Cambridge University Press & Assessment 978-1-009-35145-4 — Fixed Point Theory and Variational Principles in Metric Spaces Qamrul Hasan Ansari, Daya Ram Sahu Table of Contents <u>More Information</u>

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