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978-0-521-83821-4 — Equivalence and Duality for Module Categories with Tilting
and Cotilting for Rings

Robert R. Colby, Kent R. Fuller

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