

Aerodynamics for Engineers

Sixth Edition

Now reissued by Cambridge University Press, this sixth edition covers the fundamentals of aerodynamics using clear explanations and real-world examples. Aerodynamics concept boxes throughout showcase real-world applications, chapter objectives provide readers with a better understanding of the goal of each chapter and highlight the key "take-home" concepts, and example problems aid understanding of how to apply core concepts. Coverage also includes the importance of aerodynamics to aircraft performance, applications of potential flow theory to aerodynamics, high-lift military airfoils, subsonic compressible transformations, and the distinguishing characteristics of hypersonic flow.

Supported online by a solutions manual for instructors, MATLAB® files for example problems, and lecture slides for most chapters, this is an ideal textbook for undergraduates taking introductory courses in aerodynamics, and for graduates taking preparatory courses in aerodynamics before progressing to more advanced study.

John J. Bertin, deceased, was Professor Emeritus of Aeronautics at the U.S. Air Force Academy, formerly holding positions at NASA, The University of Texas at Austin, and Sandia National Laboratories.

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Aerodynamics for Engineers

Sixth Edition

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Contents

PREFACE			хi
CHAPTER 1	WHY STUDY AERODYNAMICS?		1
	1.1	Aerodynamics and the Energy-Maneuverability Technique 2	
	1.2	Solving for the Aerothermodynamic Parameters 8	
	1.3 1.4	Description of an Airplane 26 Summary 27	
		Problems 28 References 32	
CHAPTER 2	FUND	AMENTALS OF FLUID MECHANICS	33
	2.1 2.2 2.3 2.4 2.5 2.6 2.7 2.8 2.9	Introduction to Fluid Dynamics 34 Conservation of Mass 36 Conservation of Linear Momentum 40 Applications to Constant-Property Flows 46 Reynolds Number and Mach Number as Similarity Parameters 55 Concept of the Boundary Layer 63 Conservation of Energy 65 First Law of Thermodynamics 66 Derivation of the Energy Equation 68	
	2.10	Summary 76 Problems 76 References 87	
CHAPTER 3		MICS OF AN INCOMPRESSIBLE, CID FLOW FIELD	88
	3.1 3.2 3.3	Inviscid Flows 89 Bernoulli's Equation 90 Use of Bernoulli's Equation to Determine Airspeed 93	
	3.4 3.5 3.6 3.7	The Pressure Coefficient 96 Circulation 99 Irrotational Flow 102 Kelvin's Theorem 103	



vi				Contents
		3.8	Incompressible, Irrotational Flow and the Velocity Potential 104	
		3.9	Stream Function in a Two-Dimensional, Incompressible Flow 107	
		3.10	Relation between Streamlines and Equipotential Lines 109	
		3.11	Superposition of Flows 112	
		3.12	Elementary Flows 113	
		3.13	Adding Elementary Flows to Describe Flow Around a Cylinder 126	
		3.14	Lift and Drag Coefficients as Dimensionless Flow-Field Parameters 134	
		3.15	Flow Around a Cylinder with Circulation 139	
		3.16	Source Density Distribution on the Body Surface 144	
		3.17	Incompressible, Axisymmetric Flow 149	
		3.18	Summary 152	
			Problems 152	
			References 165	
	CHAPTER 4	visco	US BOUNDARY LAYERS	166
		4.1	Equations Governing the Boundary Layer for a Steady, Two-Dimensional, Incompressible Flow 167	
		4.2	Boundary Conditions 170	
		4.3	Incompressible, Laminar Boundary Layer 171	
		4.4	Boundary-Layer Transition 189	
		4.5 4.6	Incompressible, Turbulent Boundary Layer 193 Eddy Viscosity and Mixing Length	
		1.0	Concepts 202	
		4.7	Integral Equations for a Flat-Plate Boundary Layer 204	
		4.8	Thermal Boundary Layer for Constant-Property Flows 215	
		4.9	Summary 221	
			Problems 221	
			References 225	
	CHAPTER 5		ACTERISTIC PARAMETERS FOR AIRFOIL VING AERODYNAMICS	226
		5.1	Characterization of Aerodynamic Forces and Moments 227	

Airfoil Geometry Parameters 231

5.2



Contents

Cambridge University Press & Assessment 978-1-009-09862-5 — Aerodynamics for Engineers: 6th Edition John J. Bertin , Russell M. Cummings Frontmatter More Information

	5.3	Wing-Geometry Parameters 236	
	5.4	Aerodynamic Force and Moment	
	3.4	Coefficients 244	
	5.5	Wings of Finite Span 273	
	0.0		
		Problems 288	
		References 292	
CHAPTER 6	INCOI	MPRESSIBLE FLOWS AROUND AIRFOILS	
	OF IN	FINITE SPAN	294
	6.1	General Comments 295	
	6.2	Circulation and the Generation of Lift 296	
	6.3	General Thin-Airfoil Theory 298	
	6.4	Thin, Flat-Plate Airfoil (Symmetric Airfoil) 301	
	6.5	Thin, Cambered Airfoil 306	
	6.6	Laminar-Flow Airfoils 317	
	6.7	High-Lift Airfoil Sections 321	
	6.8	Multielement Airfoil Sections for Generating	
		High Lift 327	
	6.9	High-Lift Military Airfoils 334	
		Problems 337	
		References 339	
CHAPTER 7	INCOL	MPRESSIBLE FLOW ABOUT WINGS	
CHAI IEN I		NITE SPAN	341
	7.1	General Comments 342	
	7.2	Vortex System 345	
	7.3	Lifting-Line Theory for Unswept Wings 346	
	7.4	Panel Methods 375	
	/ . 4		
	7.4		
		Vortex Lattice Method 379	
	7.5	Vortex Lattice Method 379 Factors Affecting Drag Due-to-Lift at Subsonic	
	7.5 7.6	Vortex Lattice Method 379 Factors Affecting Drag Due-to-Lift at Subsonic Speeds 401	
	7.5 7.6 7.7	Vortex Lattice Method 379 Factors Affecting Drag Due-to-Lift at Subsonic Speeds 401 Delta Wings 404	
	7.5 7.6 7.7 7.8	Vortex Lattice Method 379 Factors Affecting Drag Due-to-Lift at Subsonic Speeds 401 Delta Wings 404 Leading-Edge Extensions 414	
	7.5 7.6 7.7	Vortex Lattice Method 379 Factors Affecting Drag Due-to-Lift at Subsonic Speeds 401 Delta Wings 404 Leading-Edge Extensions 414 Asymmetric Loads on the Fuselage at High	
	7.5 7.6 7.7 7.8	Vortex Lattice Method 379 Factors Affecting Drag Due-to-Lift at Subsonic Speeds 401 Delta Wings 404 Leading-Edge Extensions 414 Asymmetric Loads on the Fuselage at High Angles of Attack 418	
	7.5 7.6 7.7 7.8 7.9	Vortex Lattice Method 379 Factors Affecting Drag Due-to-Lift at Subsonic Speeds 401 Delta Wings 404 Leading-Edge Extensions 414 Asymmetric Loads on the Fuselage at High	
	7.5 7.6 7.7 7.8 7.9	Vortex Lattice Method 379 Factors Affecting Drag Due-to-Lift at Subsonic Speeds 401 Delta Wings 404 Leading-Edge Extensions 414 Asymmetric Loads on the Fuselage at High Angles of Attack 418 Flow Fields for Aircraft at High Angles of	
	7.5 7.6 7.7 7.8 7.9 7.10	Vortex Lattice Method 379 Factors Affecting Drag Due-to-Lift at Subsonic Speeds 401 Delta Wings 404 Leading-Edge Extensions 414 Asymmetric Loads on the Fuselage at High Angles of Attack 418 Flow Fields for Aircraft at High Angles of Attack 422	
	7.5 7.6 7.7 7.8 7.9 7.10 7.11	Vortex Lattice Method 379 Factors Affecting Drag Due-to-Lift at Subsonic Speeds 401 Delta Wings 404 Leading-Edge Extensions 414 Asymmetric Loads on the Fuselage at High Angles of Attack 418 Flow Fields for Aircraft at High Angles of Attack 422 Unmanned Air Vehicle Wings 424	

vii



viii Contents

CHAPTER 8	DYNA	MICS OF A COMPRESSIBLE FLOW FIELD	431
CHAPTER	DINA	mics of A compressible resultiles	731
	8.1	Thermodynamic Concepts 432	
	8.2	Adiabatic Flow in a Variable-Area	
		Streamtube 441	
	8.3	Isentropic Flow in a Variable-Area Streamtube 445	
	8.4	Converging-diverging Nozzles 451	
	8.5	Characteristic Equations and Prandtl-Meyer Flows 454	
	8.6	Shock Waves 462	
	8.7	Viscous Boundary Layer 473	
	8.8	Shock-Wave/Boundary-Layer Interactions 480	
	8.9	Shock/Shock Interactions 482	
	8.10	The Role of Experiments for Generating Information Defining the Flow Field 486	
	8.11	Comments About the Scaling/Correction Process(es) for Relatively Clean Cruise Configurations 494	
	8.12	Summary 495	
		Problems 495 References 502	
CHAPTER 9		RESSIBLE, SUBSONIC FLOWS TRANSONIC FLOWS	505
CHAPTER 9			505
CHAPTER 9	9.1 9.2 9.3 9.4 9.5	Compressible, Subsonic Flow 506 Transonic Flow Past Unswept Airfoils 517 Wave Drag Reduction by Design 526 Swept Wings at Transonic Speeds 527 Transonic Aircraft 543	505
	9.1 9.2 9.3 9.4 9.5 9.6	Compressible, Subsonic Flow 506 Transonic Flow Past Unswept Airfoils 517 Wave Drag Reduction by Design 526 Swept Wings at Transonic Speeds 527 Transonic Aircraft 543 Summary 548 Problems 548	505 551
	9.1 9.2 9.3 9.4 9.5 9.6	Compressible, Subsonic Flow 506 Transonic Flow Past Unswept Airfoils 517 Wave Drag Reduction by Design 526 Swept Wings at Transonic Speeds 527 Transonic Aircraft 543 Summary 548 Problems 548 References 548 DIMENSIONAL, SUPERSONIC FLOWS	
	9.1 9.2 9.3 9.4 9.5 9.6	Compressible, Subsonic Flow 506 Transonic Flow Past Unswept Airfoils 517 Wave Drag Reduction by Design 526 Swept Wings at Transonic Speeds 527 Transonic Aircraft 543 Summary 548 Problems 548 References 548 CIMENSIONAL, SUPERSONIC FLOWS ND THIN AIRFOILS Linear Theory 553 Second-Order Theory (Busemann's	



Contents

CHAPTER 11		SONIC FLOWS OVER WINGS IRPLANE CONFIGURATIONS
	11.1	General Remarks About Lift and Drag 579
	11.2	General Remarks About Supersonic Wings 581
	11.3	Governing Equation and Boundary Conditions 583
	11.4	Consequences of Linearity 584
	11.5	Solution Methods 585
	11.6	Conical-Flow Method 585
	11.7	Singularity-Distribution Method 598
	11.8	Design Considerations for Supersonic
	11.9	Aircraft 625 Some Comments About the Design of the SST and of the HSCT 627
	11.10	Slender Body Theory 634
	11.11	Base Drag 636
	11.12	Aerodynamic Interaction 639
	11.13	Aerodynamic Analysis for Complete Configurations in a Supersonic Free
		Stream 642
	11.14	Summary 643
		Problems 644
		References 646

CHAPTER 12 HYPERSONIC FLOWS

577

12.1	The Five Distinguishing Characteristics 652
12.2	Newtonian Flow Model 657
12.3	Stagnation Region Flow-Field
	Properties 660
12.4	Modified Newtonian Flow 665
12.5	High <i>L/D</i> Hypersonic Configurations—
	Waveriders 682
12.6	Aerodynamic Heating 691
12.7	A Hypersonic Cruiser for the Twenty-First
	Century? 697
12.8	Importance of Interrelating CFD, Ground-Test
	Data, and Flight-Test Data 700
12.9	Boundary-Layer-Transition Methodology 702
12.10	Summary 706
	Problems 706
	References 708



х

Cambridge University Press & Assessment 978-1-009-09862-5 — Aerodynamics for Engineers: 6th Edition John J. Bertin , Russell M. Cummings Frontmatter More Information

> Contents 711 CHAPTER 13 AERODYNAMIC DESIGN CONSIDERATIONS 13.1 High-Lift Configurations 712 13.2 Circulation Control Wing 725 13.3 Design Considerations for Tactical Military Aircraft 727 13.4 Drag Reduction 731 13.5 Development of an Airframe Modification to Improve the Mission Effectiveness of an Existing Airplane 742 13.6 Considerations for Wing/Canard, Wing/Tail, and Tailless Configurations 758 13.7 Comments on the F-15 Design 763 13.8 The Design of the F-22 764 13.9 The Design of the F-35 767 13.10 Summary 770 Problems 770 References 772 CHAPTER 14 TOOLS FOR DEFINING THE AERODYNAMIC **ENVIRONMENT** *775* 14.1 Computational Tools 777 14.2 Establishing the Credibility of CFD Simulations 783 14.3 Ground-Based Test Programs 785 14.4 Flight-Test Programs 788 14.5 Integration of Experimental and Computational Tools: The Aerodynamic Design Philosophy 789 14.6 Summary 790 References 790 APPENDIX A THE EOUATIONS OF MOTION WRITTEN IN CONSERVATION FORM 792 A COLLECTION OF OFTEN USED TABLES APPENDIX B **798** ANSWERS TO SELECTED PROBLEMS 806 **CREDITS** 811 **INDEX** 815 **CONVERSION FACTORS** 827



Preface

A great deal has happened since the preface to the fifth edition of *Aerodynamics for Engineers* was written early in 2008. During the spring and early summer of 2008, John Bertin and I were busy checking chapter proofs for "The Book" (as he liked to call it). John was at home in Houston and teaching at his beloved Rice University (you may have noticed that covers of the various editions of *Aerodynamics for Engineers* were usually blue and light gray, the colors of Rice University). I was a visiting researcher at the Institute of Aerodynamics and Flow Technology at The German Aerospace Center (DLR) in Braunschweig. John had two major struggles in his life at the time: he was working through the last stages of the illness that would take his wife, Ruth, from him. He had also been diagnosed with pancreatic cancer, and was dealing with doctors, treatments, and hospitals. We spoke on the phone often about the various challenges he was facing, both with his wife's and his own health. Through the support of his family, as well as his desire to finish the fifth edition, he made it through the summer of 2008 in reasonably good shape. Copies of the book were shipped to us in July 2008, and he was very glad that we had finished the undertaking we had started so many years earlier.

Unfortunately, John's pancreatic cancer took a turn for the worse in late summer of 2008, and he passed away on October 11, 2008. A large number of former co-workers from NASA and various universities, as well as his family and friends, attended his funeral later that month, and we all knew that a very special person had passed from our ranks.

One of the things that John and I talked about during his last months of life was his desire for *Aerodynamics for Engineers* to continue to grow and evolve, even if he was not around to help with that task. I cannot help but think that he asked me to be his co-author for the fifth edition for this purpose. So, in spite of the fact that John is no longer with us, his spirit and excitement for learning will continue to live.

So, there were many goals for writing the sixth edition of *Aerodynamics for Engineers*: (1) to continue the legacy of Professor Bertin; (2) to rewrite many of the sections that provide readers with a motivation for studying aerodynamics in a more casual, enjoyable, and readable manner; (3) to update the technical innovations and advancements that have taken place in aerodynamics since the writing of the previous edition; and (4) to add aerodynamics concept boxes throughout the book to enhance the interest of readers.

To help achieve these goals I provided readers with the following new information: importance of aerodynamics to aircraft performance, a description of the airplane, the irrotational flow condition, applications of potential flow theory to aerodynamics, expanded descriptions of airfoil geometry and nomenclature, high lift military airfoils, the effect of taper ratio on wing efficiency, induced drag estimation, converging-diverging nozzles, shock/shock interactions, subsonic compressible transformations, additional compressibility corrections, critical Mach number, drag divergence Mach number, base drag, and the distinguishing characteristics of hypersonic flow. These new sections should greatly enhance the usability of the book.

In addition, there are numerous new figures containing updated information, as well as numerous, additional up-to-date references throughout the book. Finally, numerous new example problems have been added throughout the book to enhance the

χi



xii Preface

learning of aerodynamics by the reader, and answers to selected problems have been added to help students know when they have done the problems correctly. Users of the fifth edition of the book will find that all material included in that edition is still included in the sixth edition, with the new material added throughout the book to bring a real-world flavor to the concepts being developed. I hope that readers will find the inclusion of all of this additional material helpful and informative.

Finally, no major revision of a book like Aerodynamics for Engineers can take place without the help of many people. I am especially indebted to everyone who aided in collecting new materials for the sixth edition. I want to especially thank Preston A. Henne and Robert van't Riet of McDonnell Douglas; Eli Reshotko of Case Western Reserve University; David W. Hall of DHC Engineering; Stuart Rogers of NASA Ames Research Center; David McDaniel of the University of Alabama, Birmingham; Hans Hornung of Caltech; Andreas Schütte and Martin Hepperle of DLR; Patrick Champigny of ONERA; Aaron Byerley of the U.S. Air Force Academy; John McMasters of The Boeing Company; and William H. Mason of Virginia Tech. In addition, I am very grateful for the excellent suggestions and comments made by the reviewers of the sixth edition: Roger L. Simpson of Virginia Tech, Tej R. Gupta of Embry-Riddle Aeronautical University, Serhat Hosder of Missouri University of Science and Technology, and Lisa Grega of The College of New Jersey. The editorial and production staff at Pearson has been outstanding in their support of this new edition: I greatly appreciate their efforts. I am also extremely grateful to the many students at the U.S. Air Force Academy who have pointed out errors that they found in the previous edition. I hope that everyone who reads this book will find it useful and educational.

WHAT'S NEW TO THIS EDITION?

- Aerodynamics concept boxes added throughout the book to bring real-world examples and applications to light as new material is being learned
- Chapter objectives to give readers a better understanding of the goal of each chapter and what concepts they should understand after reading through the chapter
- Significant re-writing of material and derivations from previous editions to improve clarity and usefulness
- Extra example problems to improve understanding of how to apply concepts to useful applications
- Significant new sections added on the topics of: importance of aerodynamics to aircraft performance, a description of the airplane, the irrotational flow condition, applications of potential flow theory to aerodynamics, expanded description of airfoil geometry and nomenclature, high lift military airfoils, the effect of taper ratio on wing efficiency, induced drag estimation, converging-diverging nozzles, shock/shock interactions, subsonic compressible transformations, additional compressibility corrections, critical Mach number, drag divergence Mach number, base drag, and the distinguishing characteristics of hypersonic flow
- Updated figures and photographs to help readers see concepts from real examples and on real aircraft
- Answers to selected problems

Enjoy your study of aerodynamics!



Preface xiii

INSTRUCTORS RESOURCES

Resources to accompany the text are located at www.cambridge.org/bertin-cummings6e.

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