APPROACHES TO QUANTUM GRAVITY

Toward a New Understanding of Space, Time and Matter

The theory of quantum gravity promises a revolutionary new understanding of gravity and spacetime, valid from microscopic to cosmological distances. Research in this field involves an exciting blend of rigorous mathematics and bold speculations, foundational questions and technical issues.

Containing contributions from leading researchers in this field, this book presents the fundamental issues involved in the construction of a quantum theory of gravity and building up a quantum picture of space and time. It introduces the most current approaches to this problem, and reviews their main achievements. Each part ends in questions and answers, in which the contributors explore the merits and problems of the various approaches. This book provides a complete overview of this field from the frontiers of theoretical physics research for graduate students and researchers.

DANIELE ORITI is a Researcher at the Max Planck Institute for Gravitational Physics, Potsdam, Germany, working on non-perturbative quantum gravity. He has previously worked at the Perimeter Institute for Theoretical Physics, Canada; the Institute for Theoretical Physics at Utrecht University, The Netherlands; and the Department of Applied Mathematics and Theoretical Physics, University of Cambridge, UK. He is well known for his results on spin foam models, and is among the leading researchers in the group field theory approach to quantum gravity.

APPROACHES TO QUANTUM GRAVITY

Toward a New Understanding of Space, Time and Matter

Edited by

DANIELE ORITI Max Planck Institute for Gravitational Physics, Potsdam, Germany



> CAMBRIDGE UNIVERSITY PRESS Cambridge, New York, Melbourne, Madrid, Cape Town, Singapore, São Paulo, Delhi Cambridge University Press

The Edinburgh Building, Cambridge CB2 8RU, UK

Published in the United States of America by Cambridge University Press, New York

www.cambridge.org Information on this title: www.cambridge.org/9780521860451

© Cambridge University Press 2009

This publication is in copyright. Subject to statutory exception and to the provisions of relevant collective licensing agreements, no reproduction of any part may take place without the written permission of Cambridge University Press.

First published 2009

Printed in the United Kingdom at the University Press, Cambridge

A catalogue record for this publication is available from the British Library

ISBN 978-0-521-86045-1 hardback

Cambridge University Press has no responsibility for the persistence or accuracy of URLs for external or third-party internet websites referred to in this publication, and does not guarantee that any content on such websites is, or will remain, accurate or appropriate.

A Sandra

Contents

List of contributors Preface		page x xv
Par	rt I Fundamental ideas and general formalisms	1
1	Unfinished revolution	3
	C. Rovelli	
2	The fundamental nature of space and time	13
	G. 't Hooft	
3	Does locality fail at intermediate length scales?	26
	R. D. Sorkin	
4	Prolegomena to any future Quantum Gravity	44
	J. Stachel	
5	Spacetime symmetries in histories canonical gravity	68
	N. Savvidou	
6	Categorical geometry and the mathematical	
	foundations of Quantum Gravity	84
	L. Crane	
7	Emergent relativity	99
	O. Dreyer	
8	Asymptotic safety	111
	R. Percacci	
9	New directions in background independent Quantum Gravity	129
	F. Markopoulou	
Questions and answers		150
Part II String/M-theory		167
10	Gauge/gravity duality	169
	G. Horowitz and J. Polchinski	

viii	Contents	
11	String theory, holography and Quantum Gravity T. Banks	187
12	String field theory	210
	W. Taylor	
Qu	nestions and answers	229
Pa	art III Loop quantum gravity and spin foam models	233
13	Loop quantum gravity	235
14	<i>T. Thiemann</i> Covariant loop quantum gravity?	253
11	E. Livine	235
15	The spin foam representation of loop quantum gravity <i>A. Perez.</i>	272
16		290
17		310
Qu	pestions and answers	332
Do	nt IV Discusso Quantum Cravity	339
18	It IV Discrete Quantum GravityQuantum Gravity: the art of building spacetime	339 341
10	J. Ambjørn, J. Jurkiewicz and R. Loll	541
19	Quantum Regge calculus	360
	R. Williams	
20	Consistent discretizations as a road to Quantum Gravity <i>R. Gambini and J. Pullin</i>	378
21	The causal set approach to Quantum Gravity	393
0	J. Henson	
Qu	estions and answers	414
Pa	art V Effective models and Quantum Gravity phenomenology	425
22	C	427
	G. Amelino-Camelia	
23	Quantum Gravity and precision tests C. Burgess	450
24	0	
<i></i> _r	spacetime	466
	S. Majid	

Contents	ix
25 Doubly special relativity	493
J. Kowalski-Glikman	
26 From quantum reference frames to deformed special relativity	509
F. Girelli	
27 Lorentz invariance violation and its role in Quantum Gravity	
phenomenology	528
J. Collins, A. Perez and D. Sudarsky	
28 Generic predictions of quantum theories of gravity	548
L. Smolin	
Questions and answers	571
Index	580

Contributors

J. Ambjørn

The Niels Bohr Institute, Copenhagen University, Blegdamsvej 17, DK-2100 Copenhagen O, Denmark and

Institute for Theoretical Physics, Utrecht University, Leuvenlaan 4, NL-3584 CE Utrecht, The Netherlands

G. Amelino-Camelia

Dipartimento di Fisica, Universitá di Roma "La Sapienza", P.le A. Moro 2, 00185 Rome, Italy

T. Banks

Department of Physics, University of California, Santa Cruz, CA 95064, USA and

NHETC, Rutgers University, Piscataway, NJ 08854, USA

C. Burgess

Department of Physics & Astronomy, McMaster University, 1280 Main St. W, Hamilton, Ontario, Canada, L8S 4M1

and

Perimeter Institute for Theoretical Physics, 31 Caroline St. N, Waterloo N2L 2Y5, Ontario, Canada

J. Collins

Physics Department, Pennsylvania State University, University Park, PA 16802, USA

L. Crane

Mathematics Department, Kansas State University, 138 Cardwell Hall Manhattan, KS 66506-2602, USA

List of contributors

xi

O. Dreyer

Theoretical Physics, Blackett Laboratory, Imperial College London, London, SW7 2AZ, UK

L. Freidel

Perimeter Institute for Theoretical Physics, 31 Caroline St. N, Waterloo N2L 2Y5, Ontario, Canada

R. Gambini

Instituto de Física, Facultad de Ciencias, Iguá 4225, Montevideo, Uruguay

F. Girelli

SISSA, via Beirut 4, Trieste, 34014, Italy, and INFN, sezione di Trieste, Italy

J. Henson

Institute for Theoretical Physics, Utrecht University, Leuvenlaan 4, NL-3584 CE Utrecht, The Netherlands

G. Horowitz

Physics Department, University of California, Santa Barbara, CA 93106, USA

J. Jurkiewicz

Institute of Physics, Jagellonian University, Reymonta 4, PL 30-059 Krakow, Poland

J. Kowalski-Glikman Institute for Theoretical Physics, University of Wroclaw 50-204 Wroclaw, pl. M. Borna 9, Poland

E. Livine

Ecole Normale Supérieure de Lyon, 46 Allée d'Italie, 69364 Lyon Cedex 07, France

R. Loll

Institute for Theoretical Physics, Utrecht University, Leuvenlaan 4, NL-3584 CE Utrecht, The Netherlands

S. Majid

School of Mathematical Sciences, Queen Mary, University of London 327 Mile End Rd, London E1 4NS, UK and Perimeter Institute for Theoretical Physics, 31 Caroline St. N., Waterloo ON N2L 2Y5, Canada

F. Markopoulou Perimeter Institute for Theoretical Physics, 31 Caroline St. N., Waterloo ON N2L 2Y5, Canada

xii

List of contributors

D. Oriti

Max Planck Institute for Gravitational Physics, Am Mühlenberg 1, D 14476 Golm, Germany

R. Percacci

SISSA, via Beirut 4, Trieste, 34014, Italy, and INFN, sezione di Trieste, Italy

A. Perez

Centre de Physique Théorique, Unité Mixte de Recherche (UMR 6207) du CNRS et des Universités Aix-Marseille I, Aix-Marseille II, et du Sud Toulon-Var, laboratoire afilié à la FRUMAM (FR 2291), Campus de Luminy, 13288 Marseille, France

J. Polchinski

Department of Physics, University of California, Santa Barbara CA 93106, USA

J. Pullin

Department of Physics and Astronomy, Louisiana State University, Baton Rouge, LA 70803 USA

C. Rovelli

Centre de Physique Théorique, Unité Mixte de Recherche (UMR 6207) du CNRS et des Universités Aix-Marseille I, Aix-Marseille II, et du Sud Toulon-Var, laboratoire afilié à la FRUMAM (FR 2291), Campus de Luminy, 13288 Marseille, France

N. Savvidou

Theoretical Physics, Blackett Laboratory, Imperial College London, London SW7 2AZ, UK

L. Smolin

Perimeter Institute for Theoretical Physics, Waterloo N2J 2W9, Ontario, Canada and

Department of Physics, University of Waterloo, Waterloo N2L 3G1, Ontario, Canada

R. D. Sorkin

Perimeter Institute for Theoretical Physics, Waterloo N2J 2W9, Ontario, Canada

J. Stachel

CAS Physics, Boston University, 745 Commonwealth Avenue, MA 02215, USA

D. Sudarsky

Instituto de Ciencias Nucleares, Universidad Autónoma de México, A. P. 70-543, México D.F. 04510, México

List of contributors

xiii

W. Taylor

Massachusetts Institute of Technology, Lab for Nuclear Science and Center for Theoretical Physics, 77 Massachusetts Ave., Cambridge, MA 02139-4307, USA

T. Thiemann

Max-Planck-Institut für Gravitationsphysik, Albert-Einstein-Institut, Am Mühlenberg 1, D-14476 Golm, Germany and

Perimeter Institute for Theoretical Physics, 31 Caroline St. North, Waterloo N2L 2Y5, Ontario, Canada

G. 't Hooft

Institute for Theoretical Physics, Utrecht University, Leuvenlaan 4, NL-3584 CE Utrecht, The Netherlands

R. Williams

Department of Applied Mathematics and Theoretical Physics, Centre for Mathematical Sciences, University of Cambridge, Wilberforce Road, Cambridge CB3 0WA, UK

Preface

Quantum Gravity is a dream, a theoretical need and a scientific goal. It is a theory which still does not exist in complete form, but that many people claim to have had glimpses of, and it is an area of research which, at present, comprises the collective efforts of hundreds of theoretical and mathematical physicists.

This yet-to-be-found theory promises to be a more comprehensive and complete description of the gravitational interaction, a description that goes beyond Einstein's General Relativity in being possibly valid at all scales of distances and energy; at the same time it promises to provide a new and deeper understanding of the nature of space, time and matter.

As such, research in Quantum Gravity is a curious and exciting blend of rigorous mathematics and bold speculations, concrete models and general schemata, foundational questions and technical issues, together with, since recently, tentative phenomenological scenarios.

In the past three decades we have witnessed an amazing growth of the field of Quantum Gravity, of the number of people actively working in it, and consequently of the results achieved. This is due to the fact that some approaches to the problem started succeeding in solving outstanding technical challenges, in suggesting ways around conceptual issues, and in providing new physical insights and scenarios. A clear example is the explosion of research in string theory, one of the main candidates to a quantum theory of gravity, and much more. Another is the development of Loop Quantum Gravity, an approach that attracted much attention recently, due to its successes in dealing with many long standing problems of the canonical approach to Quantum Gravity. New techniques have been then imported to the field from other areas of theoretical physics, e.g. Lattice Gauge Theory, and influenced in several ways the birth or growth of even more directions in Quantum Gravity research, including for example discrete approaches. At the same time, Quantum Gravity has been a very fertile ground and a powerful motivation for developing

xvi

Preface

new mathematics as well as alternative ways of thinking about spacetime and matter, which in turn have triggered the exploration of other promising avenues toward a Quantum Gravity theory.

I think it is fair to say that we are still far from having constructed a satisfactory theory of Quantum Gravity, and that any single approach currently being considered is too incomplete or poorly understood, whatever its strengths and successes may be, to claim to have achieved its goal, or to have proven to be the only reasonable way to proceed.

On the other hand every single one of the various approaches being pursued has achieved important results and insights regarding the Quantum Gravity problem. Moreover, technical or conceptual issues that are unsolved in one approach have been successfully tackled in another, and often the successes of one approach have clearly come from looking at how similar difficulties had been solved in another.

It is even possible that, in order to achieve our common goal, formulate a complete theory of Quantum Gravity and unravel the fundamental nature of space and time, we will have to regard (at least some of) these approaches as different aspects of the same theory, or to develop a more complete and more general approach that combines the virtues of several of them. However strong faith one may have in any of these approaches, and however justified this may be in light of recent results, it should be expected, purely on historical grounds, that none of the approaches currently pursued will be understood in the future in the same way as we do now, even if it proves to be the right way to proceed. Therefore, it is useful to look for new ideas and a different perspective on each of them, aided by the the insights provided by the others. In no area of research a "dogmatic approach" is less productive, I feel, than in Quantum Gravity, where the fundamental and complex nature of the problem, its many facets and long history, combined with a dramatically (but hopefully temporarily) limited guidance from Nature, suggest a very open-minded attitude and a very critical and constant re-evaluation of one's own strategies.

I believe, therefore, that a broad and well-informed perspective on the various present approaches to Quantum Gravity is a necessary tool for advancing successfully in this area.

This collective volume, benefiting from the contributions of some of the best Quantum Gravity practitioners, all working at the frontiers of current research, is meant to represent a good starting point and an up-to-date support reference, for both students and active researchers in this fascinating field, for developing such a broader perspective. It presents an overview of some of the many ideas on the table, an introduction to several current approaches to the construction of a Quantum Theory of Gravity, and brief reviews of their main achievements, as well as of the many outstanding issues. It does so also with the aim of offering a comparative perspective on the subject, and on the different roads that Quantum Gravity researchers

Preface

are following in their searches. The focus is on non-perturbative aspects of Quantum Gravity and on the fundamental structure of space and time. The variety of approaches presented is intended to ensure that a variety of ideas and mathematical techniques will be introduced to the reader.

More specifically, the first part of the book (Part I) introduces the problem of Quantum Gravity, and raises some of the fundamental questions that research in Quantum Gravity is trying to address. These concern for example the role of locality and of causality at the most fundamental level, the possibility of the notion of spacetime itself being emergent, the possible need to question and revise our way of understanding both General Relativity and Quantum Mechanics, before the two can be combined and made compatible in a future theory of Quantum Gravity. It provides as well suggestions for new directions (using the newly available tools of category theory, or quantum information theory, etc.) to explore both the construction of a quantum theory of gravity, as well as our very thinking about space and time and matter.

The core of the book (Parts II–IV) is devoted to a presentation of several approaches that are currently being pursued, have recently achieved important results, and represent promising directions. Among these the most developed and most practiced are string/M-theory, by far the one which involves at present the largest amount of scholars, and loop quantum gravity (including its covariant version, i.e. spin foam models). Alongside them, we have various (and rather different in both spirit and techniques used) discrete approaches, represented here by simplicial quantum gravity, in particular the recent direction of causal dynamical triangulations, quantum Regge calculus, and the "consistent discretization scheme", and by the causal set approach.

All these approaches are presented at an advanced but not over-technical level, so that the reader is offered an introduction to the basic ideas characterizing any given approach as well as an overview of the results it has already achieved and a perspective on its possible development. This overview will make manifest the variety of techniques and ideas currently being used in the field, ranging from continuum/analytic to discrete/combinatorial mathematical methods, from canonical to covariant formalisms, from the most conservative to the most radical conceptual settings.

The final part of the book (Part V) is devoted instead to effective models of Quantum Gravity. By this we mean models that are not intended to be of a fundamental nature, but are likely to provide on the one hand key insights on what sort of features the more fundamental formulation of the theory may possess, and on the other powerful tools for studying possible phenomenological consequences of any Quantum Gravity theory, the future hopefully complete version as well

xvii

xviii

Preface

as the current tentative formulations of it. The subject of Quantum Gravity phenomenology is a new and extremely promising area of current research, and gives ground to the hope that in the near future Quantum Gravity research may receive experimental inputs that will complement and direct mathematical insights and constructions.

The aim is to convey to the reader the recent insight that a Quantum Gravity theory need not be forever detached by the experimental realm, and that many possibilities for a Quantum Gravity phenomenology are instead currently open to investigation.

At the end of each part, there is a "Questions & Answers" session. In each of them, the various contributors ask and put forward to each other questions, comments and criticisms to each other, which are relevant to the specific topic covered in that part. The purpose of these Q&A sessions is fourfold: (a) to clarify further subtle or particularly relevant features of the formalisms or perspectives presented; (b) to put to the forefront critical aspects of the various approaches, including potential difficulties or controversial issues; (c) to give the reader a glimpse of the real-life, ongoing debates among scholars working in Quantum Gravity, of their different perspectives and of (some of) their points of disagreement; (d) in a sense, to give a better picture of how science and research (in particular, Quantum Gravity research) really work and of what they really are.

Of course, just as the book as a whole cannot pretend to represent a complete account of what is currently going on in Quantum Gravity research, these Q&A sessions cannot really be a comprehensive list of relevant open issues nor a faithful portrait of the (sometimes rather heated) debate among Quantum Gravity researchers.

What this volume makes manifest is the above-mentioned impressive development that occurred in the field of Quantum Gravity as a whole, over the past, say, 20–30 years. This is quickly recognized, for example, by comparing the range and content of the following contributed papers to the content of similar collective volumes, like *Quantum Gravity 2: a second Oxford symposium*, C. Isham, ed., Oxford University Press (1982), *Quantum structure of space and time*, M. Duff, C. Isham, eds., Cambridge University Press (1982), *Quantum Theory of Gravity, essays in honor of the 60th Birthday of Bryce C DeWitt*, S. D. Christensen, ed., Taylor and Francis (1984), or even the more recent *Conceptual problems of Quantum Gravity*, A. Ashtekar, J. Stachel, eds., Birkhauser (1991), all presenting overviews of the status of the subject at their time. Together with the persistence of the Quantum Gravity problem itself, and of the great attention devoted, currently just as then, to foundational issues alongside the more technical ones, it will be impossible not to notice the greater variety of current approaches, the extent to which researchers have explored beyond the traditional ones, and, most important, the

Preface

xix

enormous amount of progress and achievements in each of them. Moreover, the very existence of research in Quantum Gravity phenomenology was un-imaginable at the time.

Quantum Gravity remains, as it was in that period, a rather esoteric subject, within the landscape of theoretical physics at large, but an active and fascinating one, and one of fundamental significance. The present volume is indeed a collective report from the frontiers of theoretical physics research, reporting on the latest and most exciting developments but also trying to convey to the reader the sense of intellectual adventure that working at such frontiers implies.

It is my pleasure to thank all those that have made the completion of this project possible. First of all, I gratefully thank all the researchers who have contributed to this volume, reporting on their work and on the work of their colleagues in such an excellent manner. This is a collective volume, and thus, if it has any value, it is solely due to all of them. Second, I am grateful to all the staff at the Cambridge University Press, and in particular to Simon Capelin, for supporting this project since its conception, and for guiding me through its development. Last, I would like to thank, for very useful comments, suggestions and advice, several colleagues and friends: John Baez, Fay Dowker, Sean Hartnoll, Chris Isham, Prem Kumar, Pietro Massignan, and especially Ted Jacobson.

Daniele Oriti