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978-0-521-85442-9 - Random Networks for Communication: From Statistical Physics to Information Systems

Massimo Franceschetti and Ronald Meester

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