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Edited by Hamid Abban, Gavin Brown, Alexander Kasprzyk, Shigefumi Mori

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To Miles Reid for his 70th Birthday

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70 Miles

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