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Entries for authors refer to places where either their name or one of their publications has been cited.

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