

Index

BOLD face page entries indicate definitions, statement of theorems, etc, or clarification of notations. Index entries for the most important symbols appear on this page: the alphabetized index begins overleaf.

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