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978-0-521-89545-3 - Groups, Graphs and Trees: An Introduction to the Geometry of Infinite Groups

John Meier

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