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Edited by Anthony Nixon, Sean Prendiville

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Contents

	<i>Preface</i>	<i>page vii</i>
	<i>Anthony Nixon and Sean Prendiville</i>	
1	Fair Partitions <i>Noga Alon</i>	1
2	Hypergraph Turán Problems in ℓ_2-Norm <i>József Balogh, Felix Christian Clemen, Bernard Lidický</i>	21
3	Circuit Imbalance Measures and Linear Programming <i>Farbod Ekbatani, Bento Natura, László A. Végh</i>	64
4	Intersection Problems in Extremal Combinatorics: Theorems, Techniques and Questions Old and New <i>David Ellis</i>	115
5	Finite Geometry and Extremal Graph Theory <i>Valentina Pepe</i>	174
6	Rainbow Subgraphs and their Applications <i>Alexey Pokrovskiy</i>	191
7	Explicit Bounds for Graph Minors <i>Paul Wollan</i>	215
8	Convex and Combinatorial Tropical Geometry <i>Josephine Yu</i>	237

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Frontmatter
[More Information](#)

Preface

The twenty-ninth British Combinatorial Conference takes place at Lancaster University, from Monday 11th to Friday 15th of July 2022. The British Combinatorial Committee invited nine distinguished combinatorialists to give survey lectures in areas of their expertise, and this volume contains the survey articles on which eight of these lectures are based.

In compiling this volume, we are indebted to the authors for preparing their articles so accurately and professionally, and to the referees for their rapid responses and keen eye for detail. We would also like to thank Tom Harris at Cambridge University Press. Finally, without the previous efforts of editors of earlier Surveys and the guidance of the British Combinatorial Committee, the preparation of this volume would have been somewhat daunting.

The twenty-ninth British Combinatorial Conference is organised in partnership with the Clay Mathematics Institute, the Heilbronn Institute for Mathematical Research through the UKRI/EPSRC Additional Funding Programme for Mathematical Sciences, the London Mathematical Society, the Institute of Combinatorics and its Applications, the Foundation Compositio Mathematica and Lancaster University; we thank each of these organisations for their generous involvement and support.

Anthony Nixon
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