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978-0-521-87909-5 - Rigidity in Higher Rank Abelian Group Actions, Volume I.:

Introduction and Cocycle Problem

Anatole Katok and Viorel Nitica

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