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978-0-521-84767-4 - Probability and Statistics by Example: II Markov Chains: a Primer in Random Processes and their Applications

Yuri Suhov and Mark Kelbert

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