehnder interferometer (MZI), 173, 174
 - single photon, 173–175
 - SU(2) formulation, 179–185
- ion traps, 258
- irreversible decay, 101

- Jaynes–Cummings model
 - atom–field interactions, 105–115
 - CQED realization, 316–320, 325–326
 - extensions, 125–126
 - quantum state engineering, 326–328
 - Schmidt decomposition, 126–127
 - trapped ion, 328–332
 - von Neumann entropy, 127
- jumping cat transition, 266–265
- Kerr interaction, 223
- Kerr-like medium, 222
- Lamb–Dicke parameter, 330
- laser cooling, 5
- light quanta, 2
- LIGO (Laser Interferometer Gravitational-Wave Observatory), 178
- Liouville equation, 396
- local oscillator, 209
- logic gates, 371
- Lorentz gauge, 90
- Mach–Zehnder interferometer (MZI), 173, 174, 175–177
- masers, 4
- master equation, 259
- Maxwell’s equations, 11
- metrology, 304
- mixed states, 387
- momentum entanglement, 301
- monochromatic light field, 136–139
- Moore’s law, 338–339
- multimode field quantization
 - annihilation and creation operators, 24
 - cubicle cavity, 20–21
 - dipole approximation, 27
 - electric field, 26–27
 - field energy, 24
 - magnetic contribution, 23–24
 - mode density, 22
 - transversality condition, 22
 - vector potential, 22
- multimode number state, 25
- multipartite systems, 391
- multiphoton interference, 186
- mutual coherence, 135
- no-cloning theorem, 342–343
- nonclassical states of light
 - broadband squeezed light, 232–233
 - correlated double beams, 216–232
 - criterion for, 191
 - entanglement generation, 238–239
 - pair coherent states, 233–238
 - photon antibunching effect, 213–216
 - quantum state engineering, 239–247
 - Schrödinger-cat states, 216–225
 - squeezed states of light, 191–213
- quantum non-demolition
 - measurement, 325–326
- nonlinear susceptibility, 207–209
- nonlocal hidden variable, 280
- nonlocality
 - Aharonov–Bohm effect, 177
 - Bell’s inequalities violation, 177
- normally ordered operator, 71–72
- no-signaling theorem, 341–342
- number operator, 15
- number–phase uncertainty relation, 211–213
- number squeezed states of light, 211–213
- number state, 17
- odd coherent states, 219
- one-photon interference experiments, 281–285
- one-time pad, 358
- optical cavity QED, 332
- optical equivalence theorem, 71
- optical frequency standard, 259
- optical lattice, 379
- $\pi/2$ -pulses, 324, 372
- pair coherent states, 233–238
- paired single-photon states, 281–285
- parametric amplifier, 211
- parametric approximation, 185
- parametric down-conversion, 5
- parity measurement, 349
- parity operator, 75–78
- Pauli exclusion principle, 167

- Pauli spin algebra, 106
 Pegg–Barnett phase operators,
 42–45, 106
 periodic boundary conditions, 20
 perturbation theory, 89–91
 phase uncertainty, 178
 phonons, 328–329
 photodetection, 140
 photoelectric effect, 155
 photon
 non-interference, 186
 photon-added coherent state, 241
 photon antibunching effect, 151,
 213–216
 photon bunching effect, 149
 nonclassical state generation,
 239–247
 single-photon beam splitter,
 165–166
 single-photon interferometry,
 173–175
 single-photon source, 156
 photon subtraction, 243
 photon tunneling exhibiting
 superluminal effects, 293–294
 photonic band-gap material, 293
 photon number parity operator and
 Wigner function, 293
 photons, 20
 Planck’s radiation law, 32
 plane-wave field, 27
 Poisson process, 53
 polarization, 22
 population inversion, 101
 π -pulses, 293–294
P-representation, 73
 privacy amplification, 366
 private key crypto-systems, 357–358
 public key crypto-systems, 358–360
 pure state, 110–111
 purity (in atom–field interactions), 127
- Q* function, 82, 83
Q-parameter, 152–153
 quadrature operator, 19
 quadrature squeezed state of light
 detection, 209–211
 generation, 207–209
 overview, 191–207
- quadrature variance, 46
 quantum algorithm, 6
 quantum computation, 6
 quantum computation gates
 aspects of, 370–375
 optical realization, 376–379
 quantum computers, 338
 quantum correlations, 4
 quantum cryptography
 B92 protocol, 367–368
 BB84 protocol, 365–366
 Ekert protocol, 369–370
 overview, 364
 quantum key distribution (QKD),
 364–365
 quantum defect, 308
 quantum electrodynamics (QED), 3–4
 quantum eraser, 287–290
 quantum error correction, 380
 quantum estimation theory, 45
 quantum gates, 6
 quantum information processing
 cryptography, 355–356
 private key crypto-systems,
 357–358
 public key crypto-systems, 358–360
 quantum cryptography, 364–370
 quantum random number
 generator, 360–363
 quantum teleportation, 353–355
 quantum information processing,
 future prospects
 decoherence and error
 correction, 380
 gate optical realization, 376–379
 quantum computation gates,
 370–375
 quantum interference, 3
 quantum jump method, 262–266
 quantum key distribution (QKD),
 364–365
 quantum measurement theory, 398–401
 quantum mechanical first-order
 coherence functions, 141–143
 quantum mechanics
 ensembles, 266–276
 interaction-free measurement,
 175–177
 nonlocality, 177

- single realizations, 262–265
- quantum mechanics, history
 - coherent interactions and
 - transients, 4–5
 - entanglement, 7
 - factorization, 6
 - ion trap, 6–7
 - Jaynes–Cummings model, 5–6
 - masers, 4
 - nature of light rays, 2
 - phase-sensitive noise, 5
 - photon, 2–3
 - quantum computation, 6
 - quantum electrodynamics (QED), 3–4
 - quantum information processing, 4
 - quantum interference, 3
 - quantum memories, 7
 - quantum nonlinear optics, 5
 - quantum optics, 4
 - quantum theory of coherence, 4
 - wave and particle properties, 3
- quantum memories, 7
- quantum nonlinear optics, 5
- quantum phase, 18, 37–45
- quantum processor, 7
- quantum random number generator, 360–363
- quantum register, 370–371
- quantum state engineering, 239–247
- quantum state tomography, 85
- quantum teleportation, 353–355
- quantum theory of coherence, 4
- quantum trajectory approach, 258
- quasi-probability distribution, 4

- Rabi model, 102–105
- Ramsey interferometry, 317
- rate equations, 258
- Rayleigh–Jeans limit, 312
- Rayleigh’s law, 31
- realism, 280
- renormalization, 3
- resonance fluorescence, 5
- right eigenstates of annihilation, 50–51
- rotated quadrature operators, 195
- rotating-wave approximation, 89
- Rydberg atoms
 - cavity–field interaction, 311–315

- CQED experiments, 308
 - overview, 308–311

- Schmidt decomposition, 126–127, 392–394
- Schrödinger-cat states, 89, 216–225
- second-order quantum coherence, 149
- Segal–Bargmann space, 63
- semigroup relations, 57
- signal mode, 208
- single-ion traps, 259
- single realizations
 - jumping cat transition, 266–265
 - quantum jump method, 262–266
 - V system, 259–262
- single-mode field quadrature operators, 18–20
- single-mode field quantization
 - canonical variable replacement, 12–15
 - equivalence to harmonic oscillator, 11–12
 - harmonic oscillation energy levels, 16
 - operator replacement, 12–17
- single-mode field quantum fluctuations
 - number state, 17
 - quantum phase, 18
 - uncertainty of the field, 17
 - vacuum fluctuations, 18
- space-like separations, 280
- s-parameterized function, 80
- spin
 - coherent states, 333
 - Pauli spin algebra, 106
- spin coherent states, 333
- spontaneous emission, 33, 101–102
- squeezed states of light
 - interferometric measurement, 178–179
 - number, 211–213
 - quadrature, 191–211
- standard quantum limit, 178
- Stark shift, 317
- state reduction, 225
- state vector collapse, 398
- states of light
 - classical, 177–179
 - displaced number, 185

- states of light (cont.)
 interference containing multiple photons, 186
 nonclassical, 191–247
 phase uncertainty, 178
 squeezed, 178–179
 statistical mixture, 163
 Stefan–Boltzmann law, 32
 SU(2) formulation of beam splitters and interferometry, 179–185
 sub-Poissonian statistics, 152
 superluminal tunneling, 293–294
 super-radiance, 332
 Susskind–Glogower (SG) operator, 39
- tempered distribution, 71
 temporal coherence, 136–139
 thermal distribution, 230
 thermal fields, 29, 32
 thermal radiation, 33
 time evolution, 59–60
 time standard, 261
 time–energy uncertainty, 18
 transition rate, 96
 transversality condition, 22
 transverse gauge, 22
 twin beams, 228
 two photon interference experiments
 entanglement, 390–392
 Hong–Ou–Mandel interferometer, 285–287
- Schmidt decomposition, 392–394
 two-mode squeezed vacuum states of light, 216–232
- uncertainty of the field, 17
 uncertainty principle, 297
- V system, 259–262
 vacuum-field Rabi oscillations, 109
 vacuum fluctuations
 defined, 18
 displaced, 56–58
 field quantization, 32–37
 vacuum Rabi frequency, 314
 vibrational motion, 178, 308
 von Neumann entropy, 394–395
- wave packets, 58–59
 Wien’s displacement law, 32
 Weisskopf–Wigner theory, 3–4
 which-path information, 289
 Wien’s law, 32
 Wigner functions, 73
- Young’s interference, 143–146
 Yurke–Stoler state, 219
- zero-point energy (ZPE)
 Casimir effect, 35–37
 Lamb shift, 33–35